

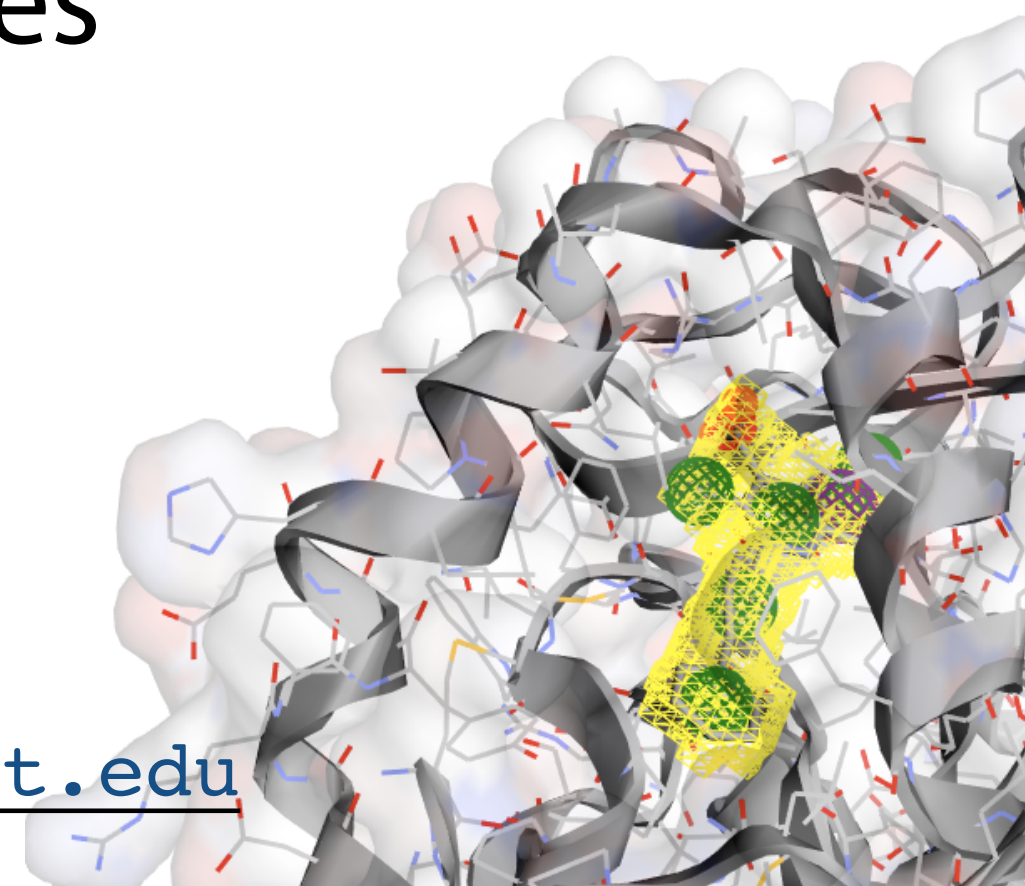


# Computational Drug Discovery

David Ryan Koes

11/6/2018

<http://bits.csb.pitt.edu>



# What is a drug?

*According to the Food, Drug, and Cosmetic Act* (1) : a substance recognized in an official pharmacopoeia or formulary (2) : a substance intended for use in the diagnosis, cure, mitigation, treatment, or prevention of disease (3) : **a substance** other than food **intended to affect the structure or function** of the body (4) : a substance intended for use as a component of a medicine but not a device or a component, part, or accessory of a device

<http://www.merriam-webster.com/dictionary/drug>

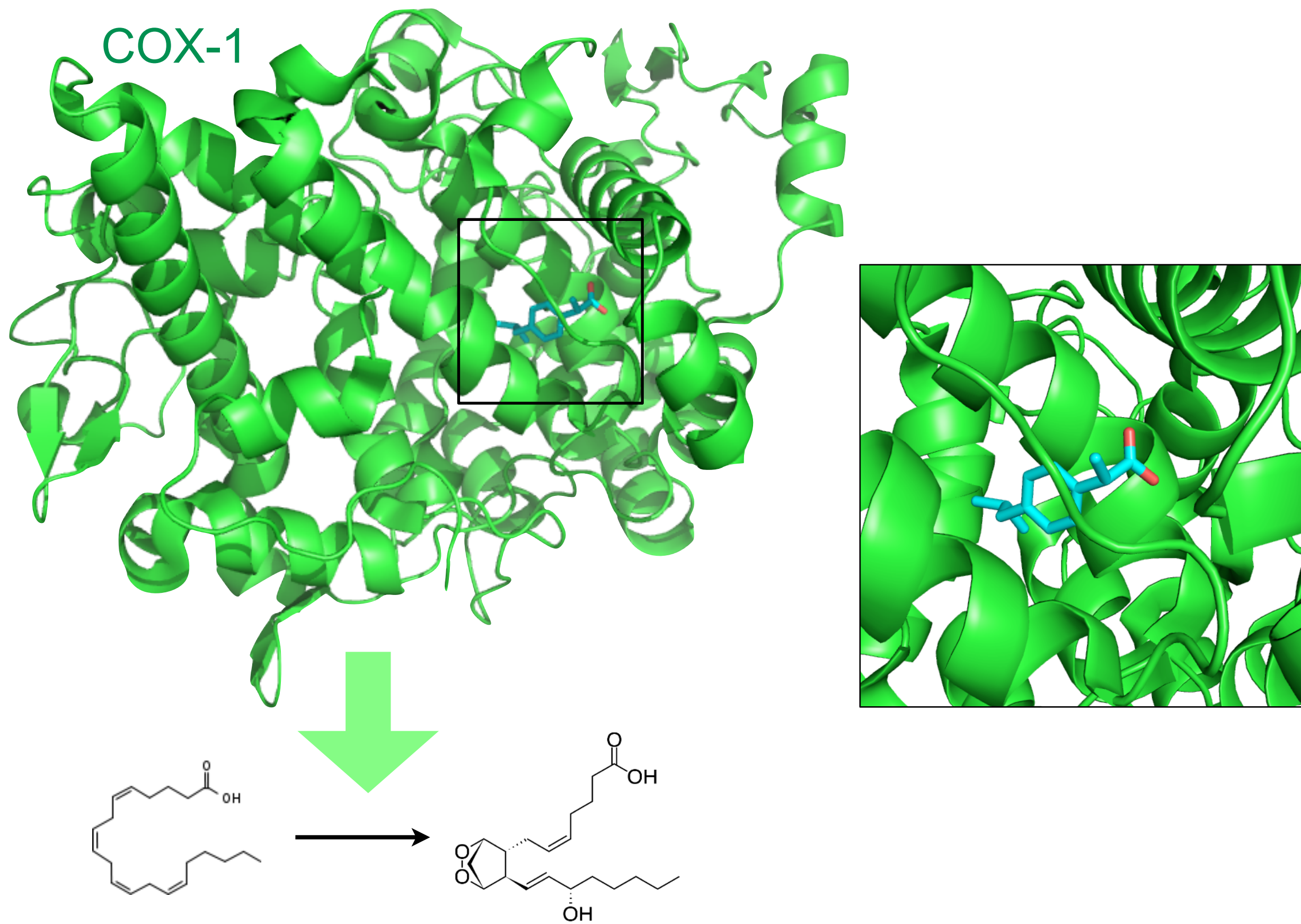


# What is a drug?

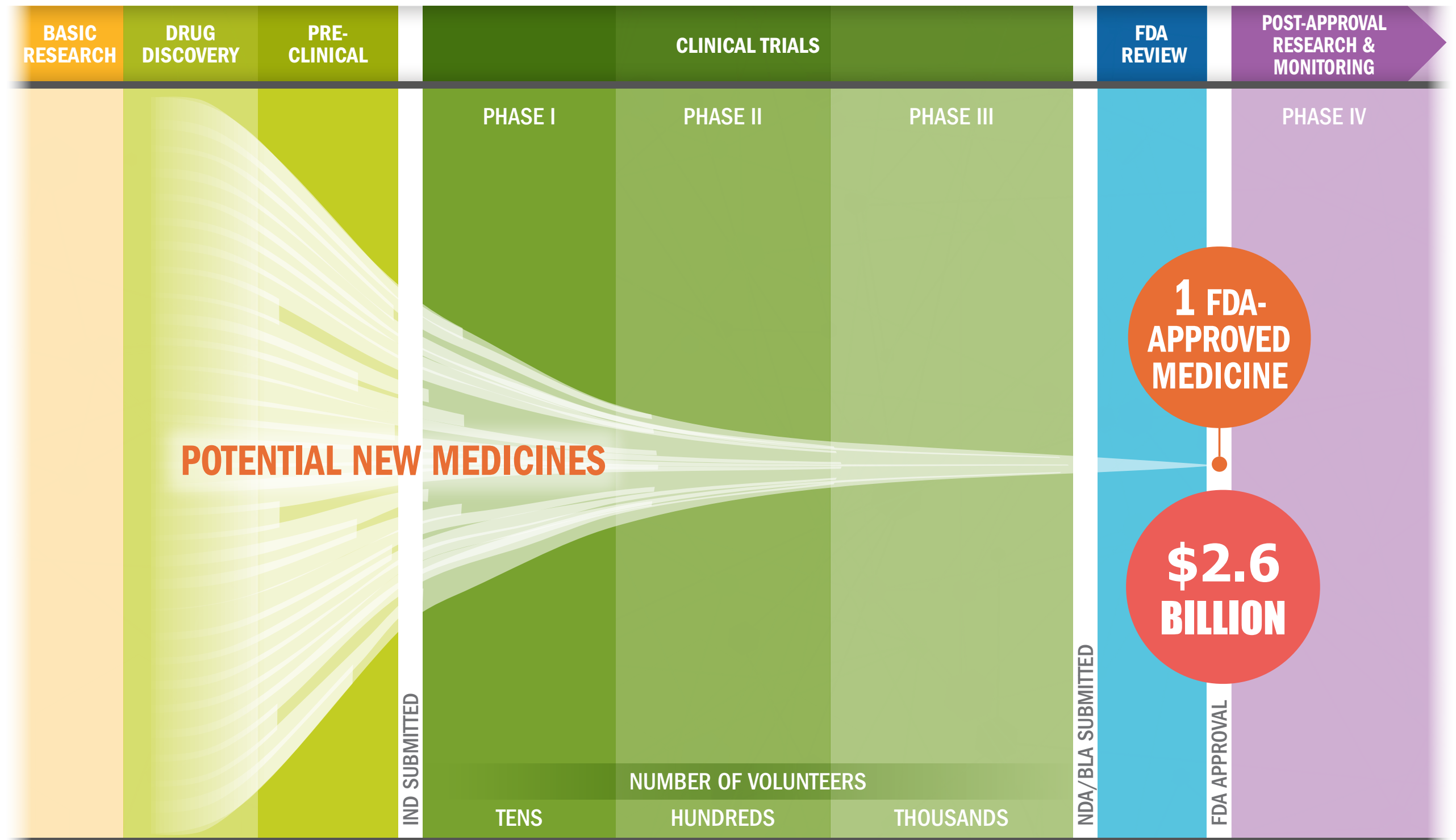
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<http://www.merriam-webster.com/dictionary/drug>

*A **small molecule** intended to affect the structure/function of macromolecules*

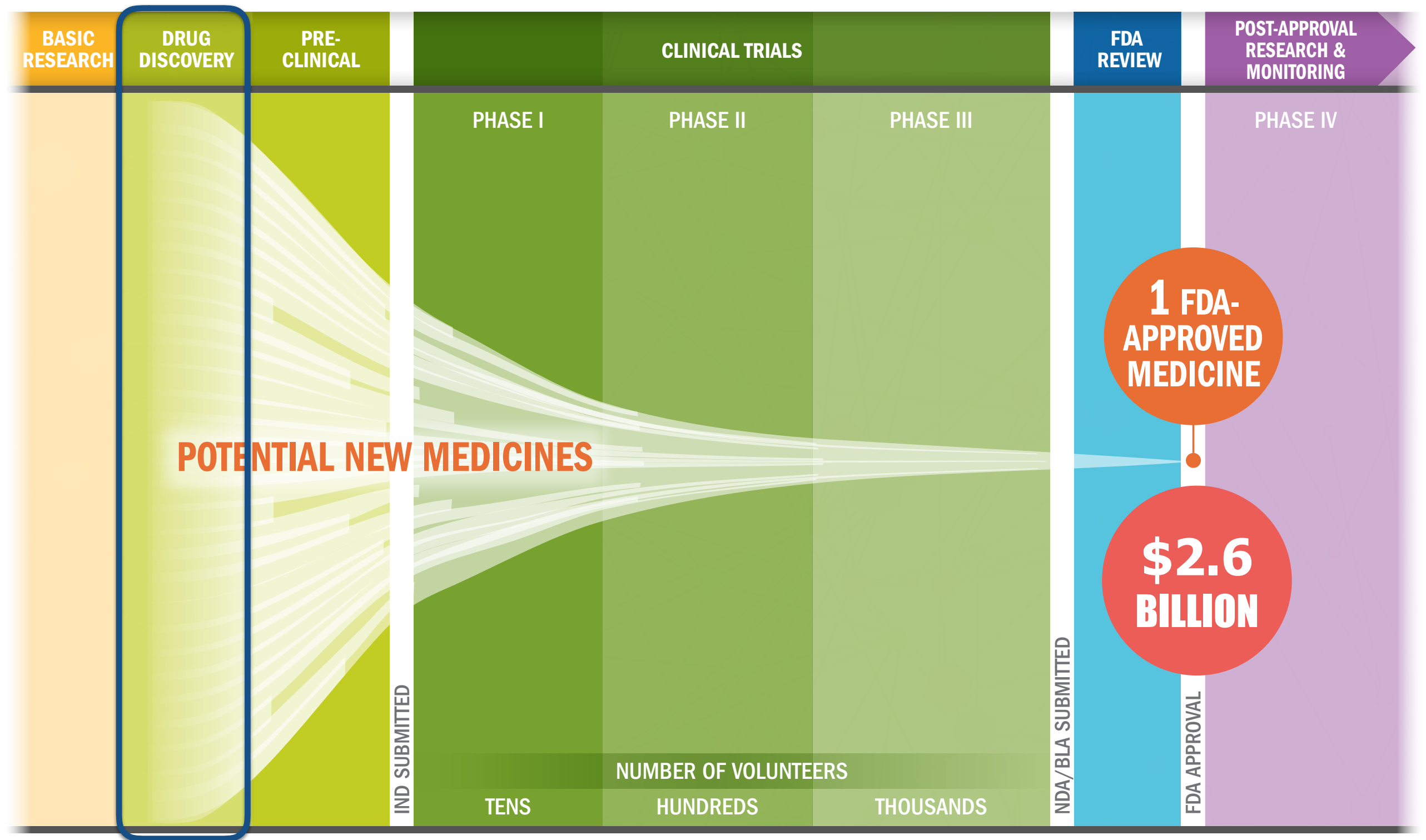


# THE BIOPHARMACEUTICAL RESEARCH AND DEVELOPMENT PROCESS



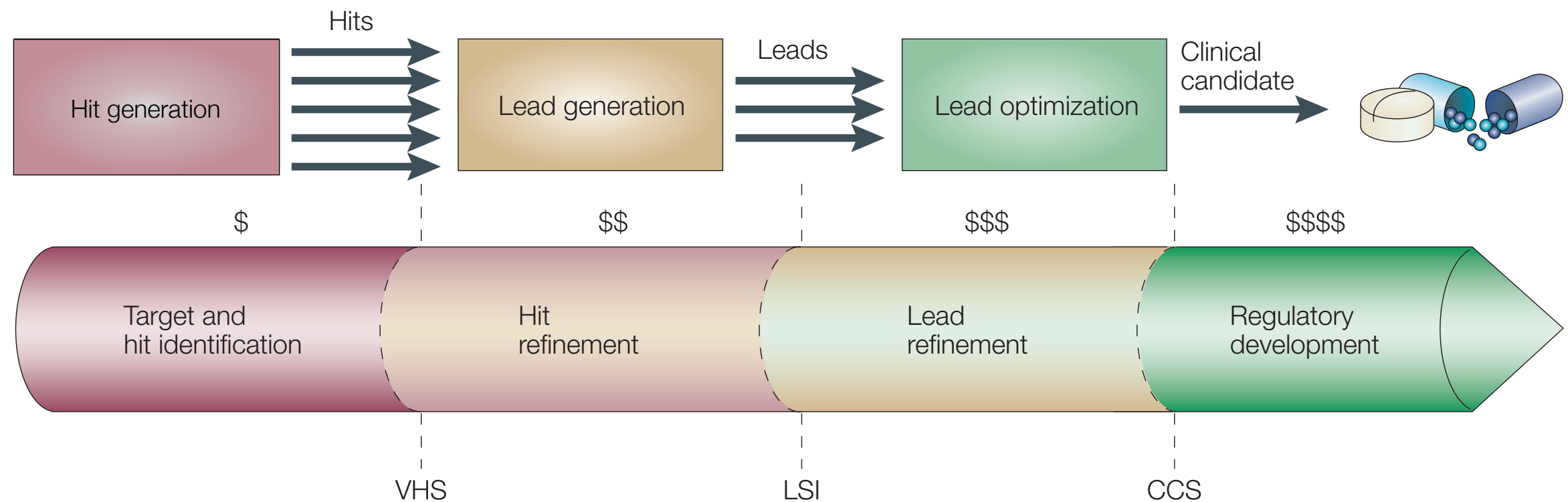
Source: Pharmaceutical Research and Manufacturers of America (<http://phrma.org>)

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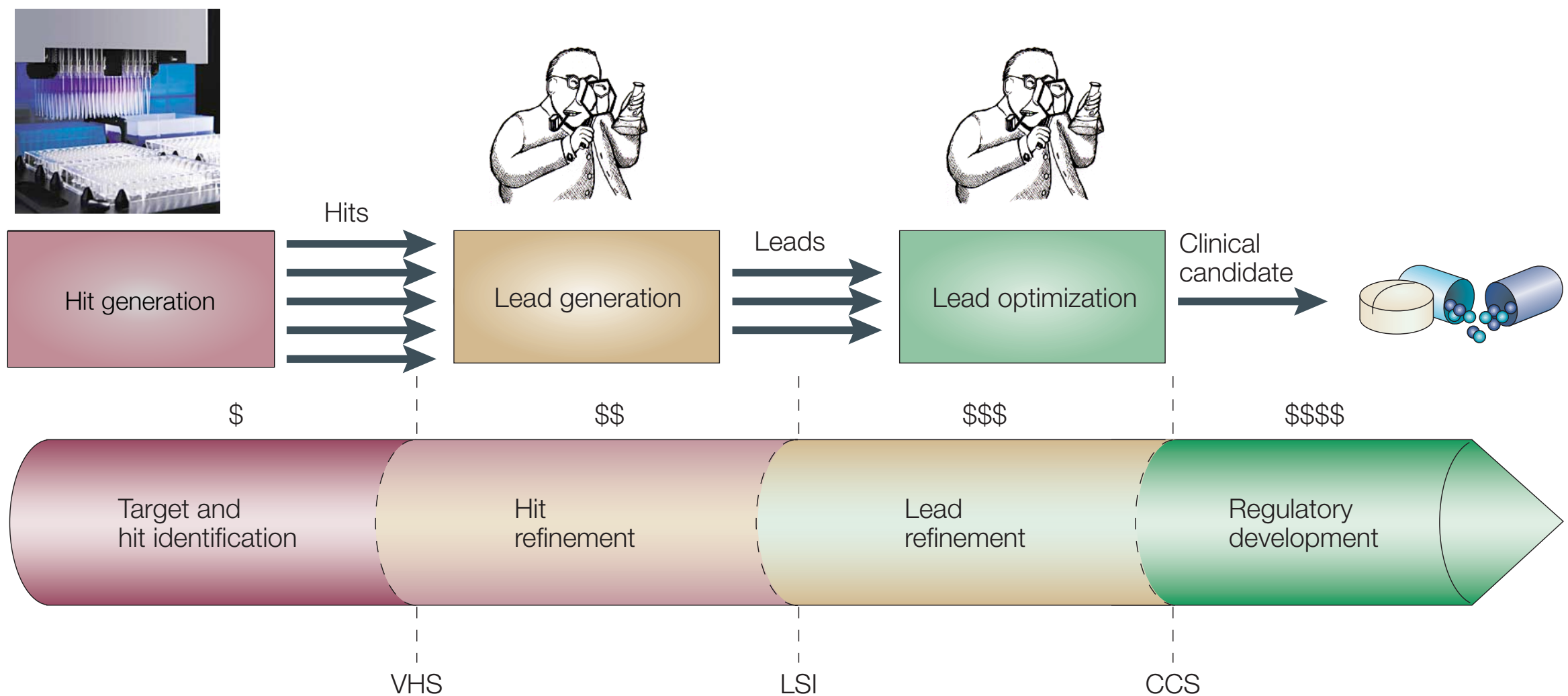
# Drug Discovery





# Drug Discovery

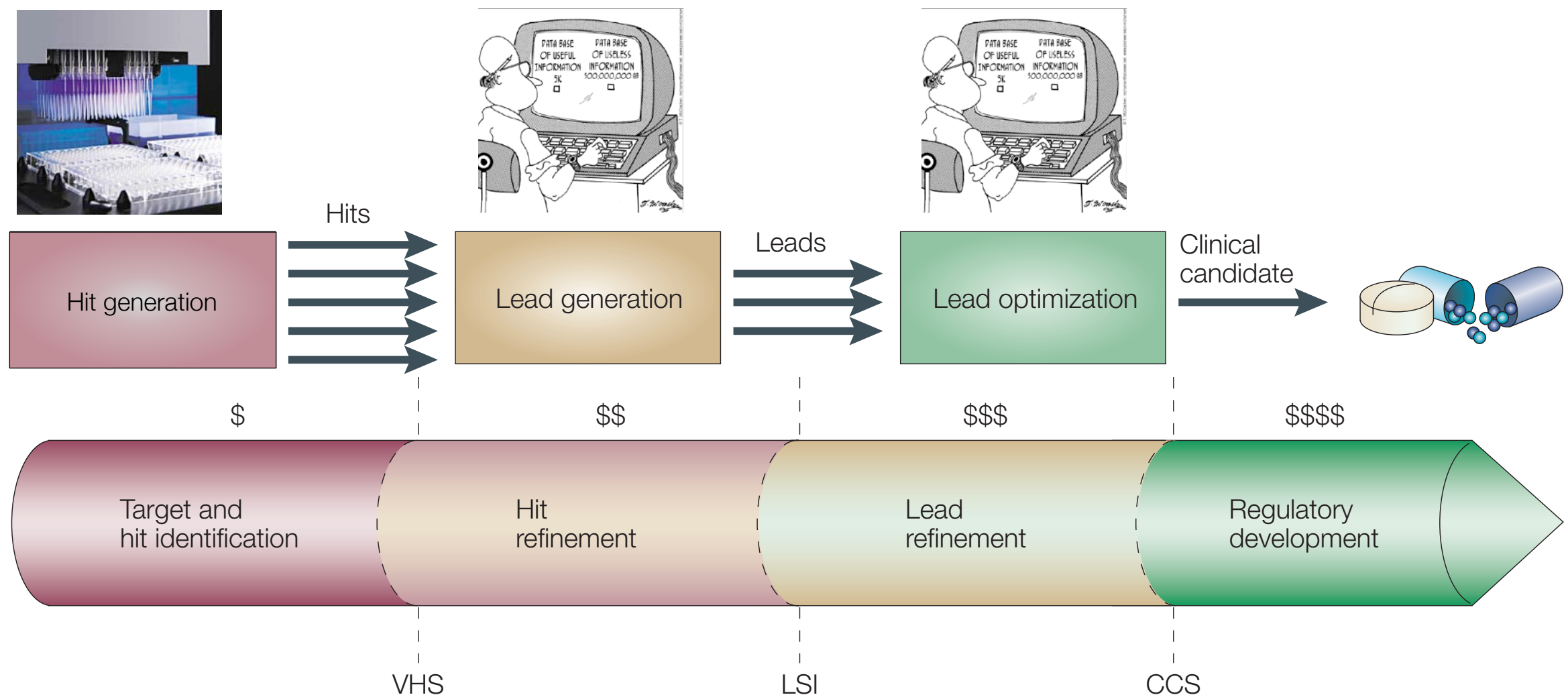
## High Throughput Screening





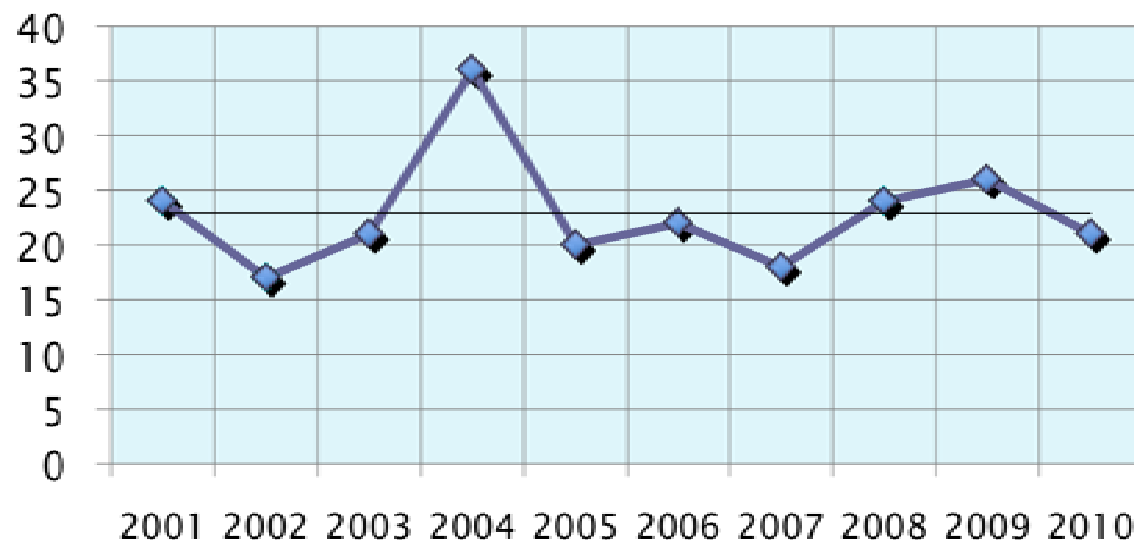
# Drug Discovery

## High Throughput Screening

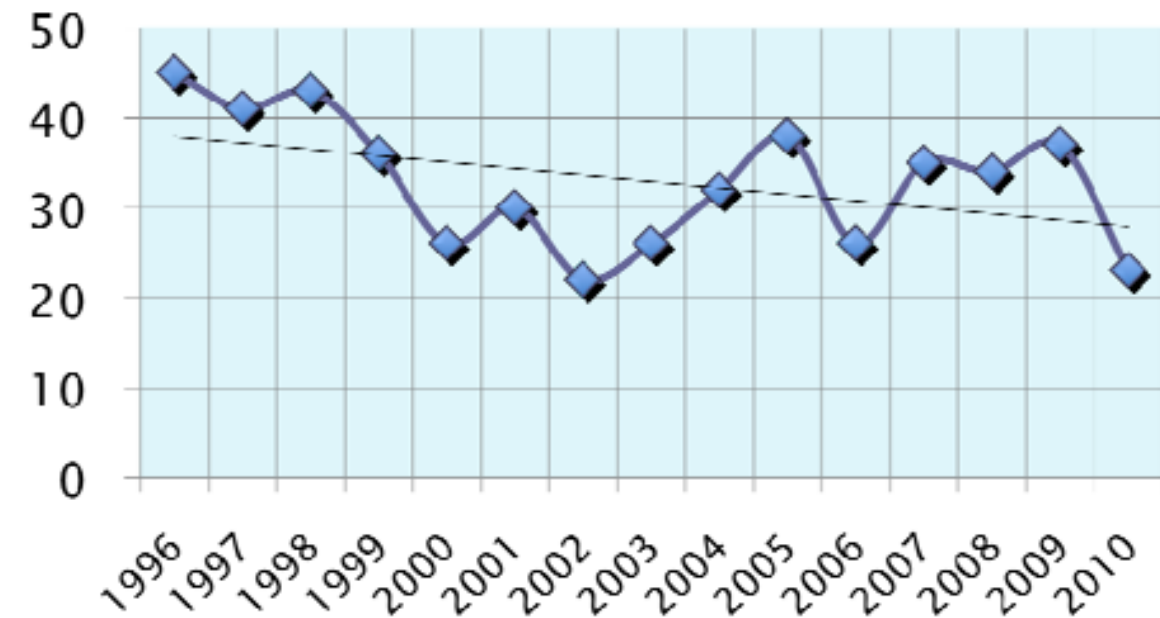


# The State of Drug Development

## New Drugs Approved



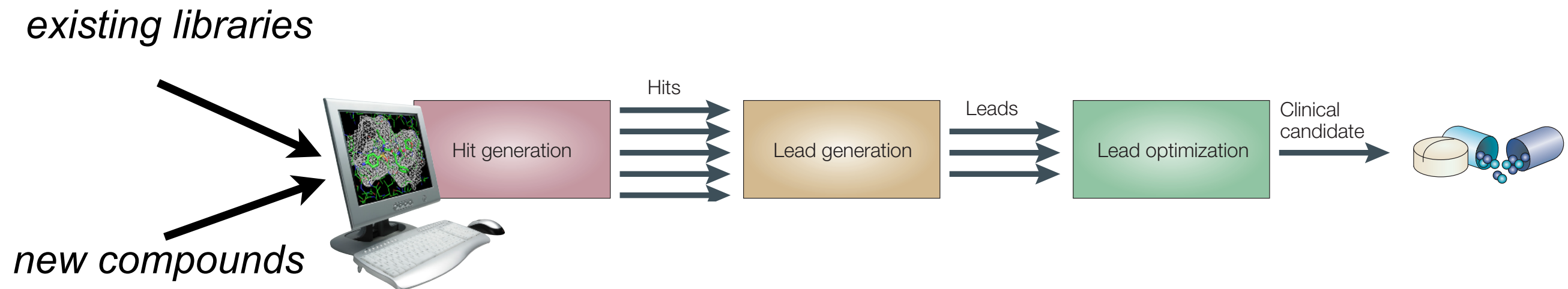
## New Drug Applications



<http://www.fda.gov/downloads/AboutFDA/Transparency/Basics/UCM247465.pdf>

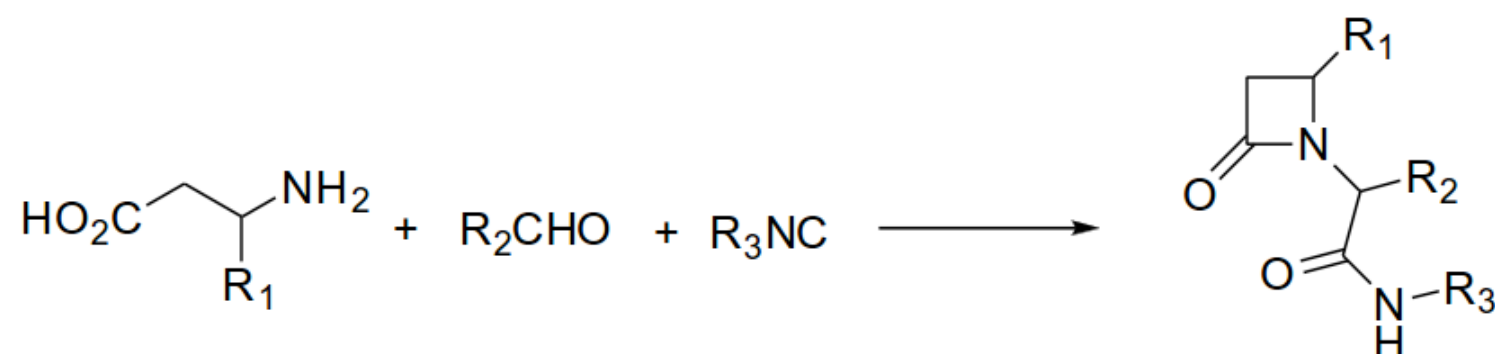
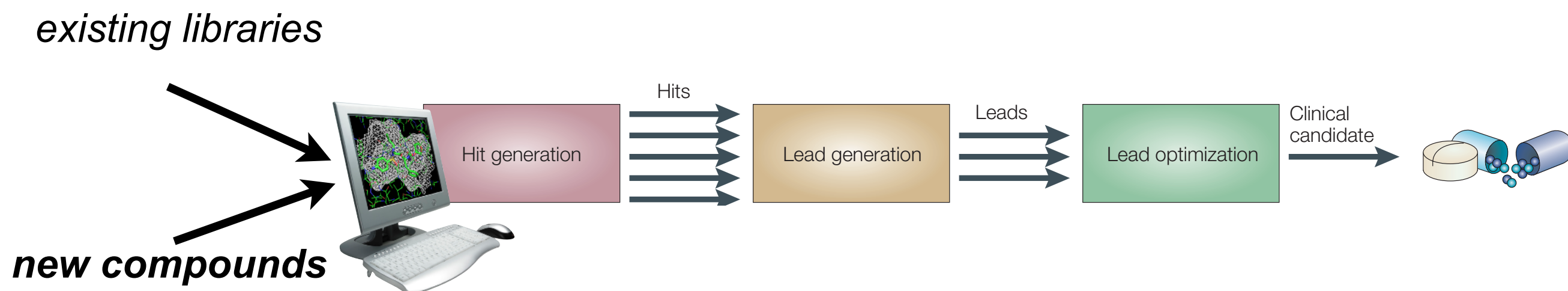
# Computational Drug Discovery

## Virtual Screening



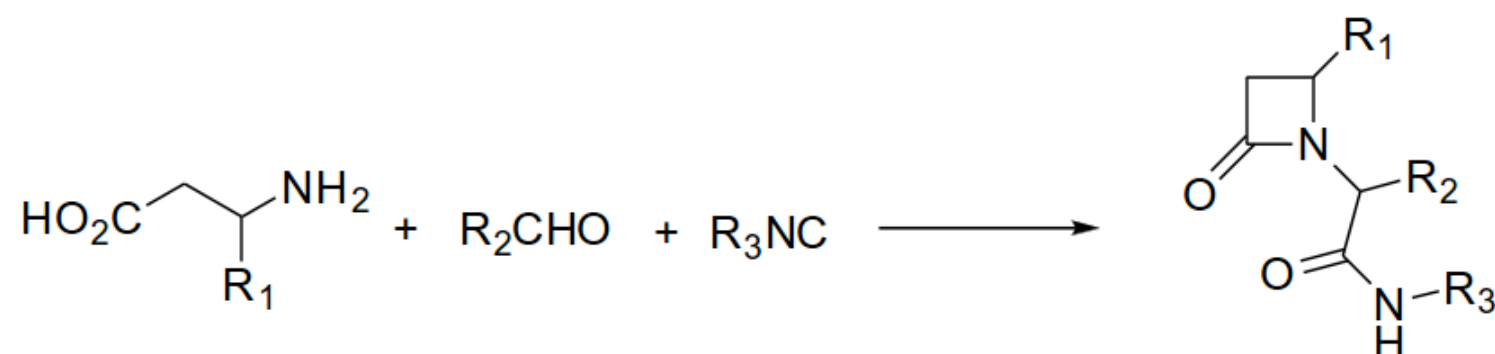
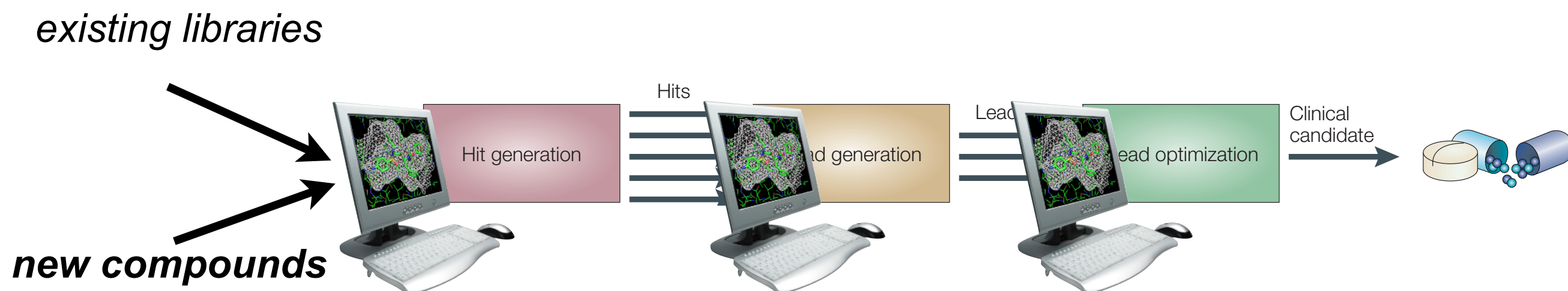
# Computational Drug Discovery

## Virtual Screening



# Computational Drug Discovery

## Virtual Screening



# Kinds of Virtual Screening

## **ADMET**

### Ligand Based

- similarity to known binder
- QSAR
- pharmacophore

### Receptor Based

- dock and score
- simulation

MM/GBSA, MM/PBSA, thermodynamic integration, free energy perturbation, Jarzynski, umbrella sampling, Monte Carlo, weighted ensemble, metadynamics...



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Not going to cover today



# ADMET

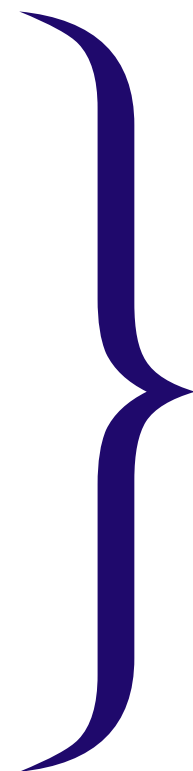
Absorption

Distribution

Metabolism

Excretion

Toxicity



Will this be a usable drug?

## Screening for ADMET:

*Cytochrome P450 interaction*

*Lipinski's Rule of Five*

*QSPR: Quantitative Structure*

*Property Relationship*

# Kinds of Virtual Screening

ADMET

## **Ligand Based**

- similarity to known binder
- QSAR
- pharmacophore

## Receptor Based

- dock and score

# Ligand Based: Similarity

## Fingerprint Methods

- map molecules to a descriptor space:

1D: molecule weight, #h-bonds, etc.

2D: paths, bond distances between atom-pairs



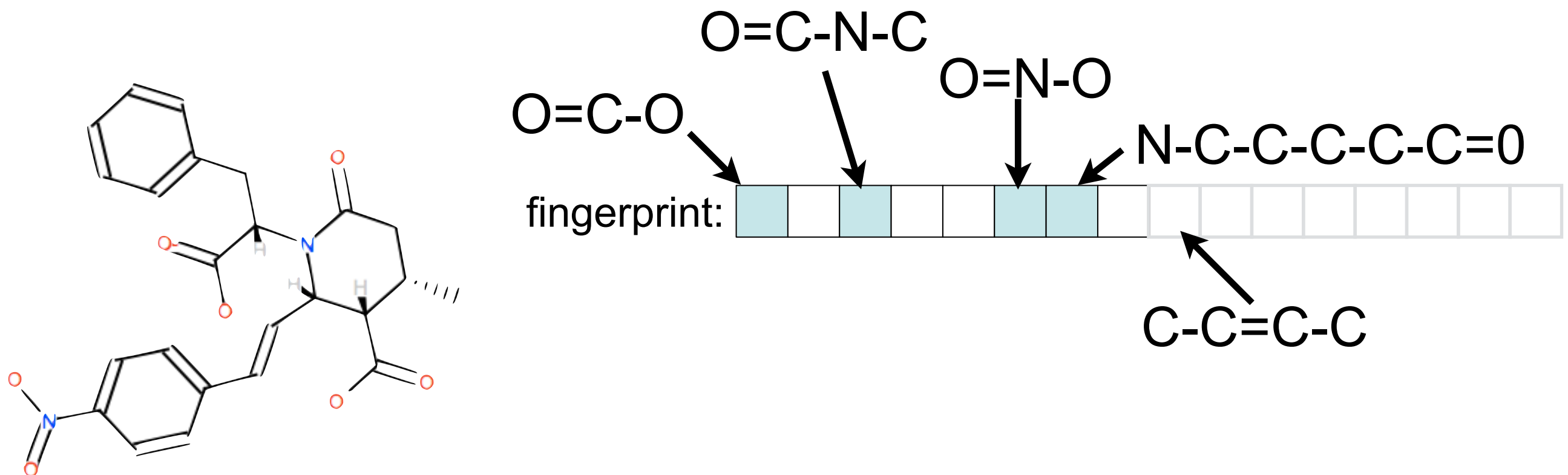
- similarity is “distance” between descriptors
- for bit vectors, Tanimoto distance used

$$T(A, B) = \frac{|A \cap B|}{|A \cup B|}$$

# Topological Fingerprints

## Daylight/FP2 Fingerprints

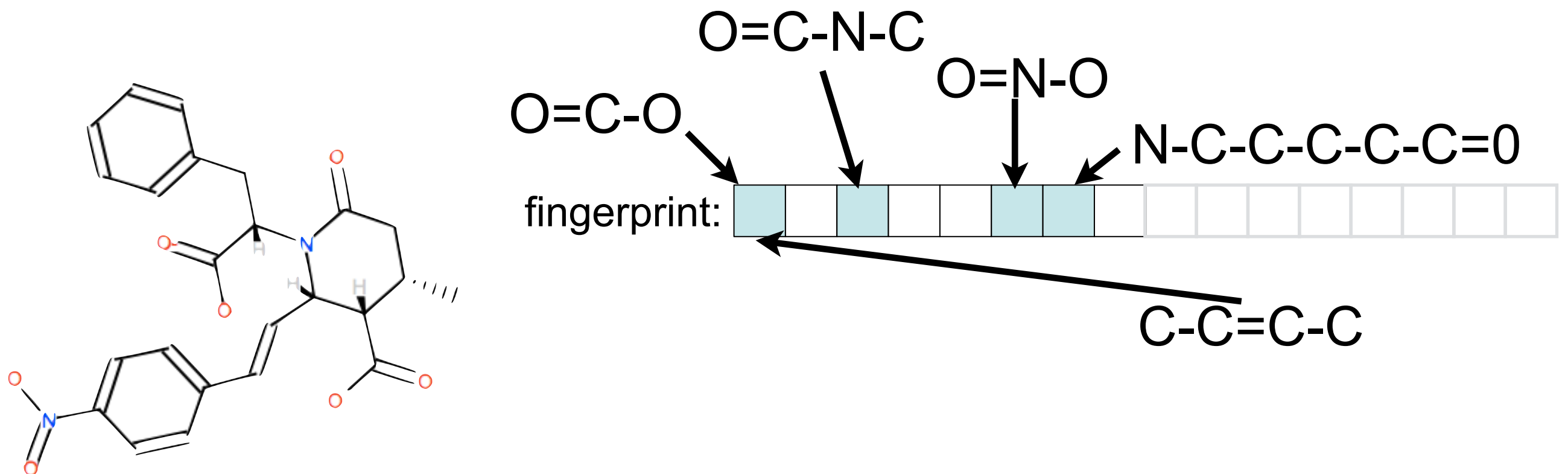
- all paths up to 7 bonds long
- each path corresponds to bit position (**hashing**)
- fast similarity checking (Tanimoto)



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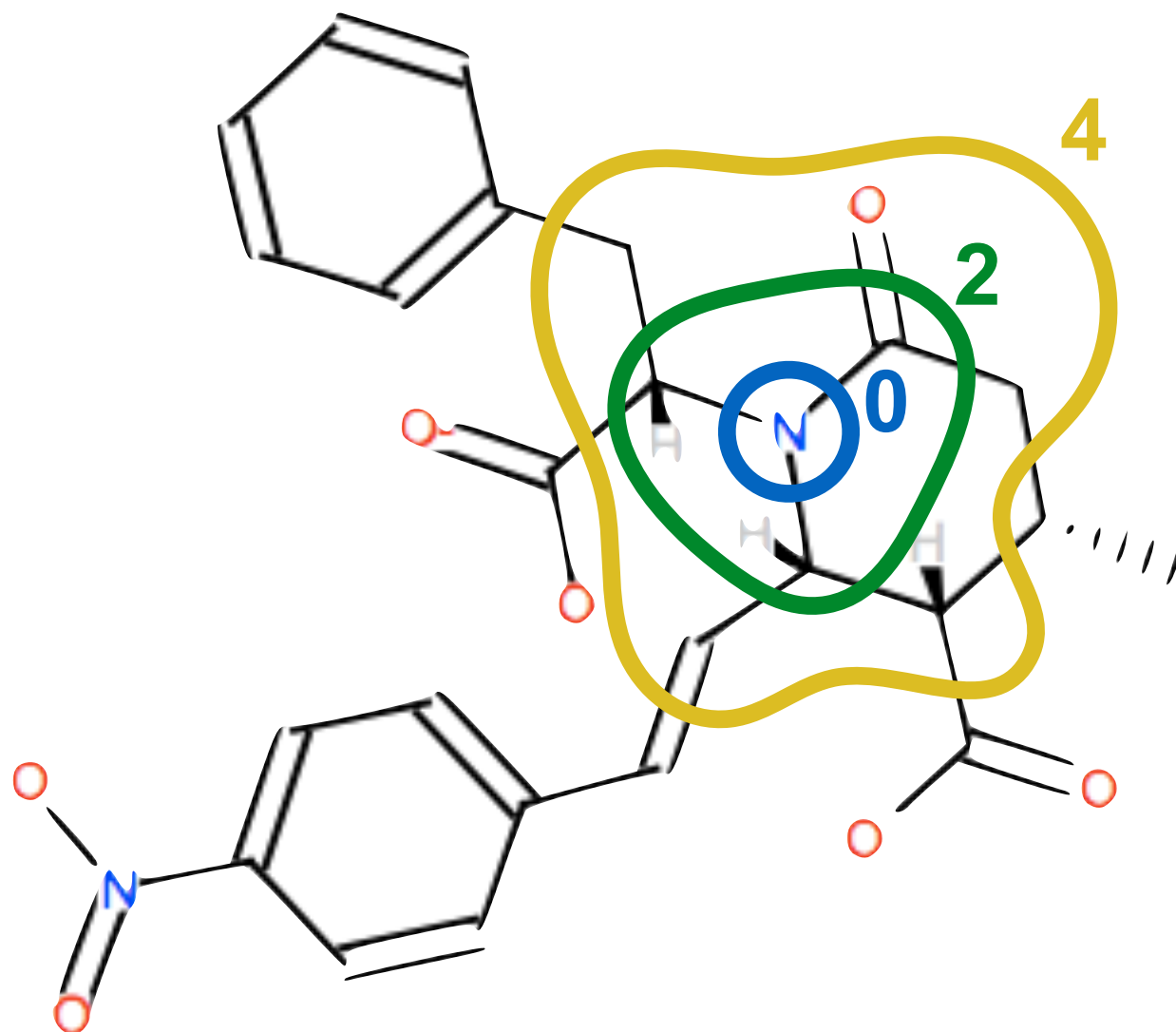




# Topological Fingerprints

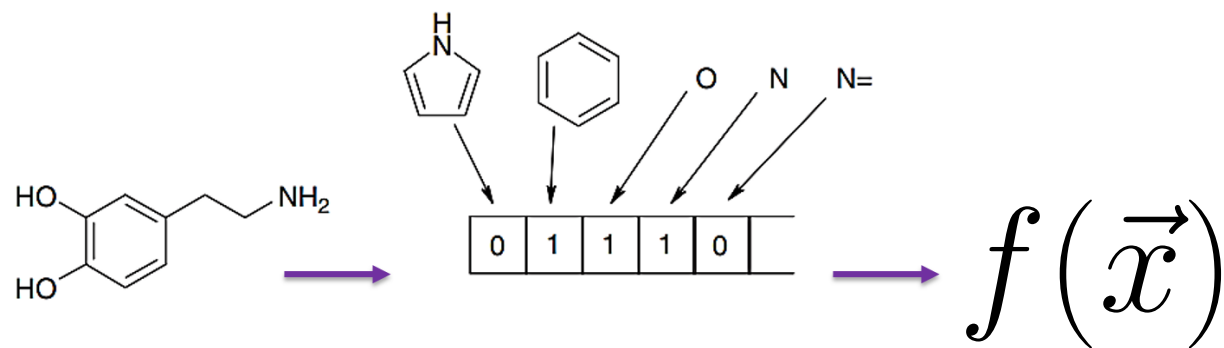
## ECFP4

- all substructures with diameter 4 around every atom

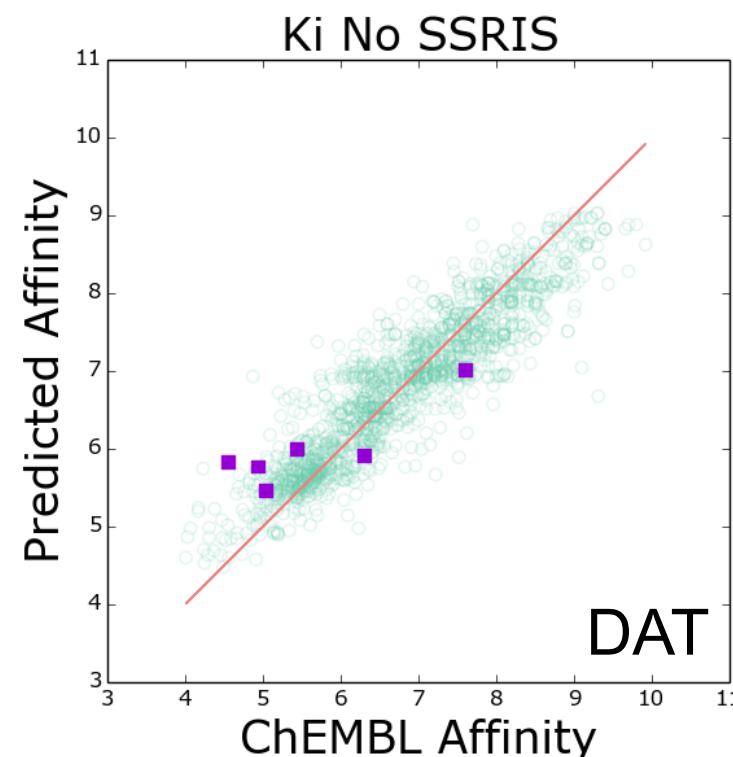
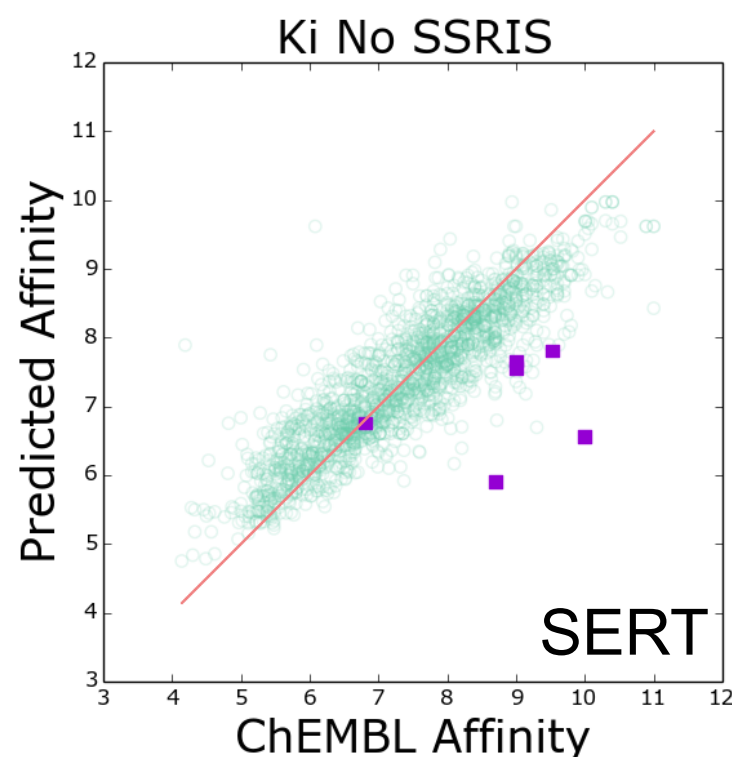
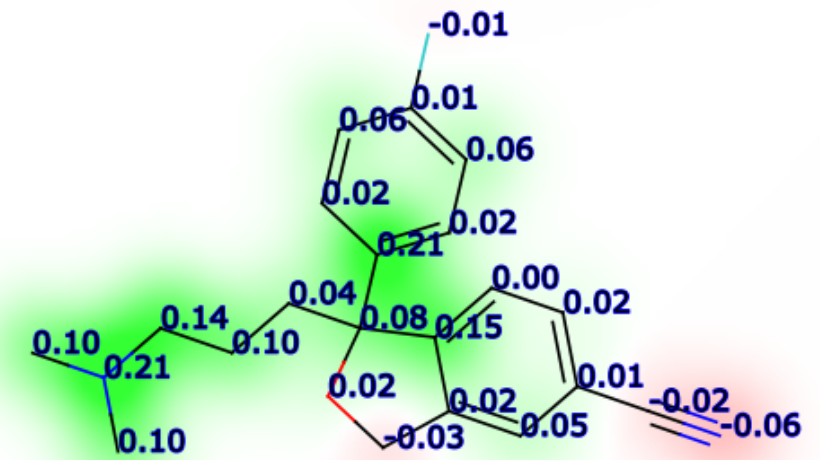


# Ligand Based: QSAR

## Quantitative Structure/Activity Relationships



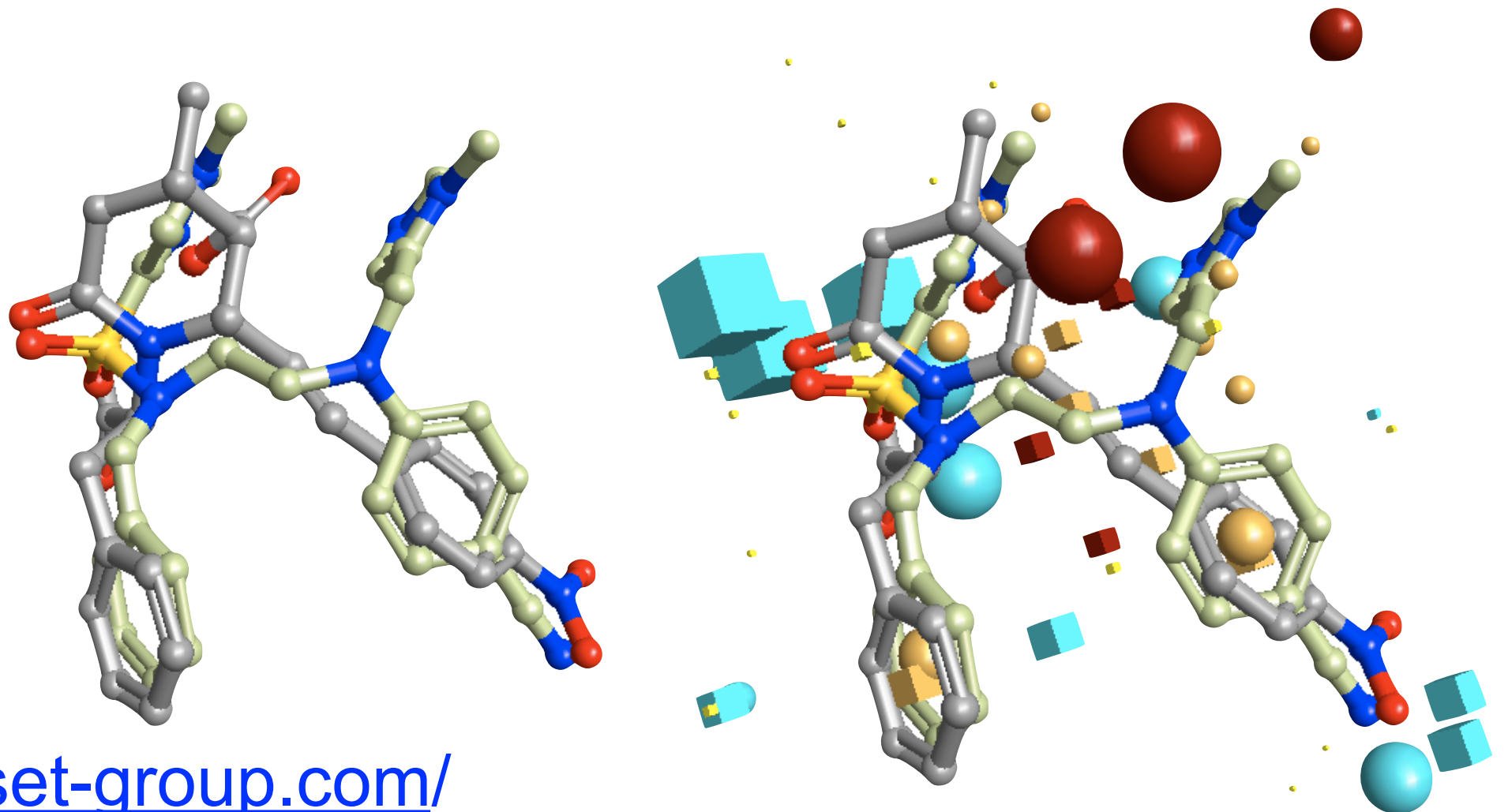
$$f(\vec{x}) = w_1\vec{x}_1 + w_2\vec{x}_2 + w_3\vec{x}_3 + \dots + b$$



# Ligand Based: Similarity

## Superposition Methods

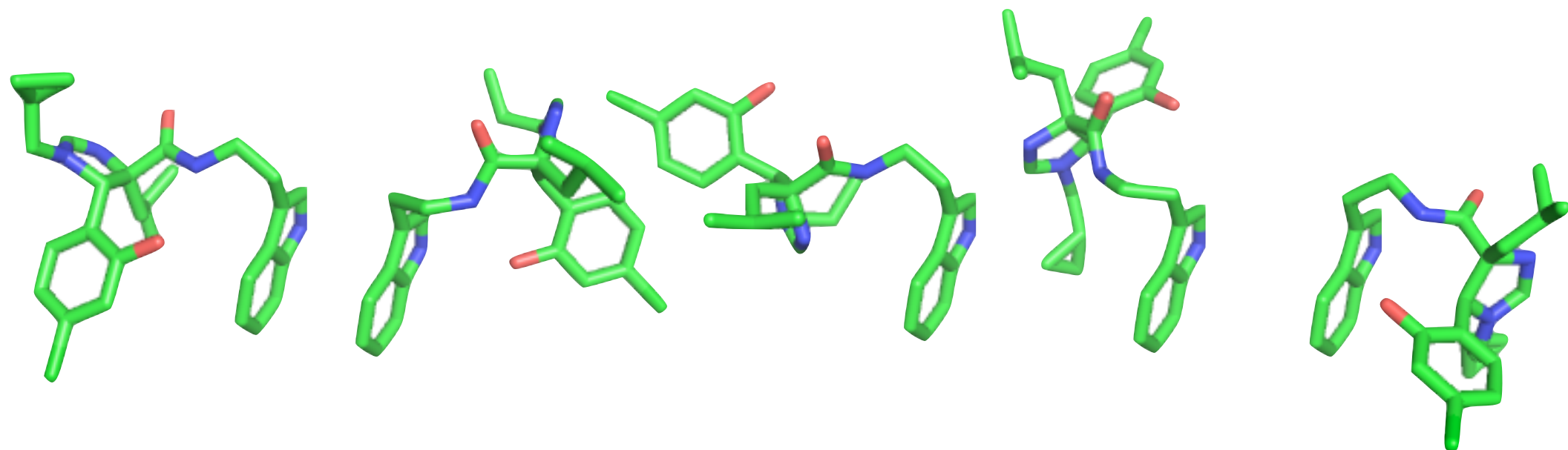
- compute “overlap” between molecules
- consider shape, electrostatics, **pharmacophores**



# Representing Compounds

## Conformations

A single compound has many different shapes



Choices: Store sampling of explicit conformations, search for a good conformation, ignore conformations (2D only)

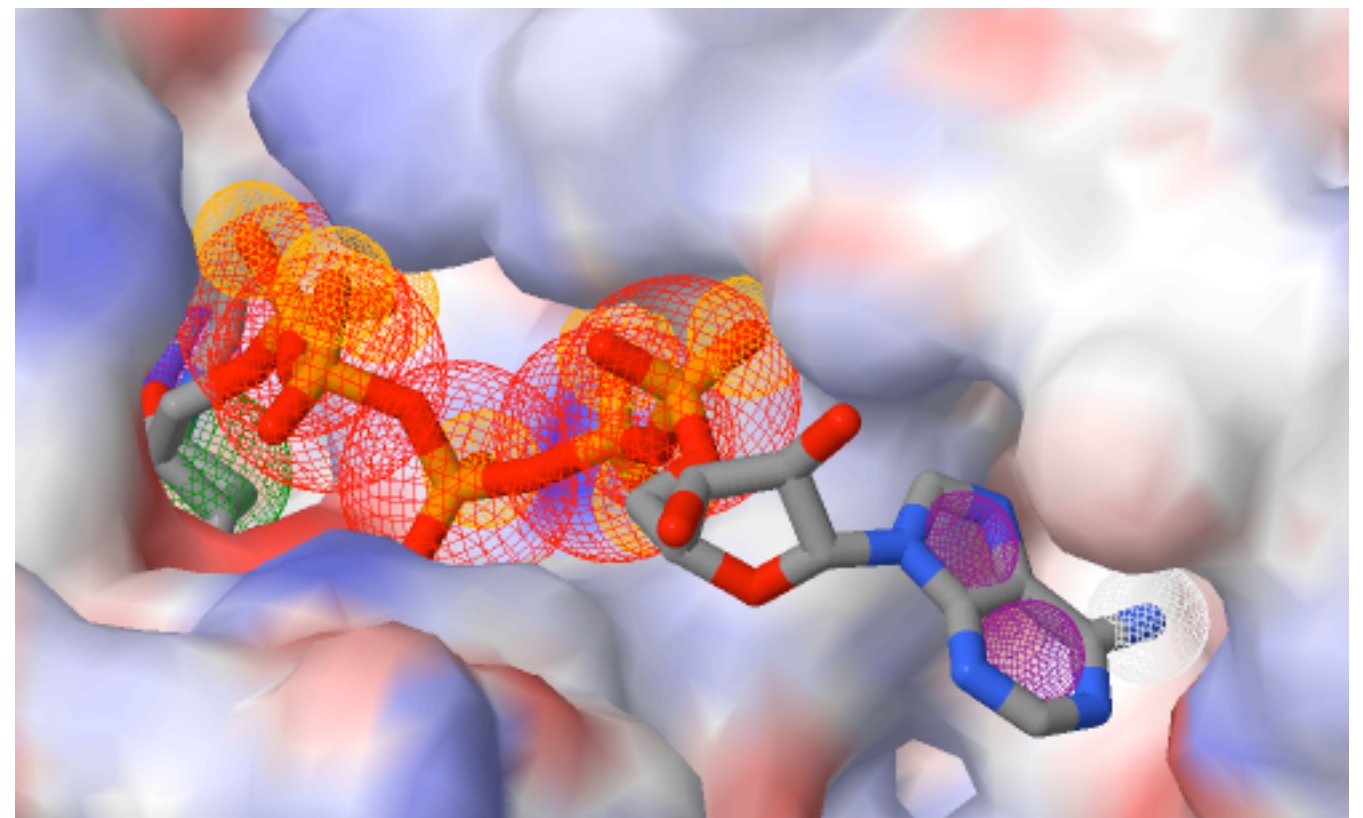
# Ligand Based: Pharmacophore

## Pharmacophore:

IUPAC: The ensemble of steric and electronic features that is necessary to ensure the optimal supra-molecular interactions with a specific biological target structure and to trigger (or to block) its biological response.

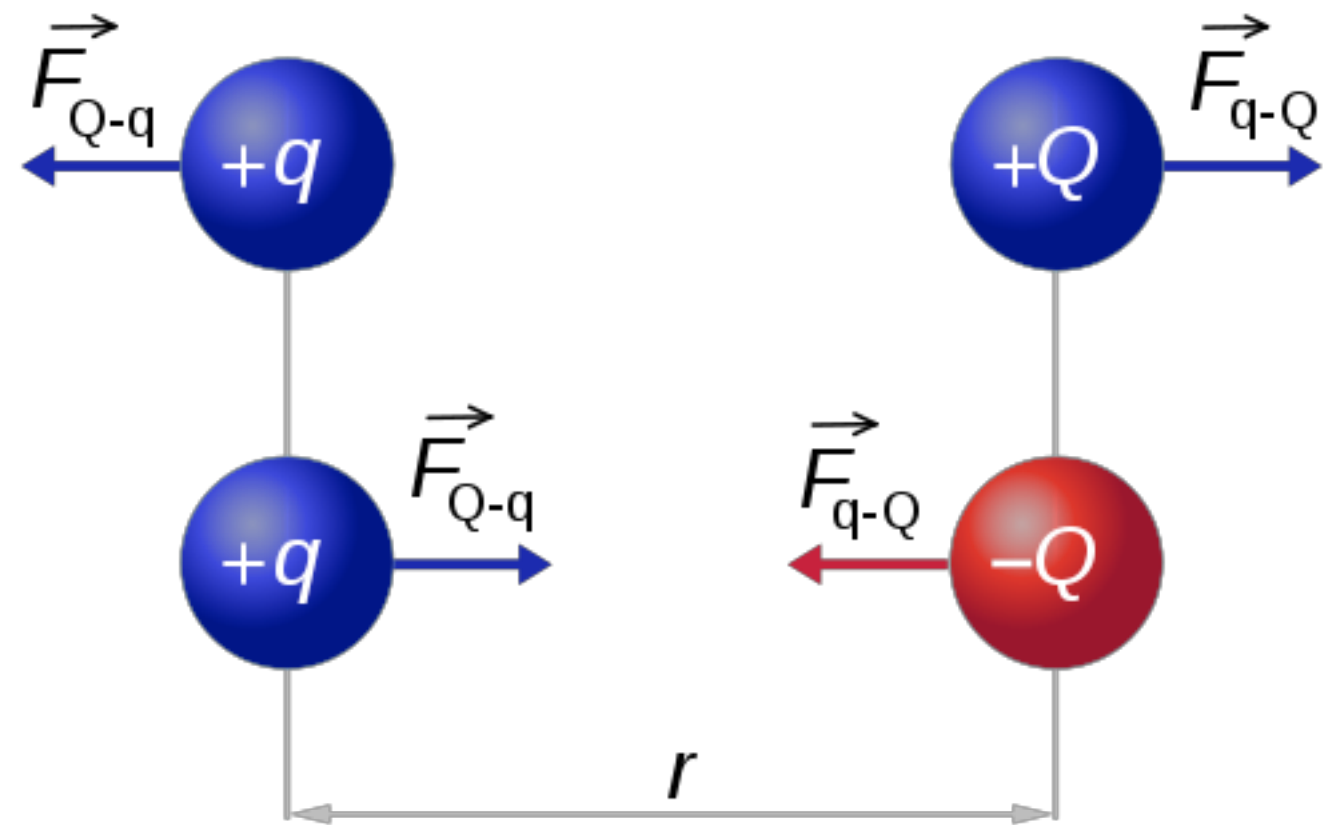
### Common Features:

- aromatic ring
- hydrophobic area
- positive ionizable
- negative ionizable
- hydrogen bond donor
- hydrogen bond acceptor

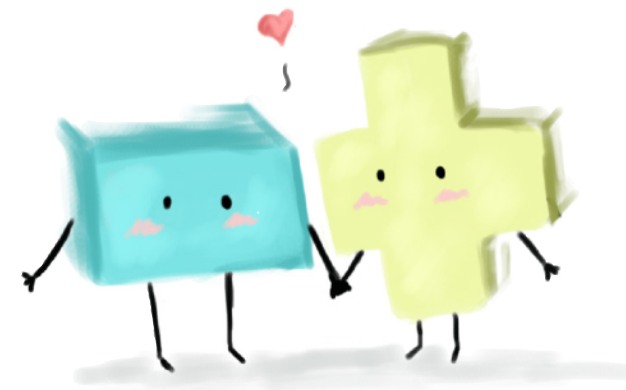




# Charge-Charge

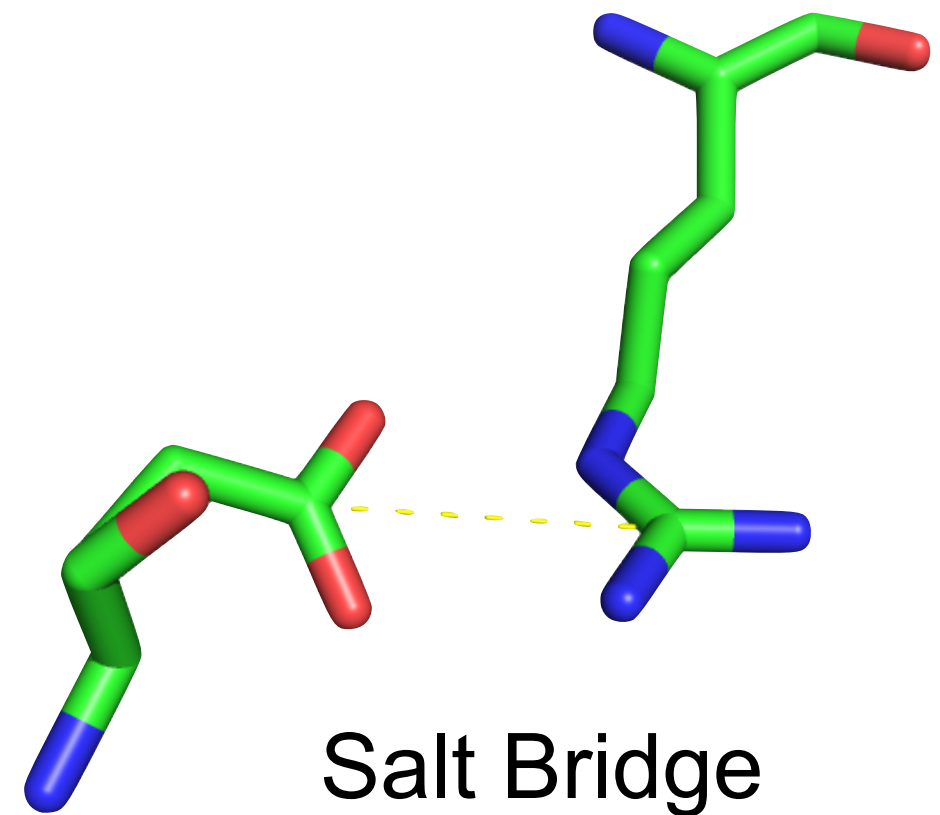
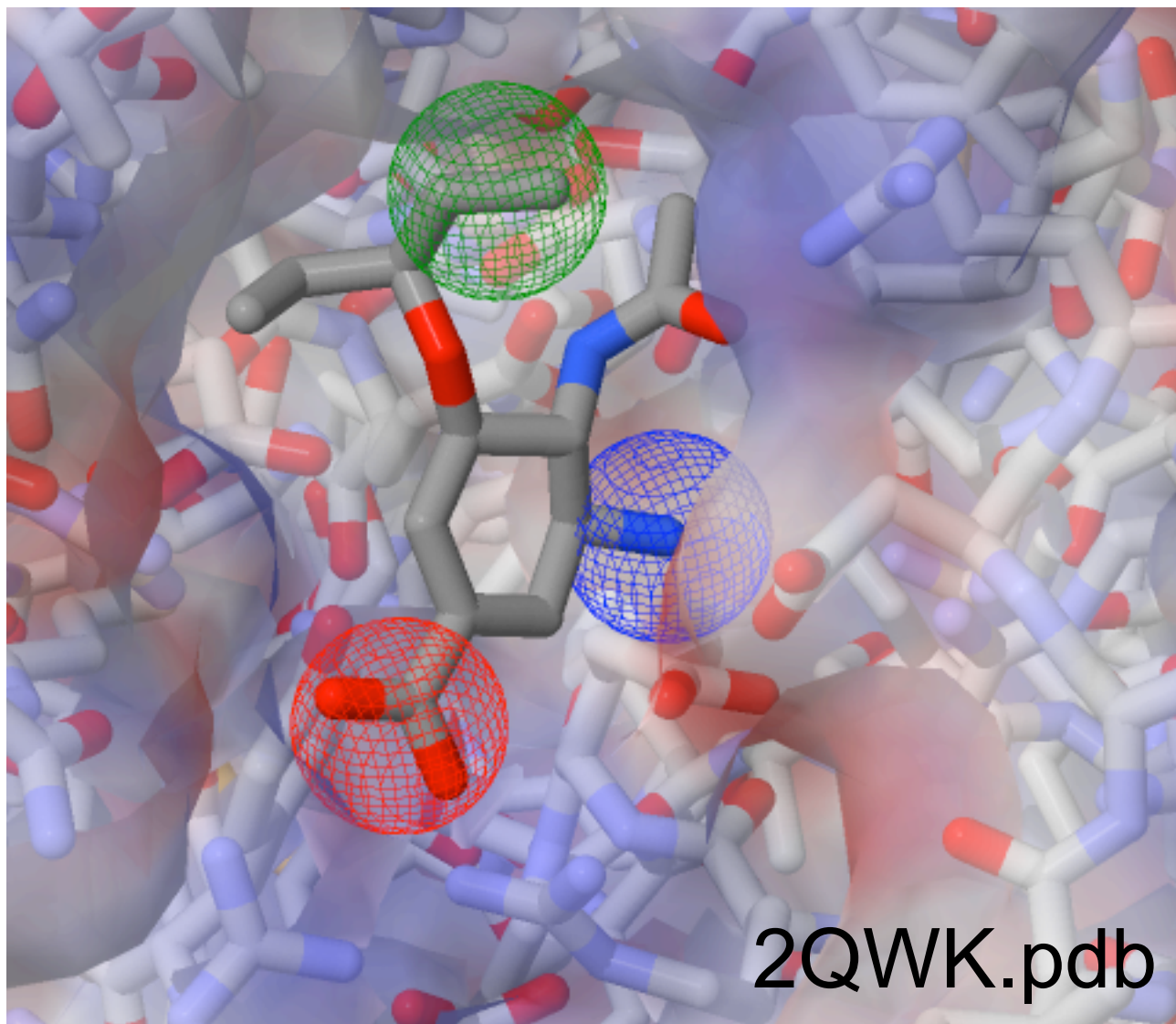


$$|\vec{F}_{Q-q}| = |\vec{F}_{q-Q}| = k \frac{|q \times Q|}{r^2}$$

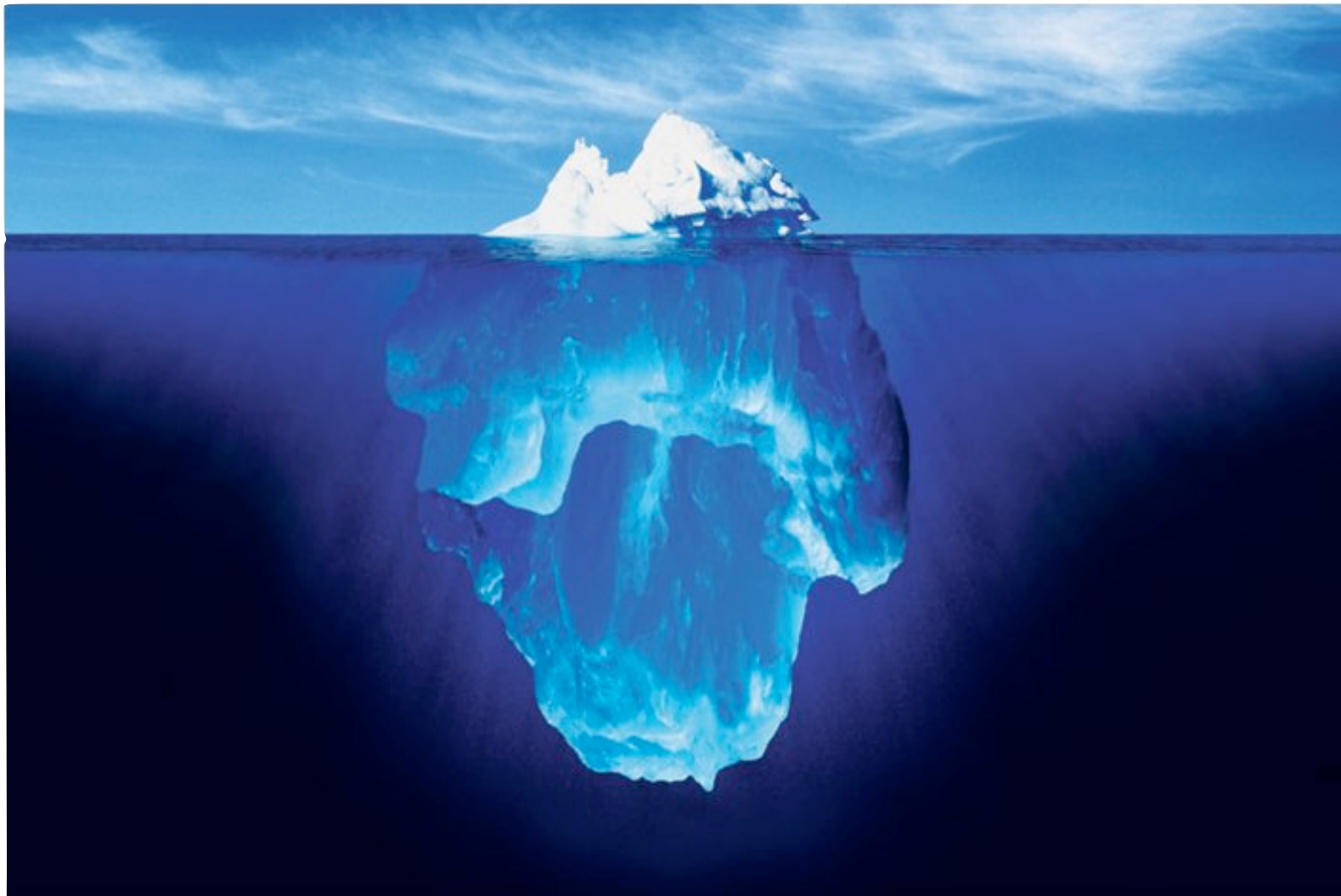




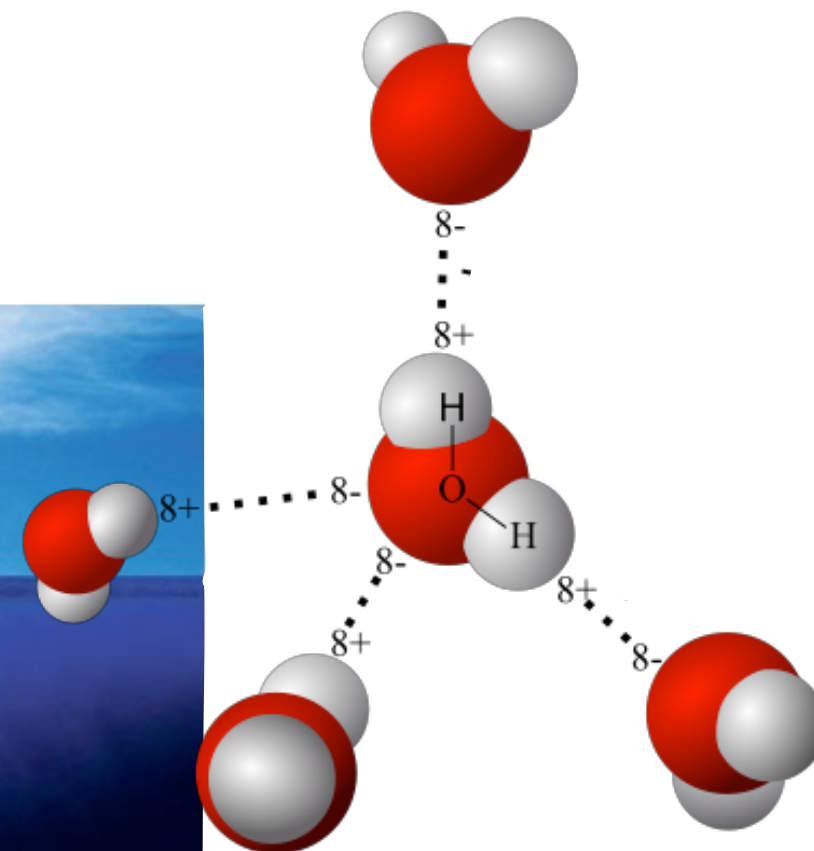
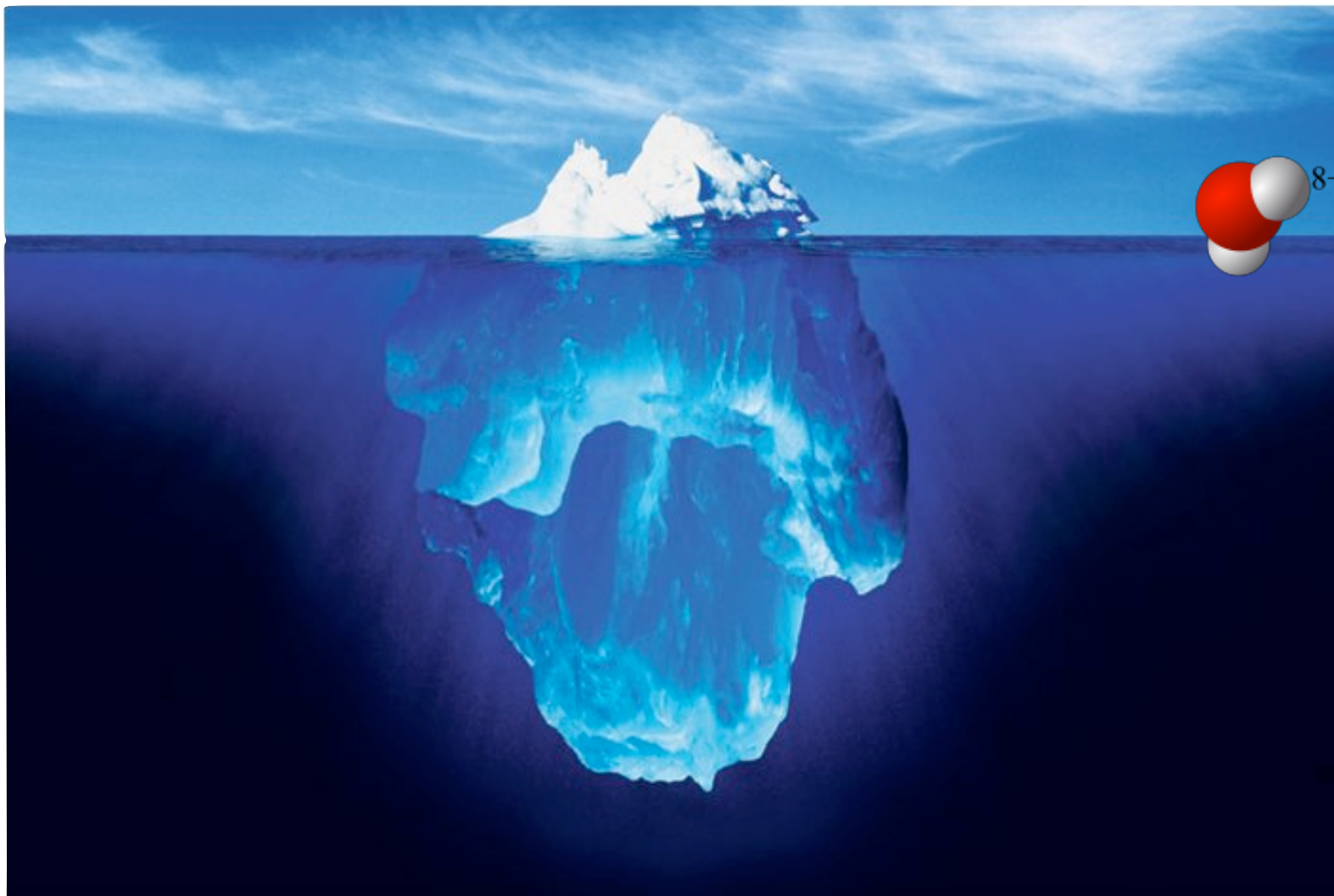
# Charge-Charge



# Hydrogen Bond

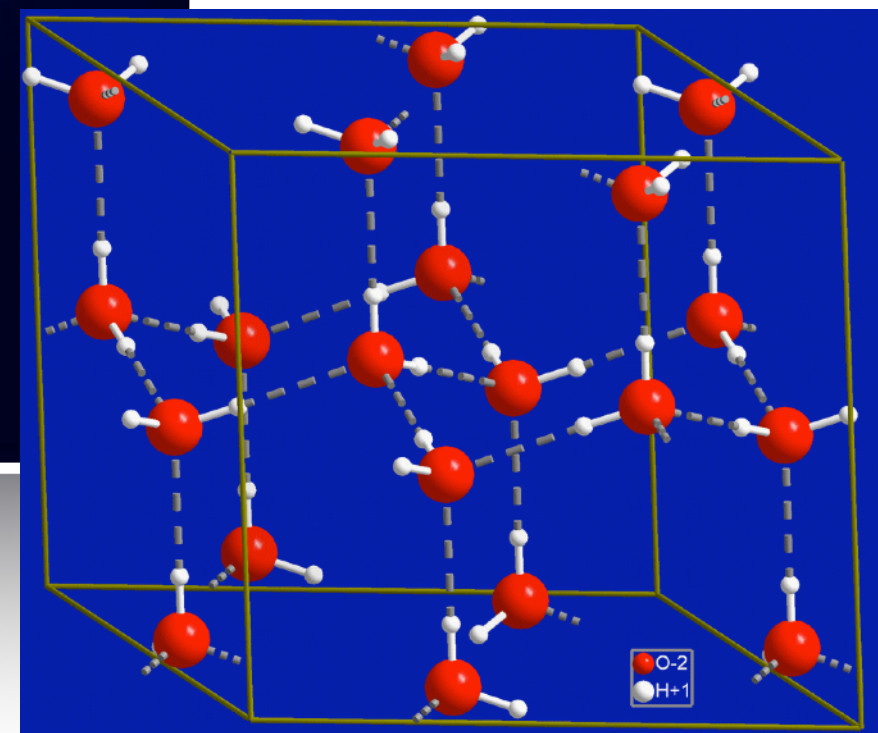
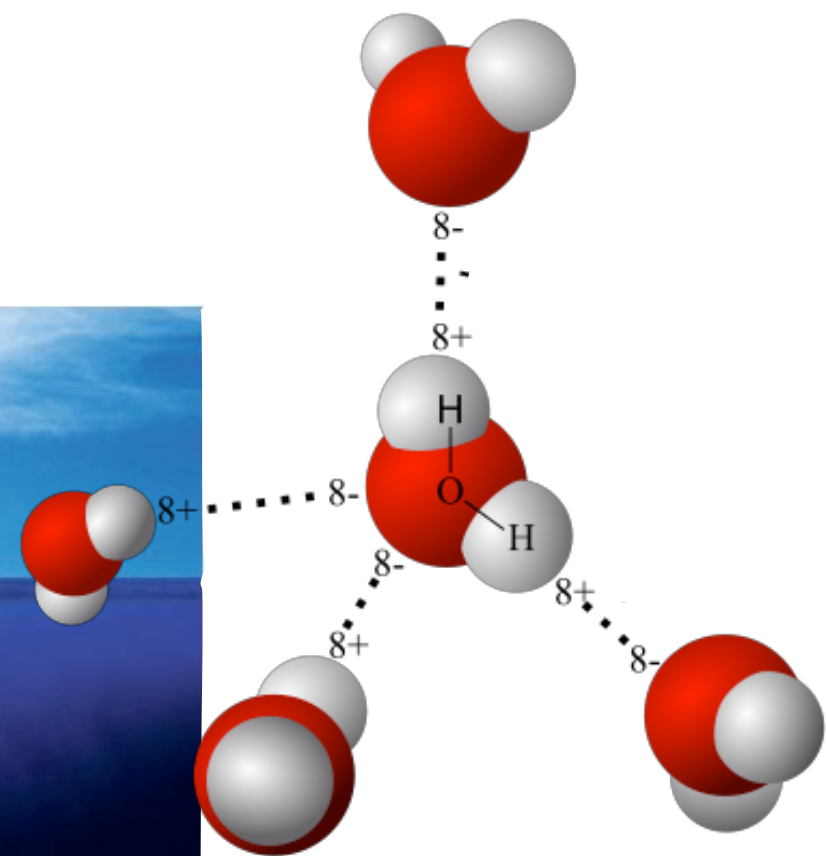
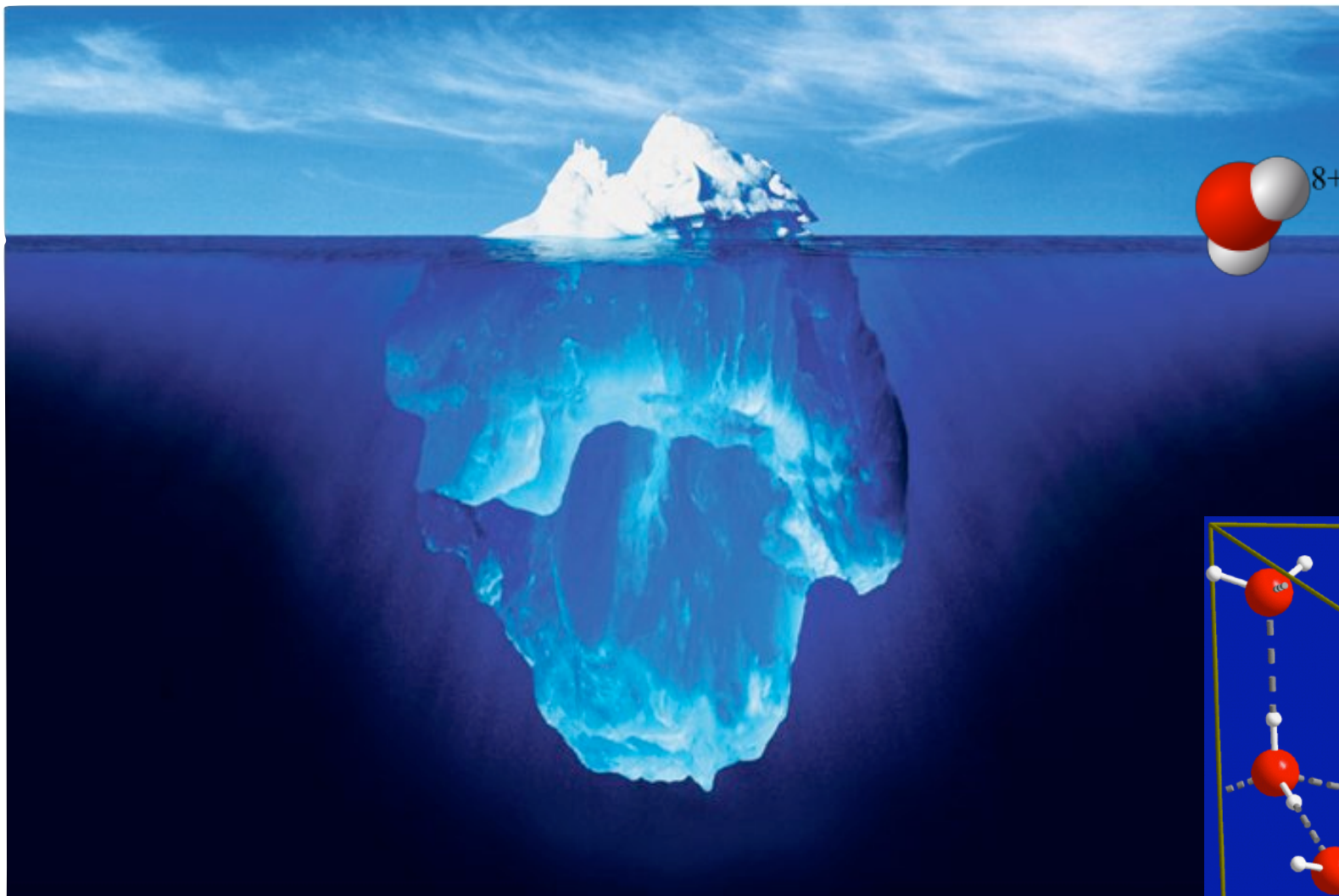


# Hydrogen Bond

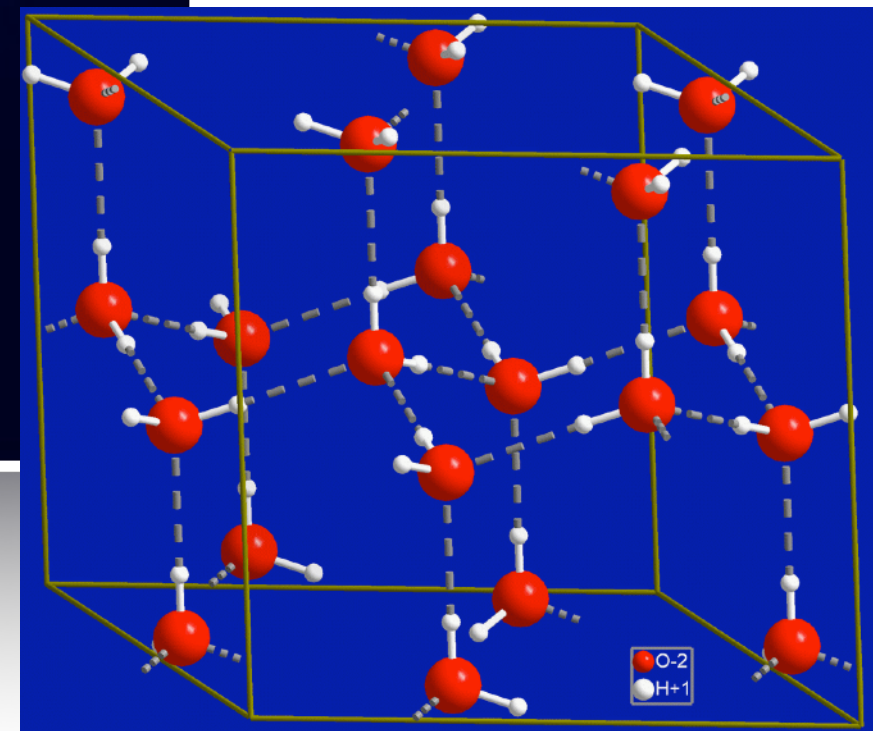
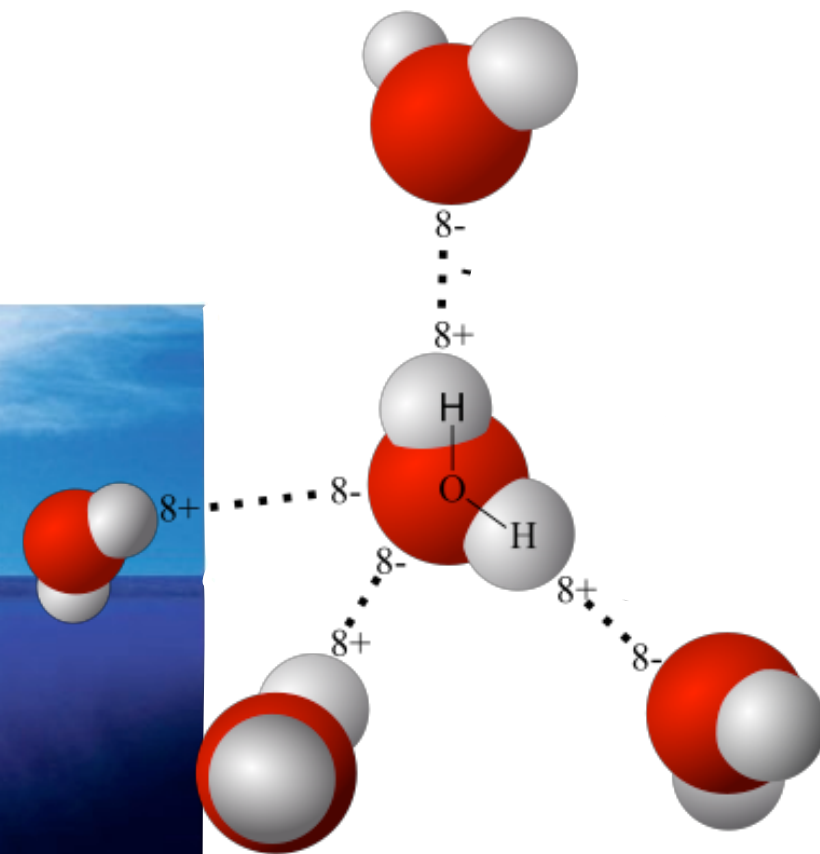
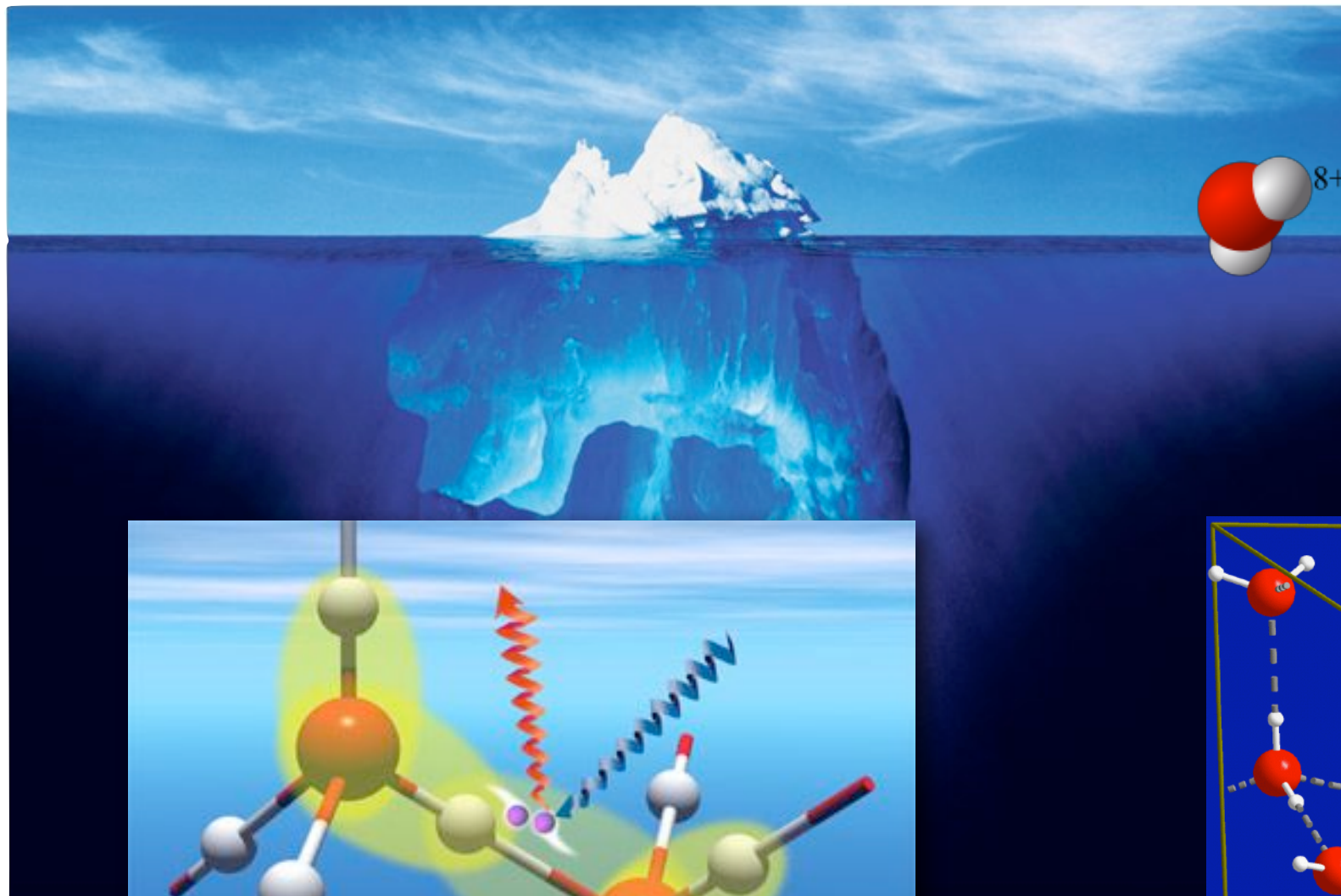




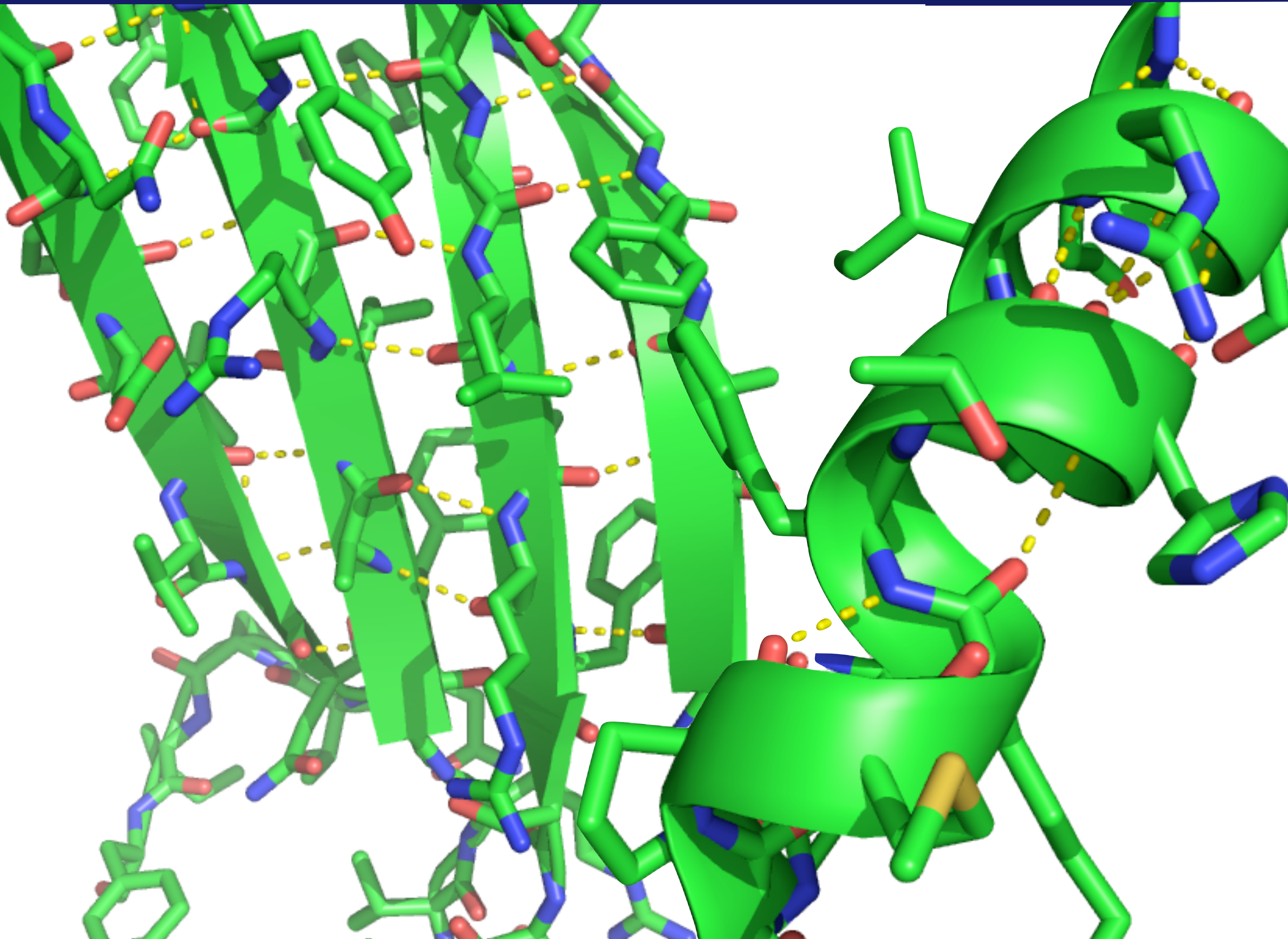
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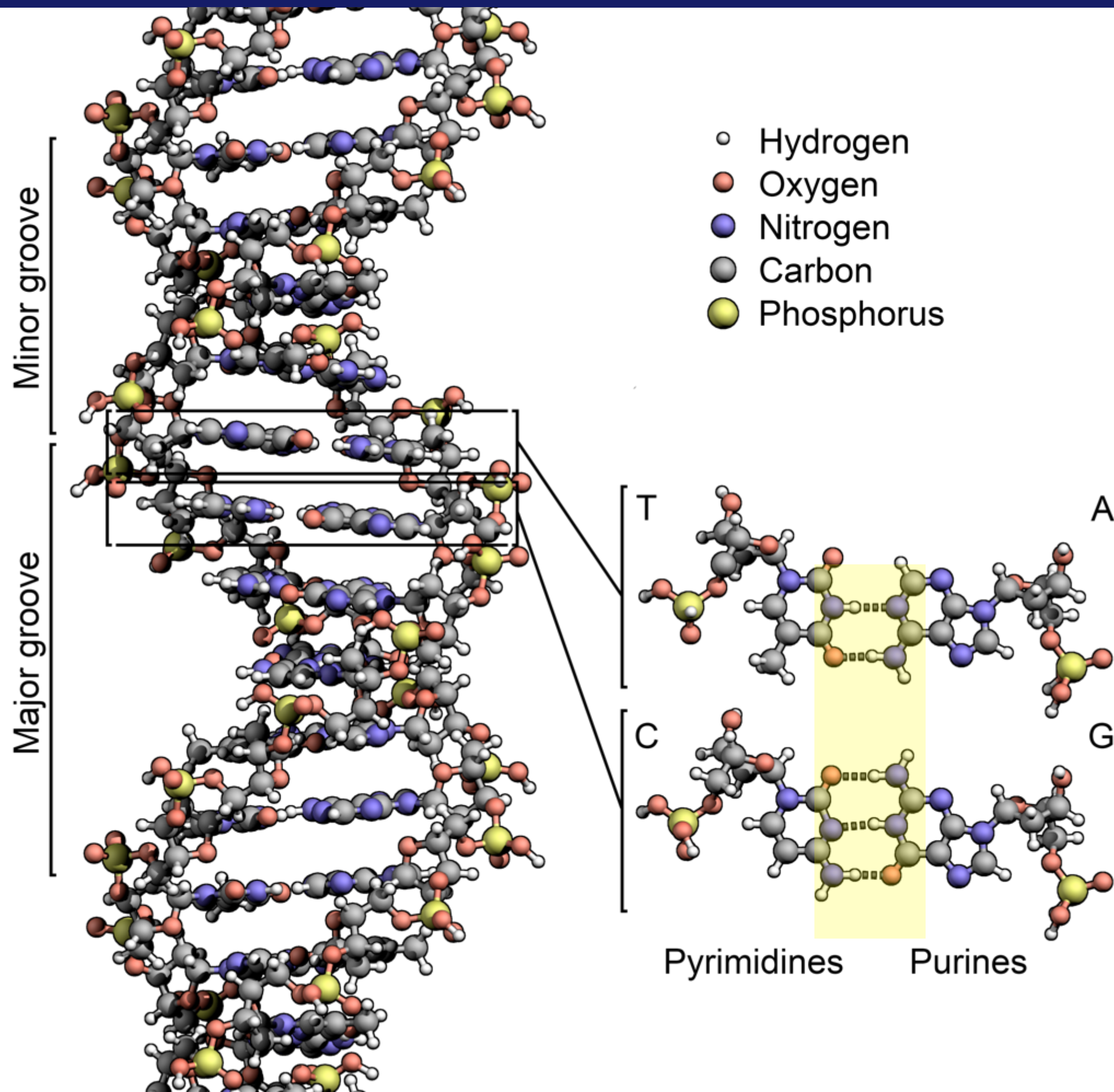
# Hydrogen Bond



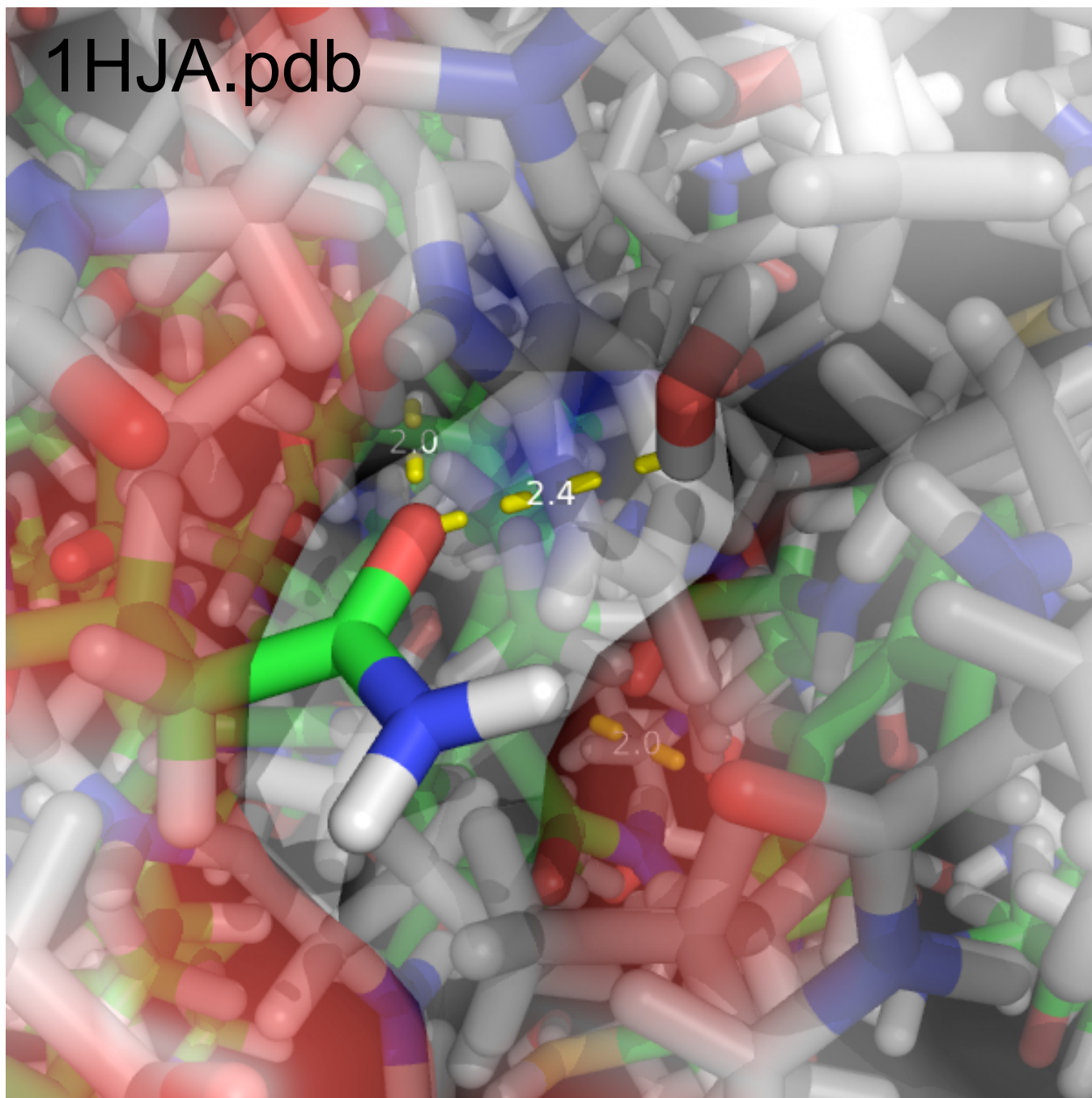








# Hydrogen Bond



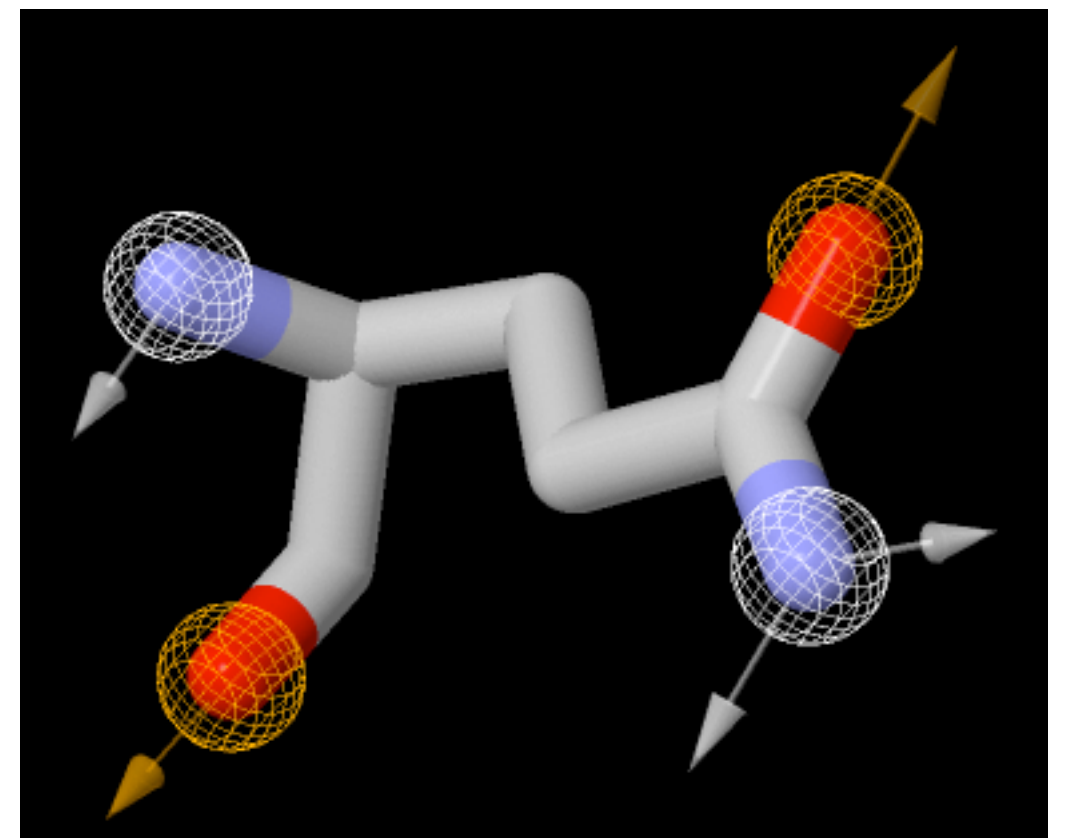
## Distance:

D-A:  $2.5\text{\AA} - 3.5\text{\AA}$  ( $4.0\text{\AA}?$ )

H-A:  $1.5\text{\AA} - 2.5\text{\AA}$

## Angle:

Depends on context

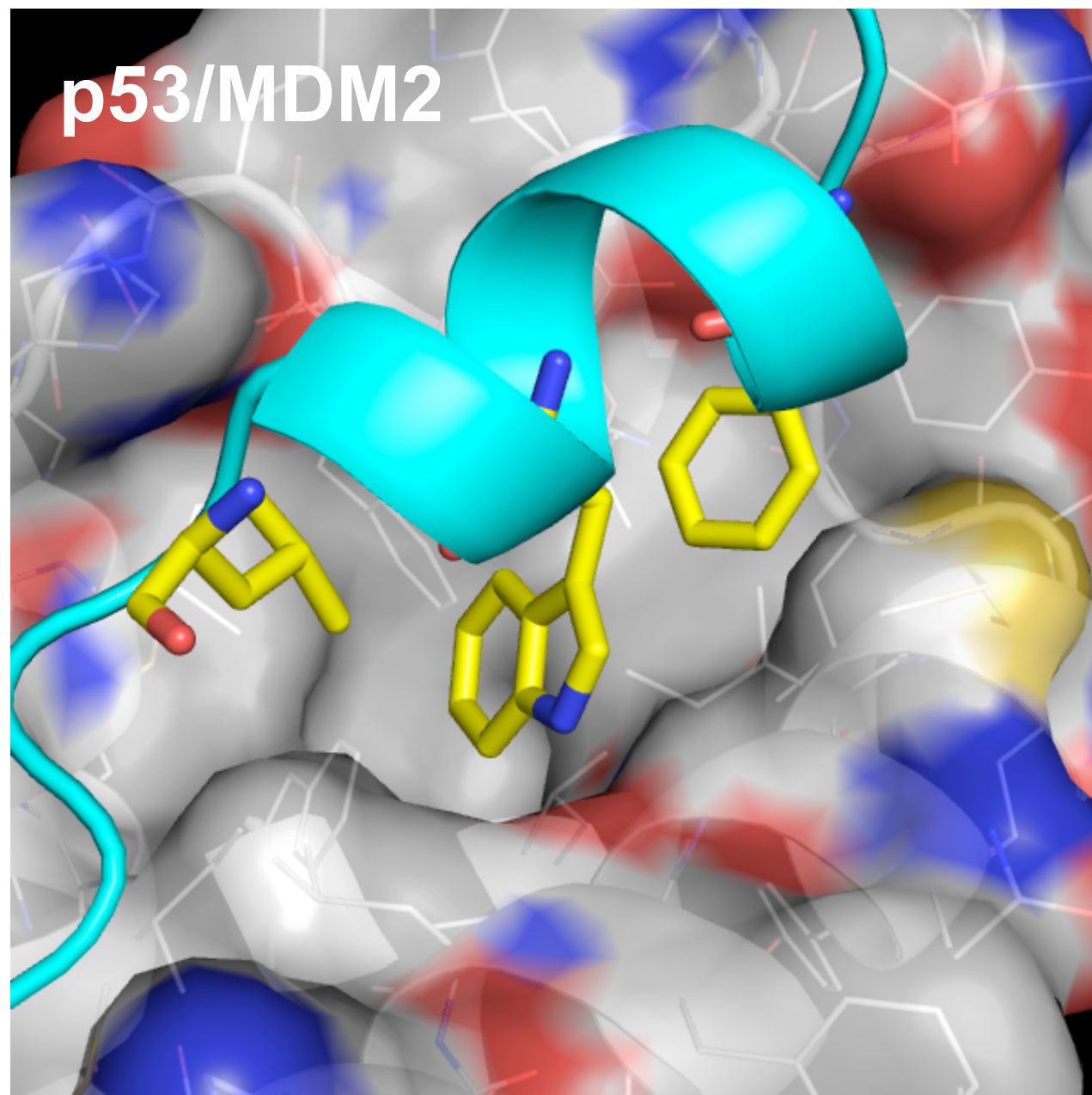




# Hydrophobic

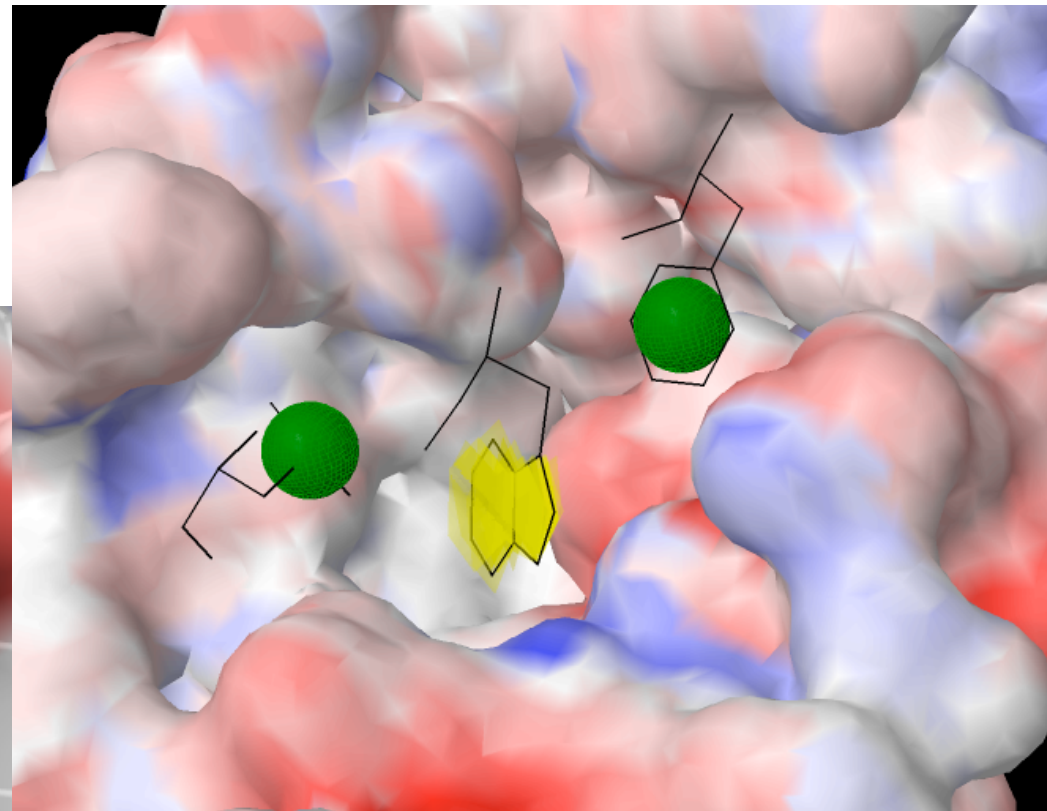
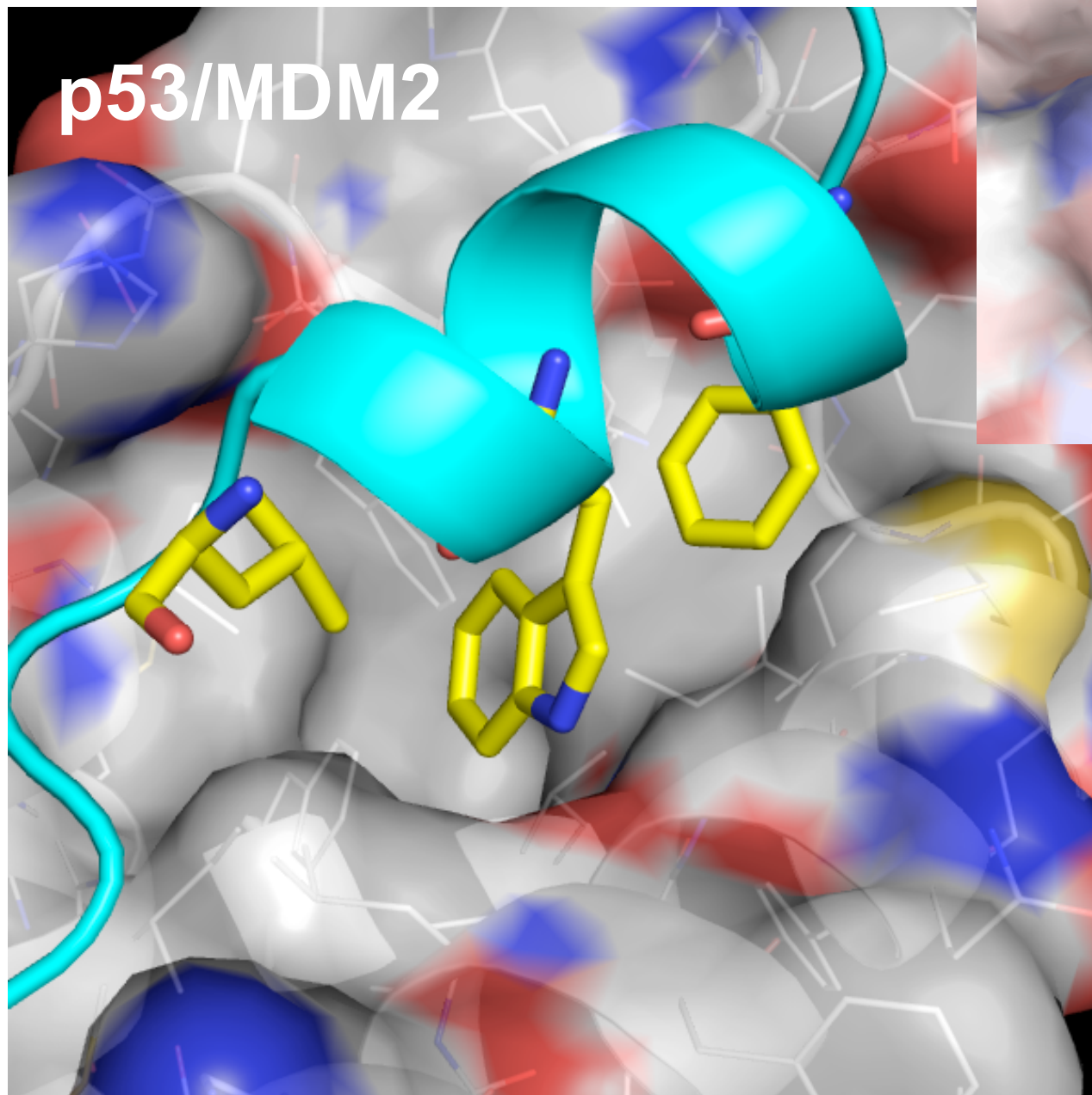


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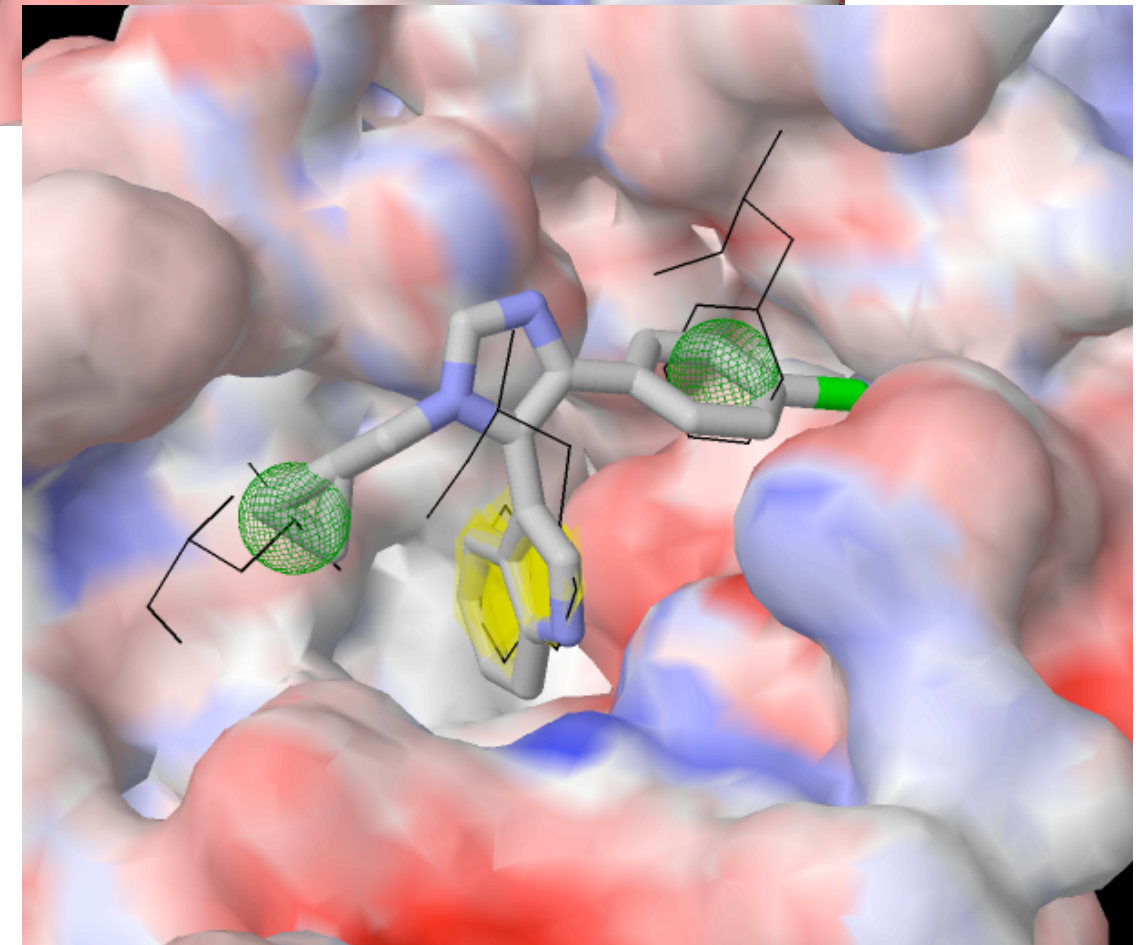
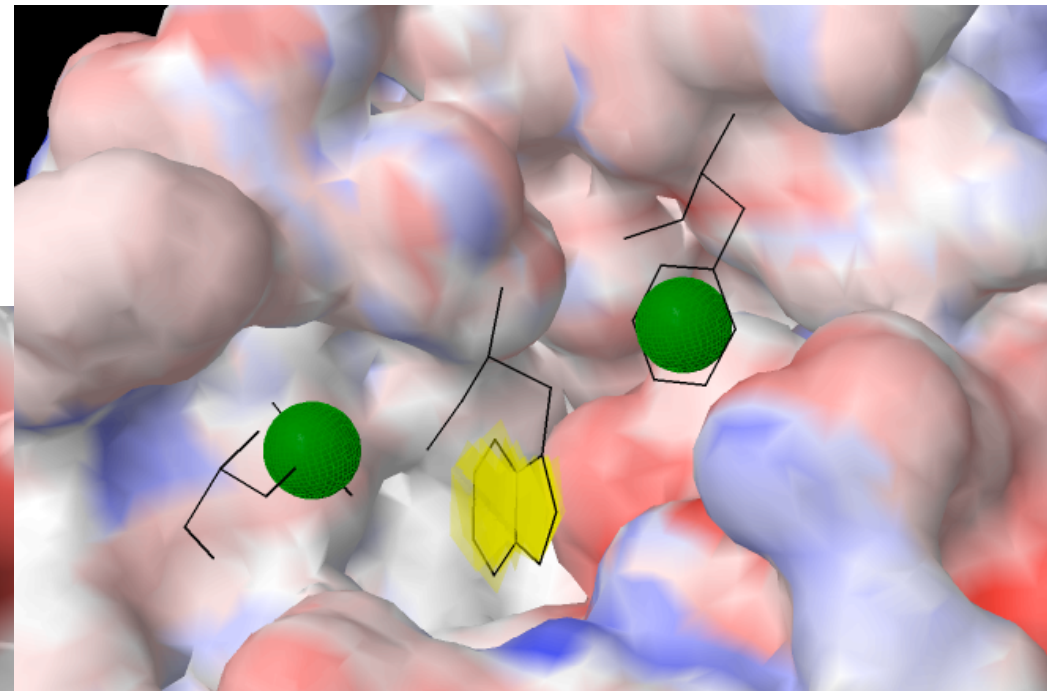
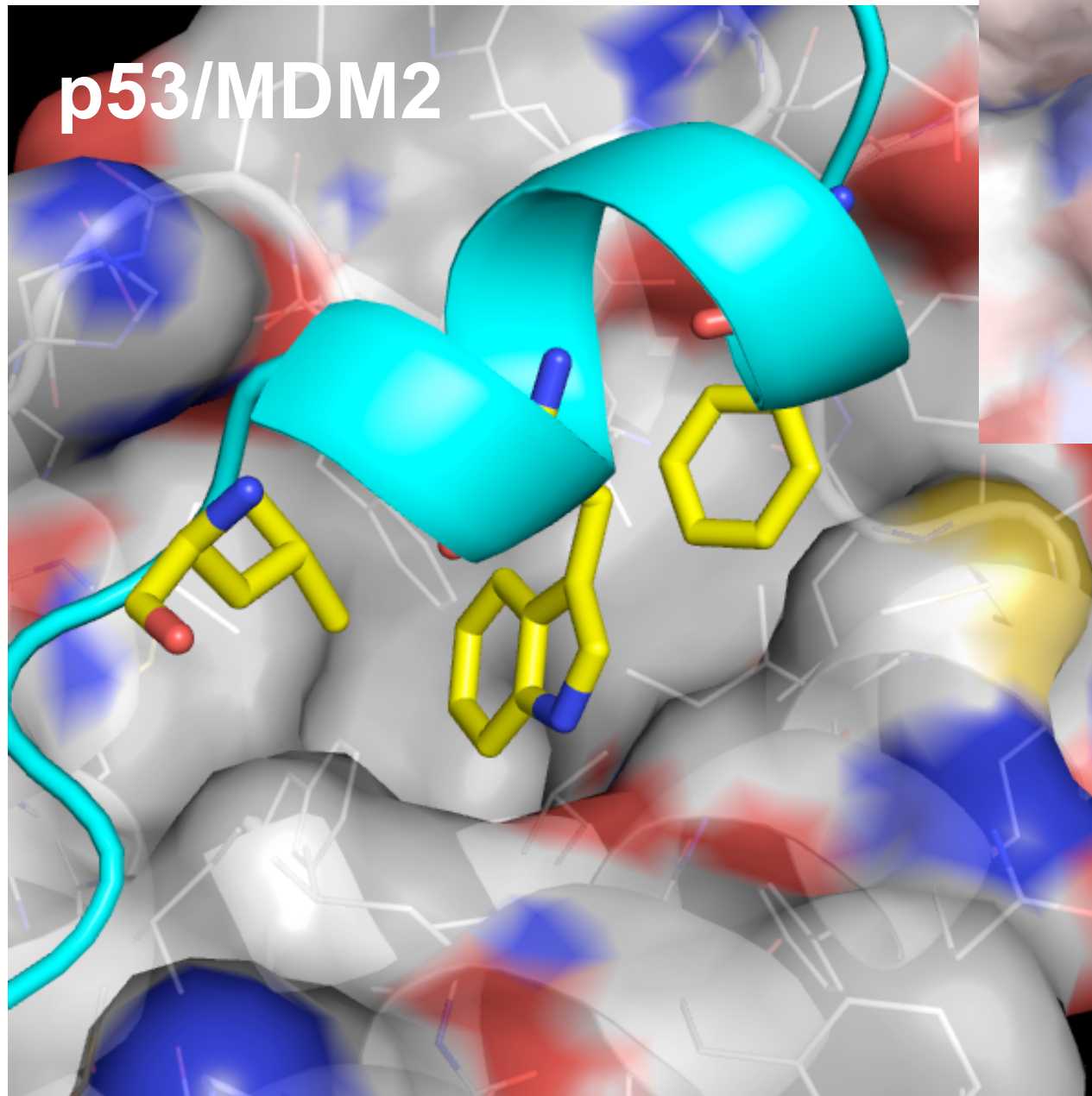




# Hydrophobic

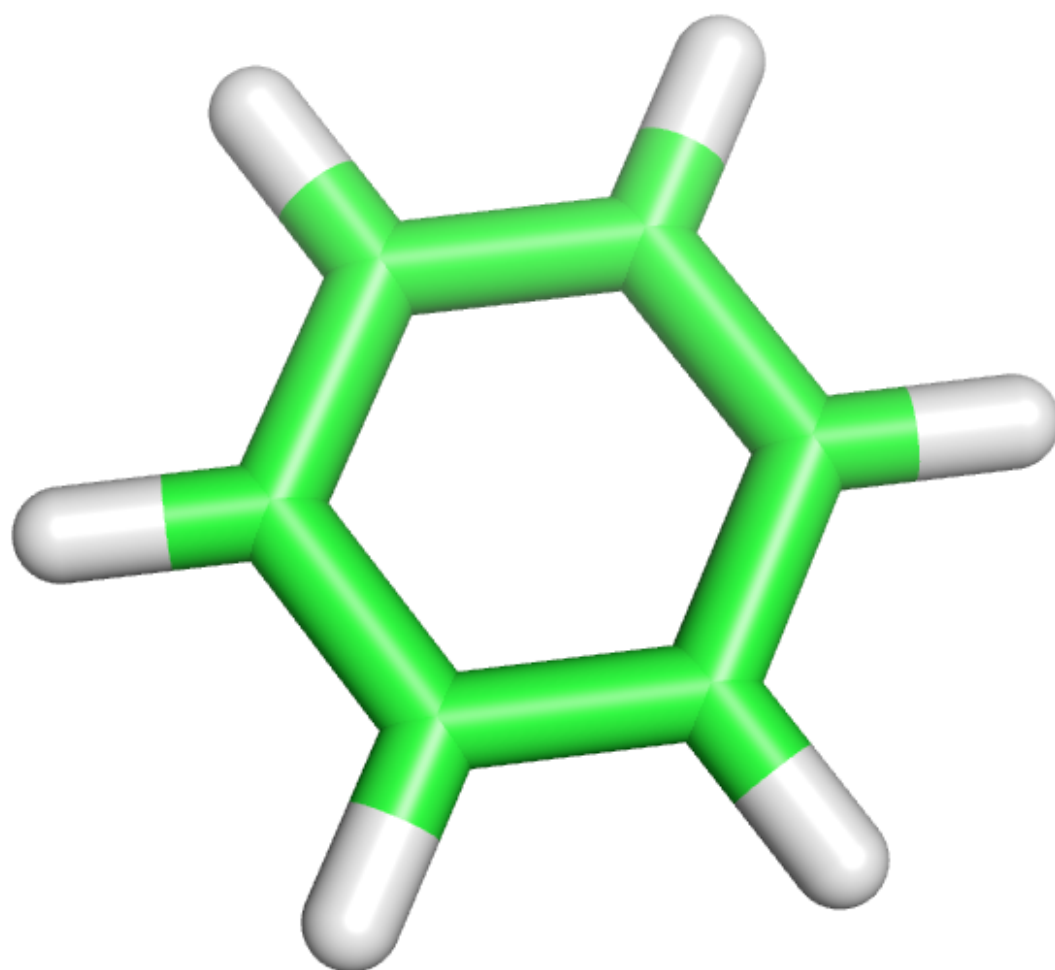


# Hydrophobic



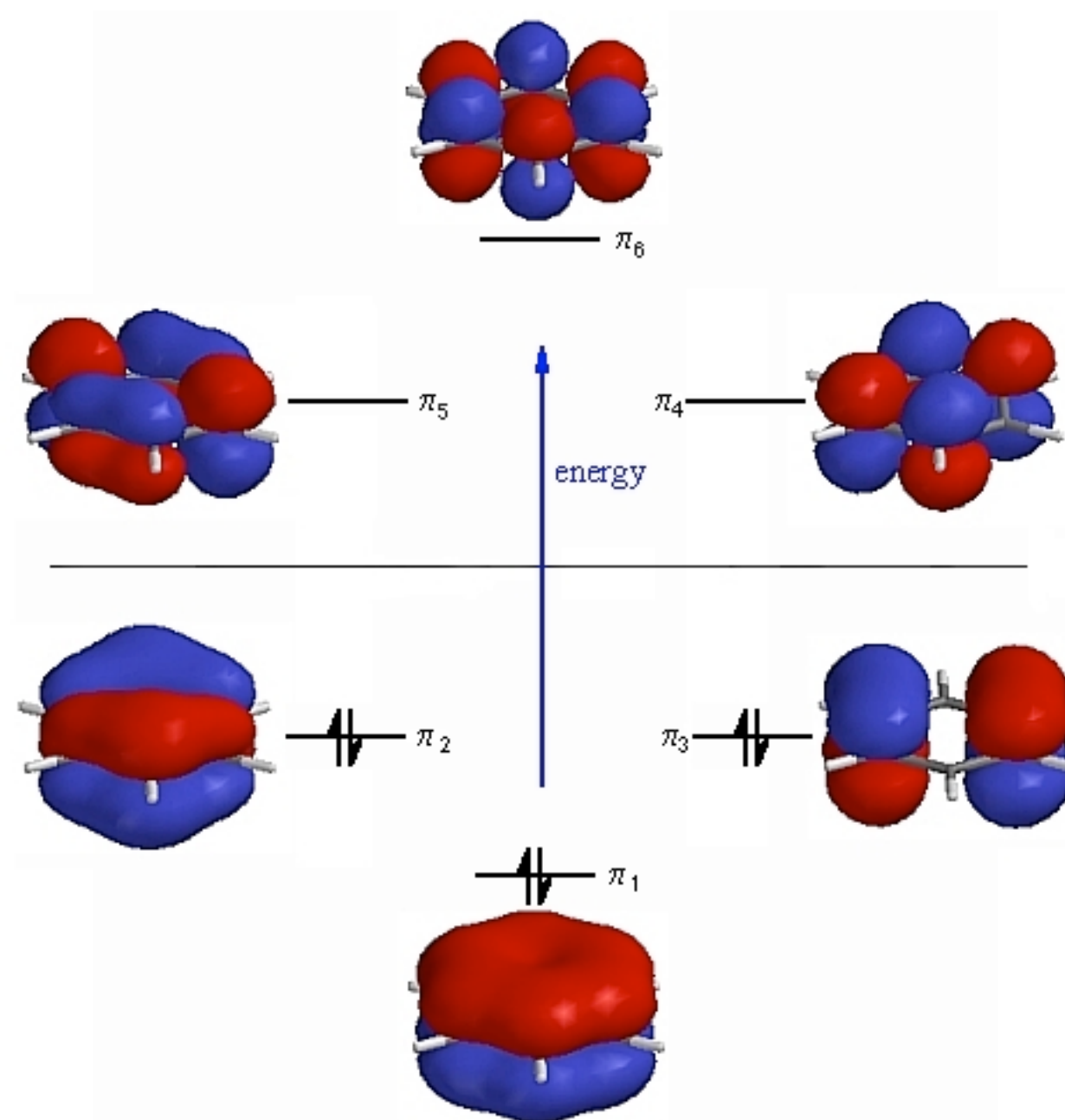
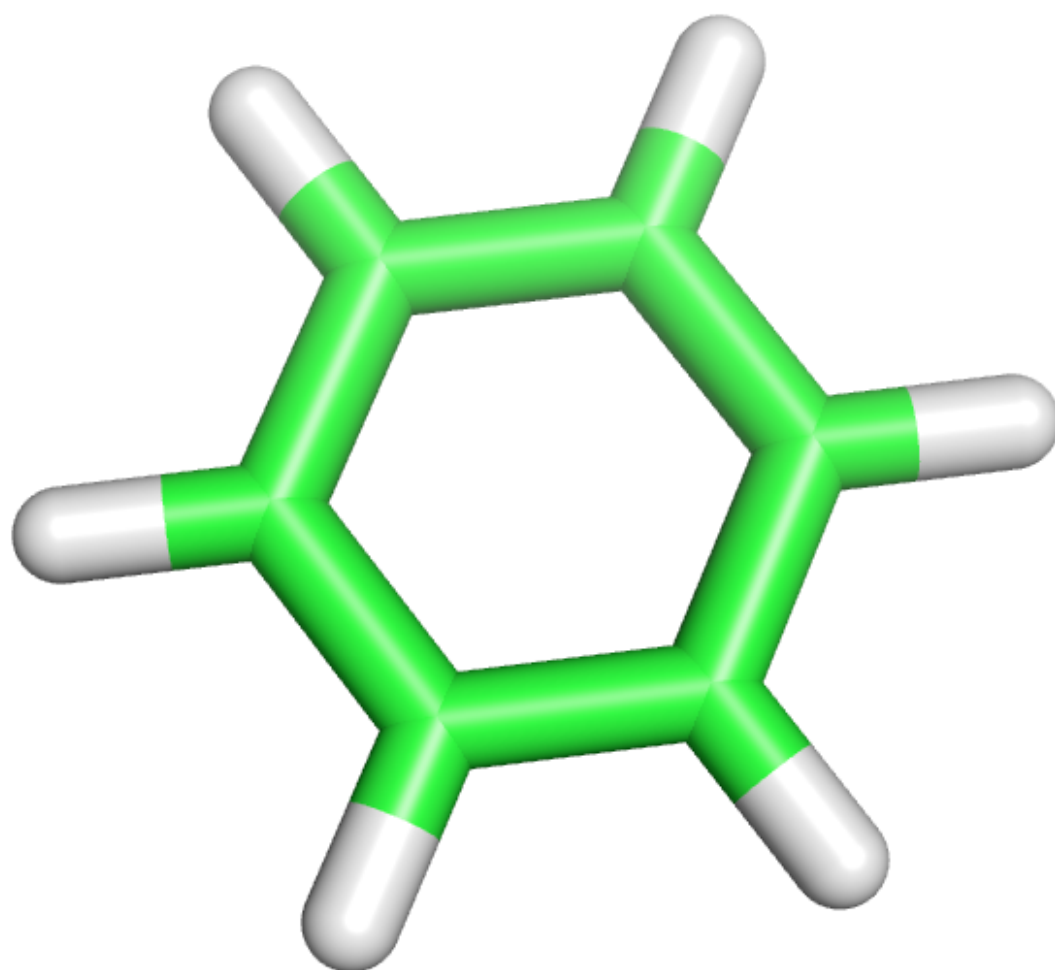


# Aromatic



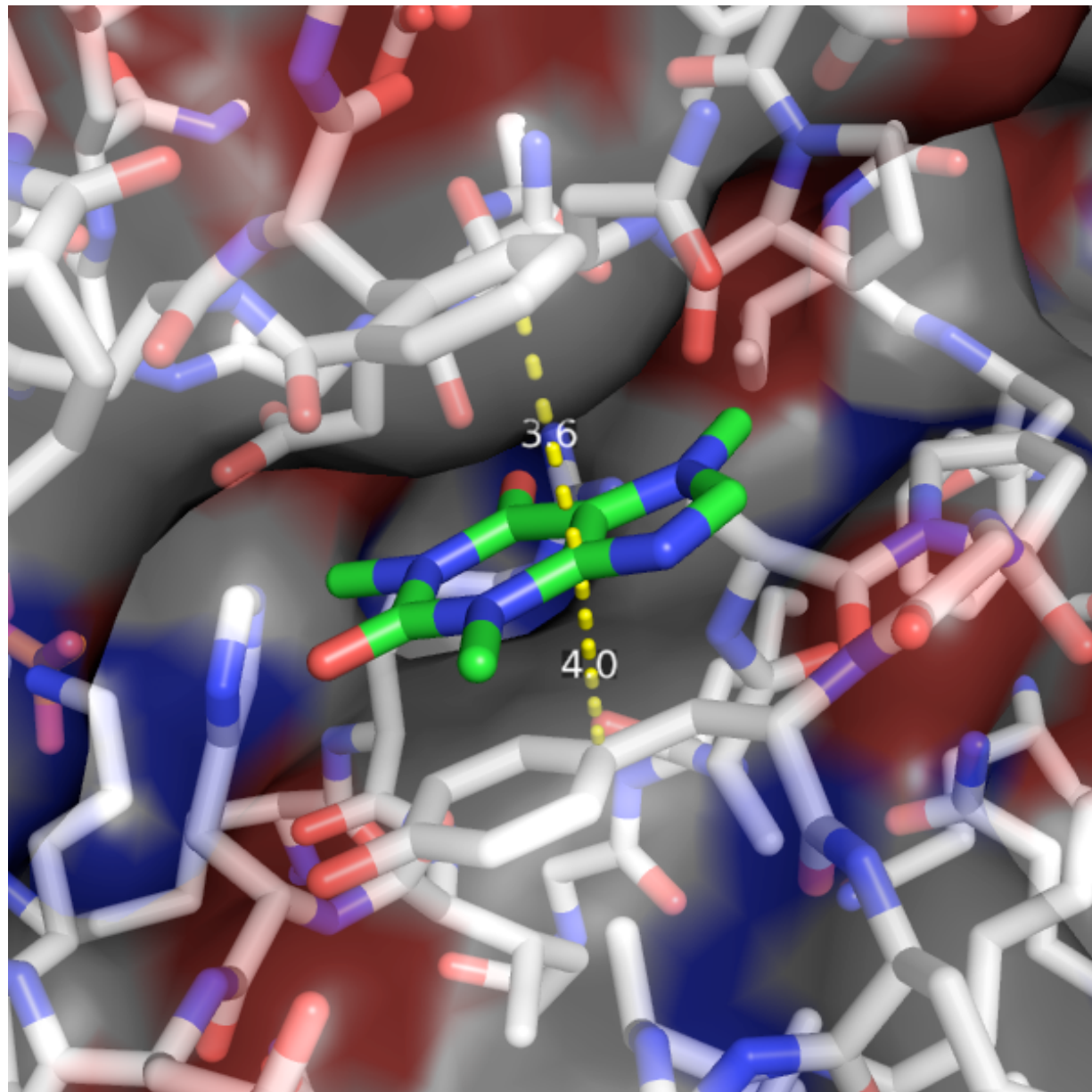
|                                            |                                       |                                           |                                    |                                         |                                    |
|--------------------------------------------|---------------------------------------|-------------------------------------------|------------------------------------|-----------------------------------------|------------------------------------|
| 2<br><b>He</b><br>Helium<br>4.002602       |                                       |                                           |                                    |                                         |                                    |
| 5<br><b>B</b><br>Boron<br>10.811           | 6<br><b>C</b><br>Carbon<br>12.0107    | 7<br><b>N</b><br>Nitrogen<br>14.0067      | 8<br><b>O</b><br>Oxygen<br>15.9994 | 9<br><b>F</b><br>Fluorine<br>18.9984032 | 10<br><b>Ne</b><br>Neon<br>20.1797 |
| 13<br><b>Al</b><br>Aluminium<br>26.9815386 | 14<br><b>Si</b><br>Silicon<br>28.0855 | 15<br><b>P</b><br>Phosphorus<br>30.973762 | 16<br><b>S</b><br>Sulfur<br>32.065 | 17<br><b>Cl</b><br>Chlorine<br>35.453   | 18<br><b>Ar</b><br>Argon<br>39.948 |

# Aromatic

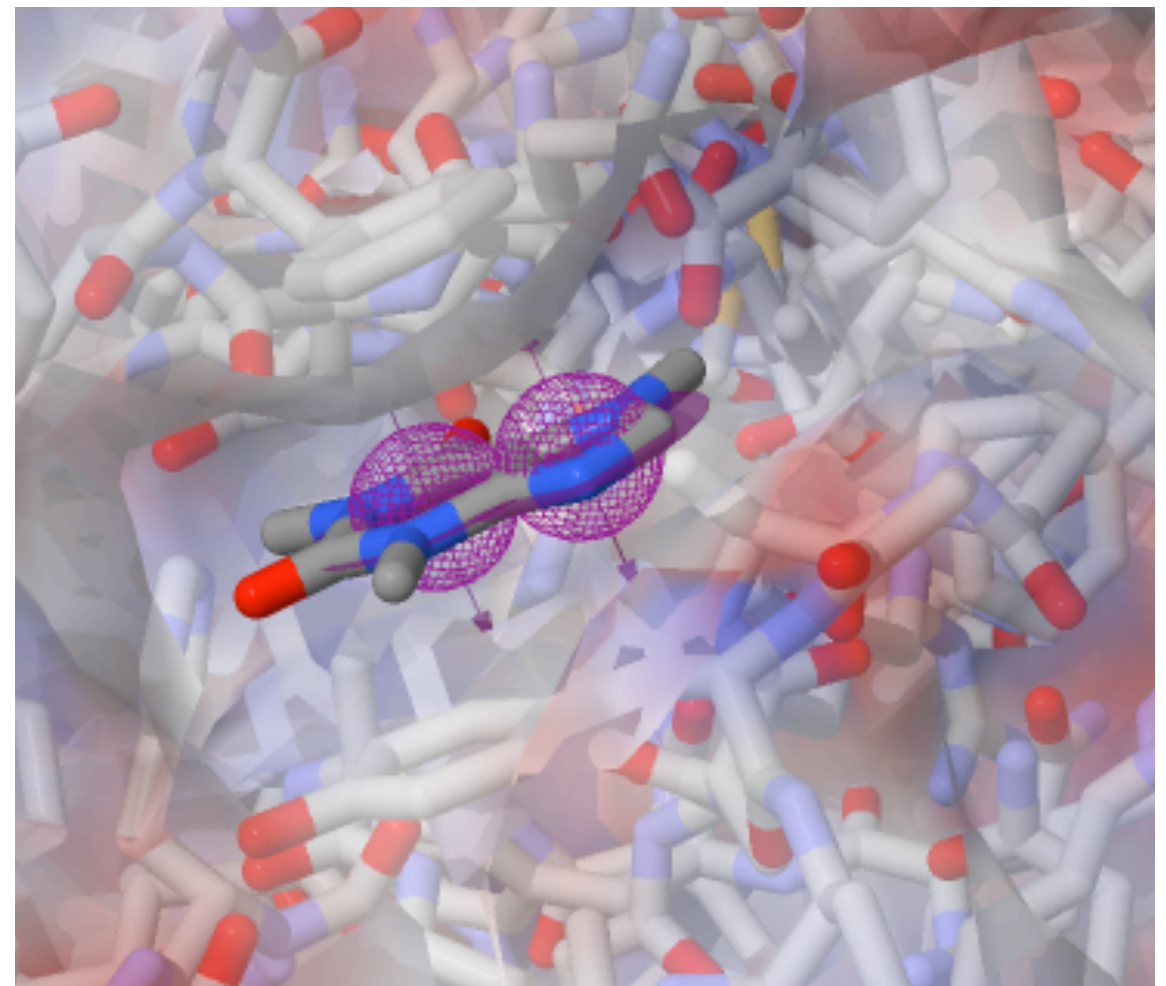


|                                            |                                       |                                           |                                    |                                         |                                    |
|--------------------------------------------|---------------------------------------|-------------------------------------------|------------------------------------|-----------------------------------------|------------------------------------|
| 5<br><b>B</b><br>Boron<br>10.811           | 6<br><b>C</b><br>Carbon<br>12.0107    | 7<br><b>N</b><br>Nitrogen<br>14.0067      | 8<br><b>O</b><br>Oxygen<br>15.9994 | 9<br><b>F</b><br>Fluorine<br>18.9984032 | 10<br><b>Ne</b><br>Neon<br>20.1797 |
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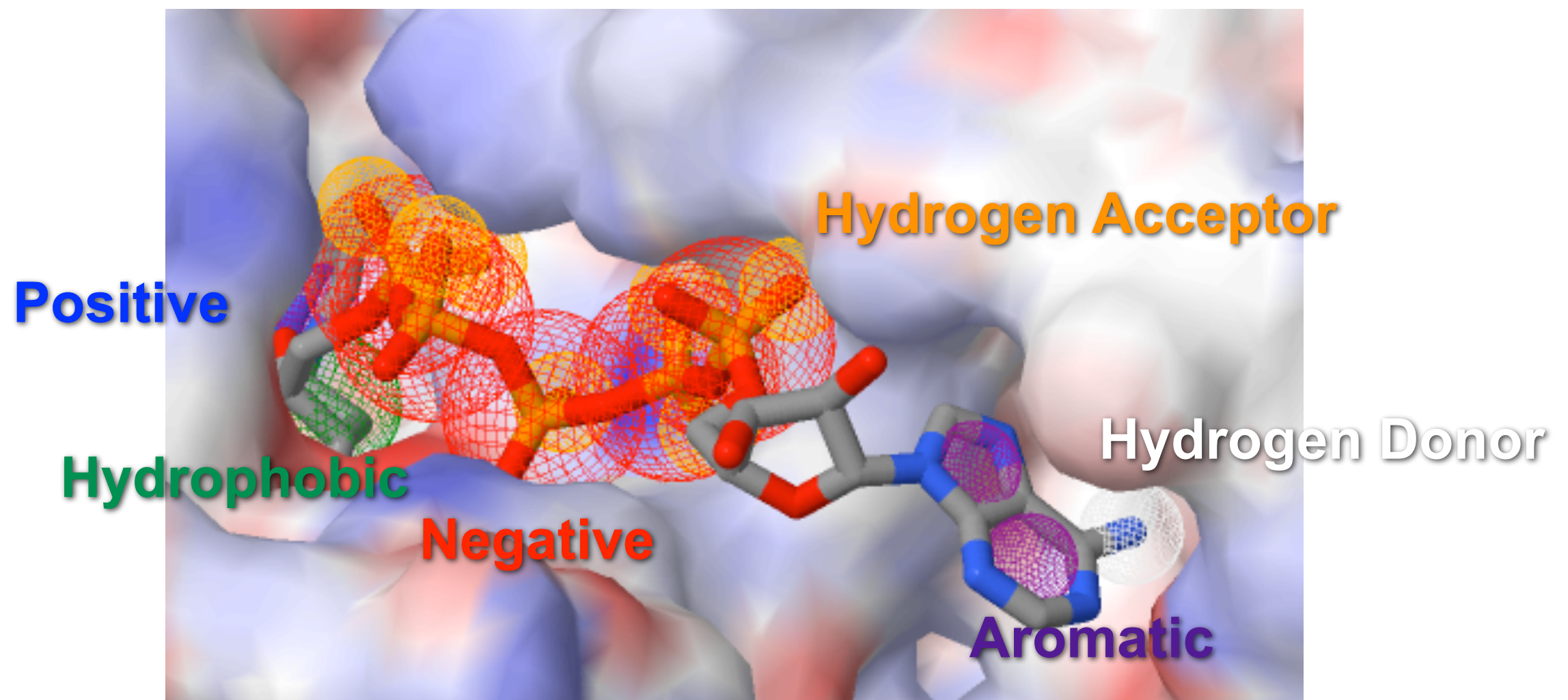


Rings offset  
Interplanar distance: 3.3-3.8Å





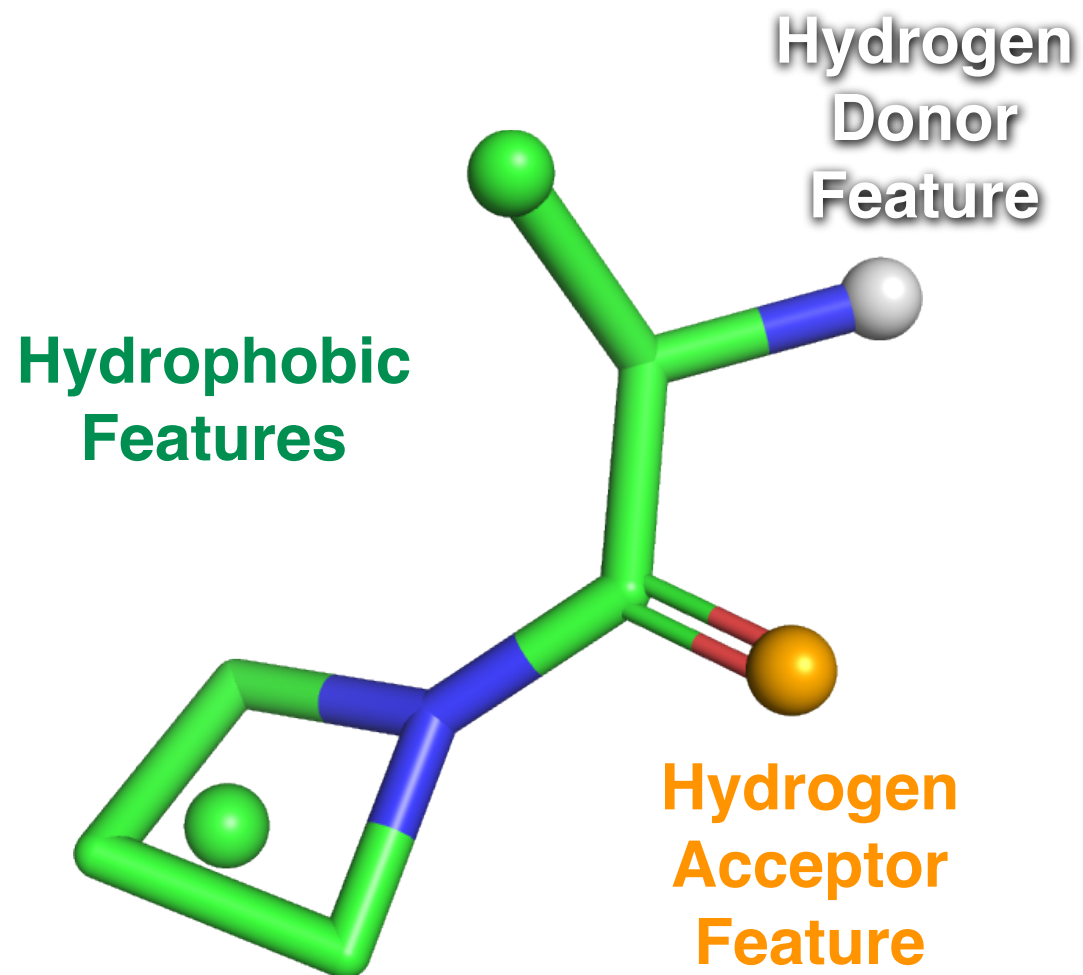
# Pharmacophore Features





Pharmer

# Efficient and Exact Pharmacophore Search



## Pharmacophore

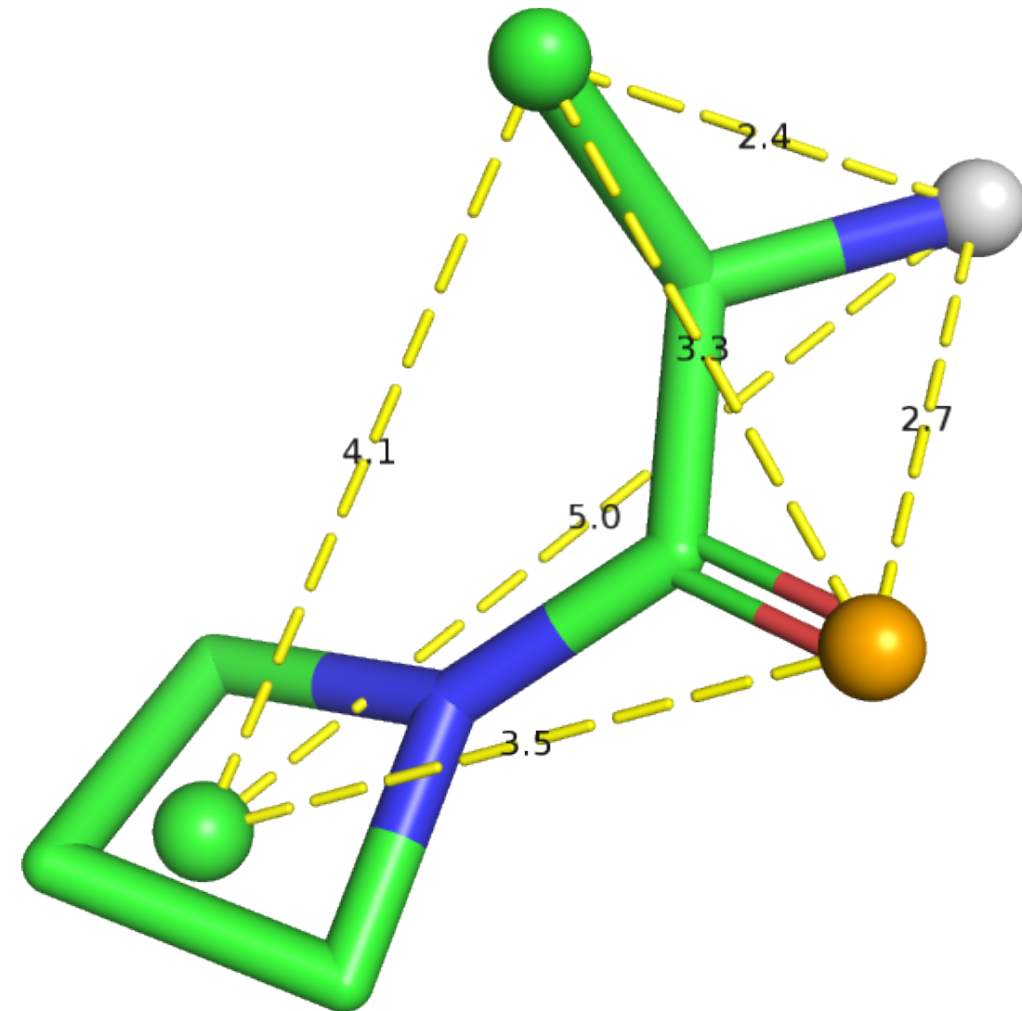
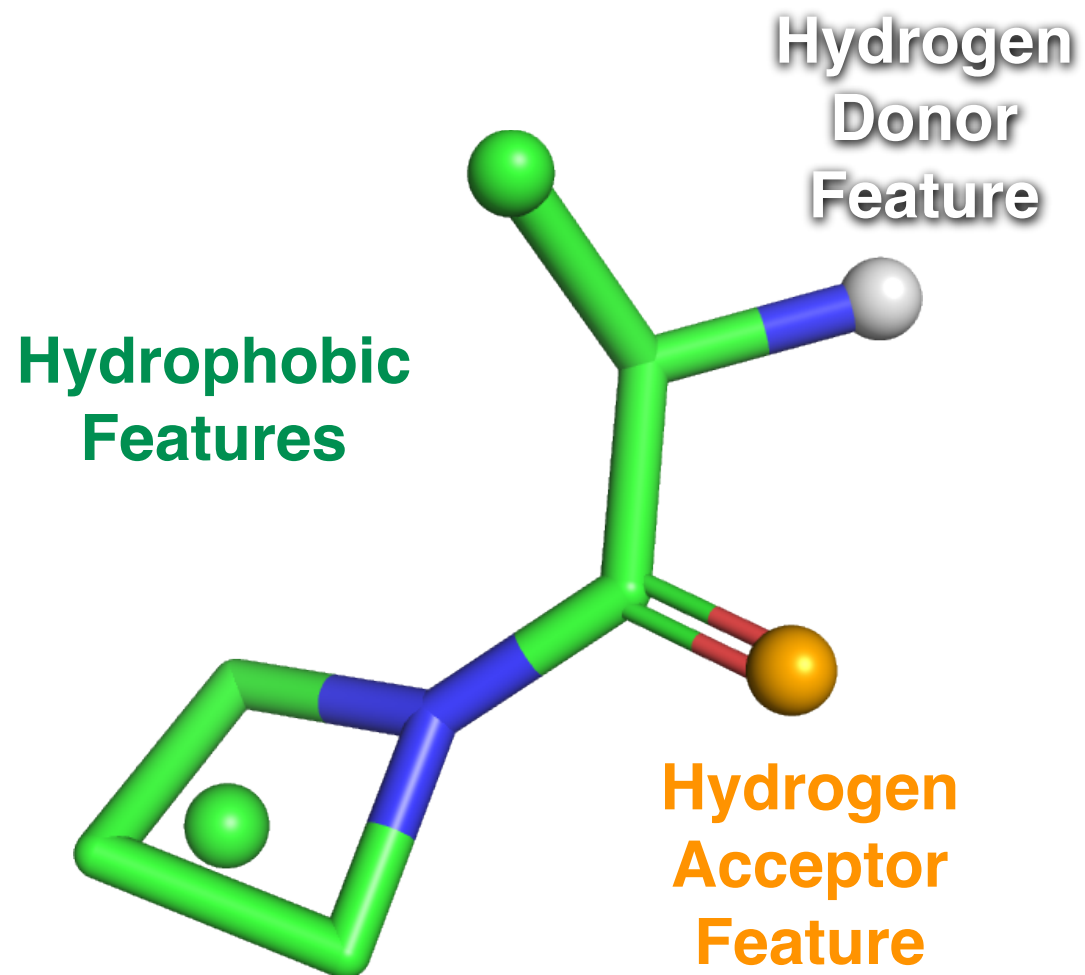
A spatial arrangement of molecular features essential for biological activity

Koes, D. R., & Camacho, C. J. (2011). Pharmer: efficient and exact pharmacophore search. *Journal of Chemical Information and Modeling*, 51(6), 1307-1314. doi:10.1021/ci200097m

Koes, D. R., & Camacho, C. J. (2012). ZINCPharmer: pharmacophore search of the ZINC database. *Nucleic acids research*, 40(Web Server issue), W409-414. doi:10.1093/nar/gks378

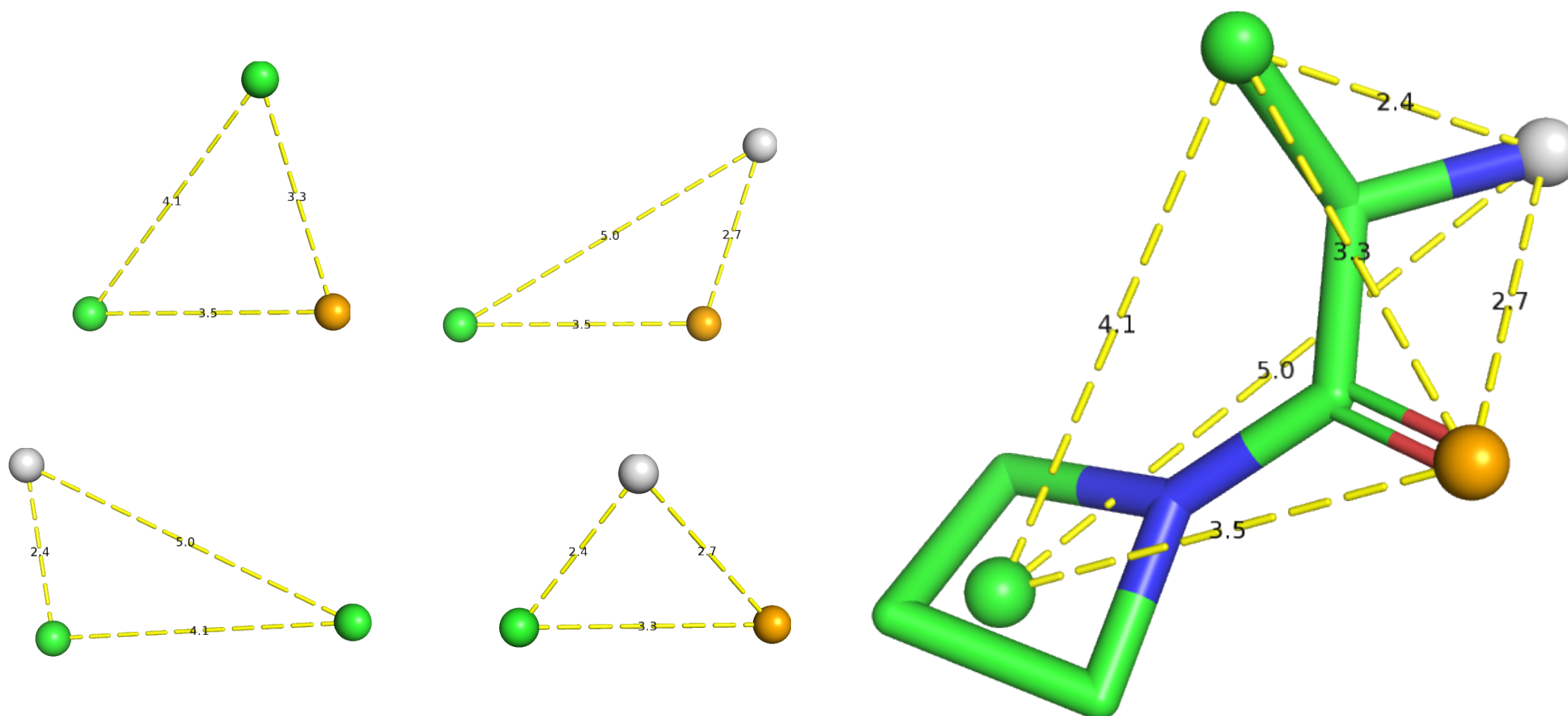
Pharmer

## Efficient and Exact Pharmacophore Search



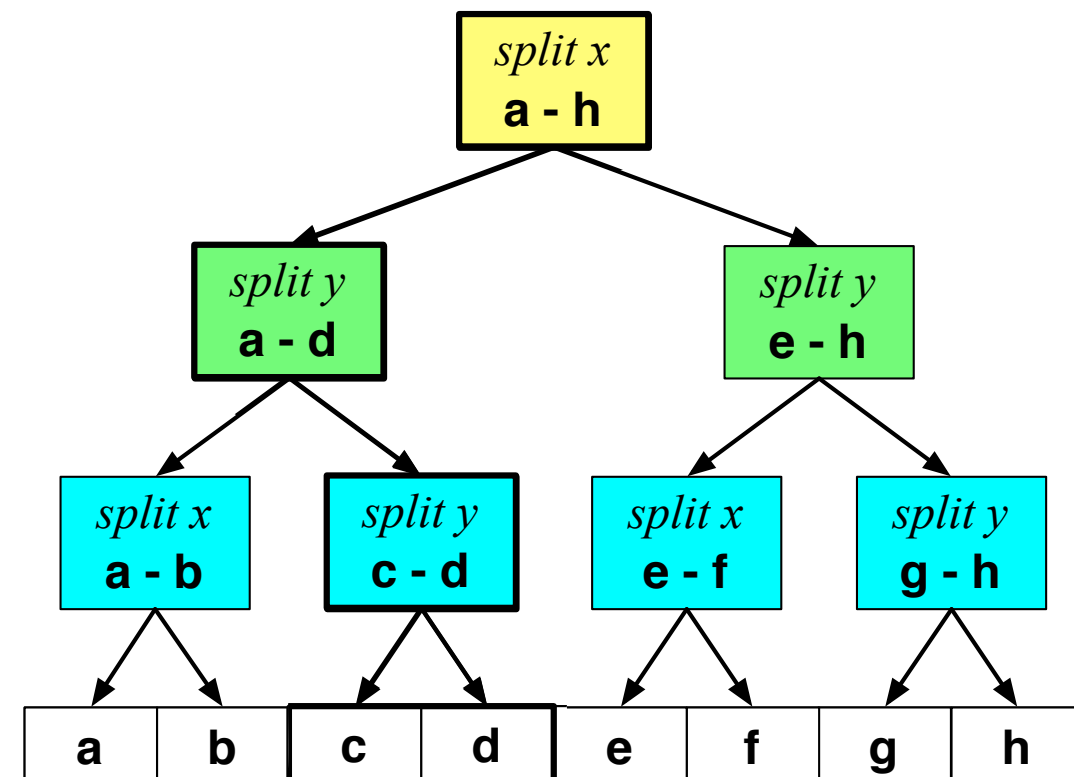
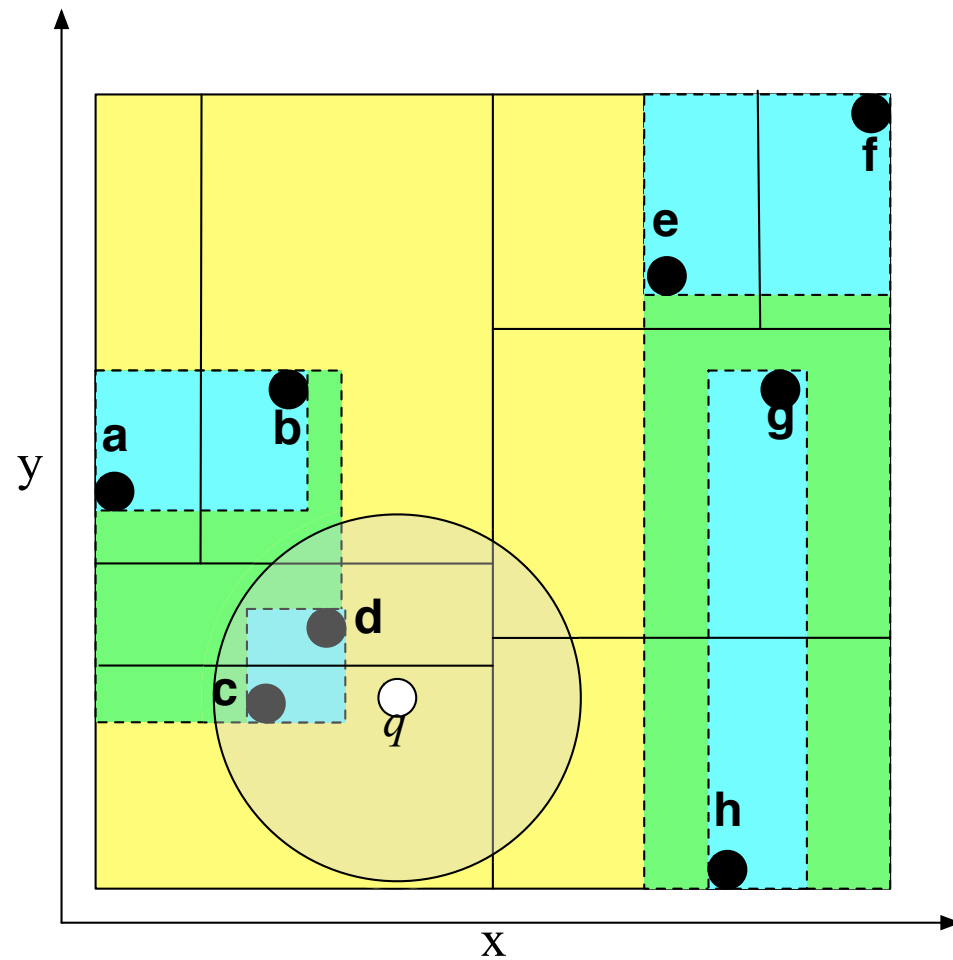
Pharmer

## Efficient and Exact Pharmacophore Search



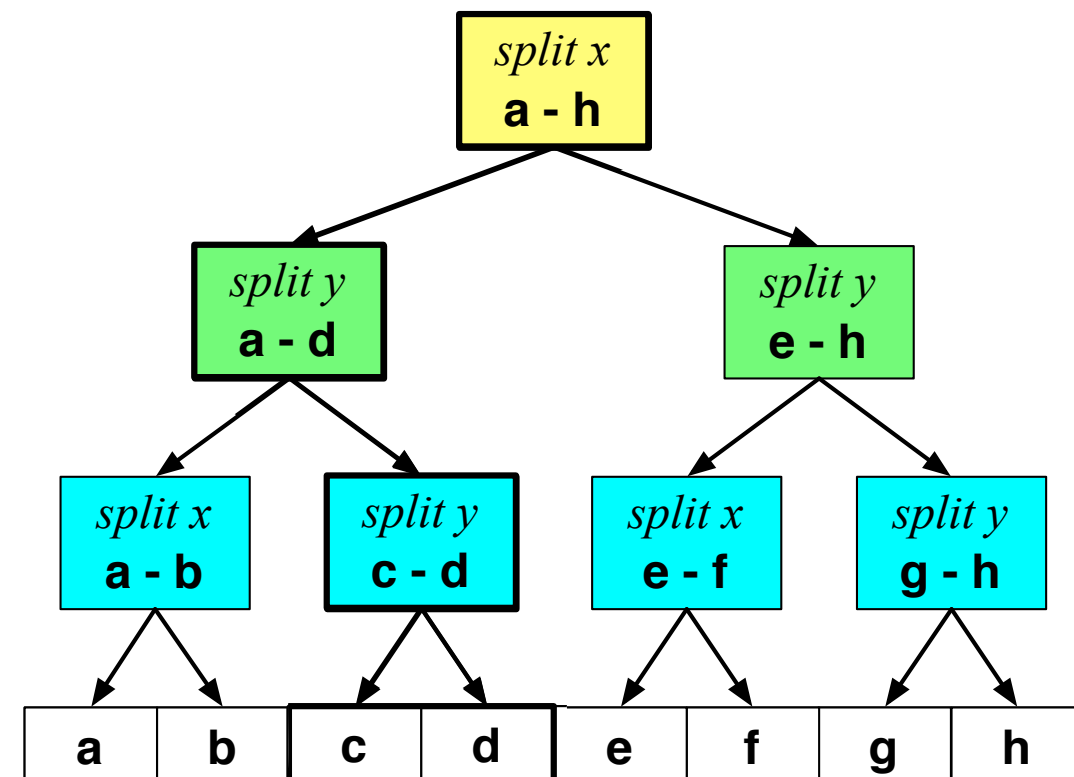
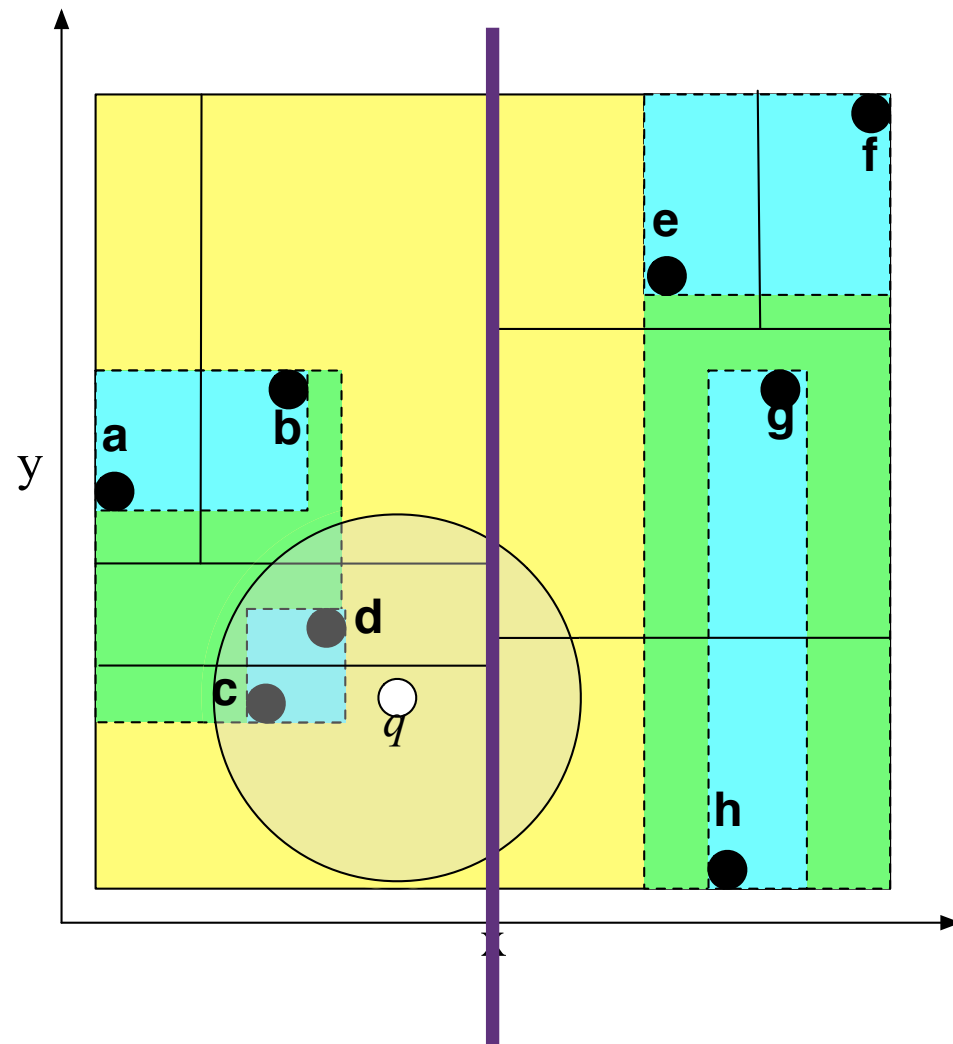
Pharmer

## Efficient and Exact Pharmacophore Search



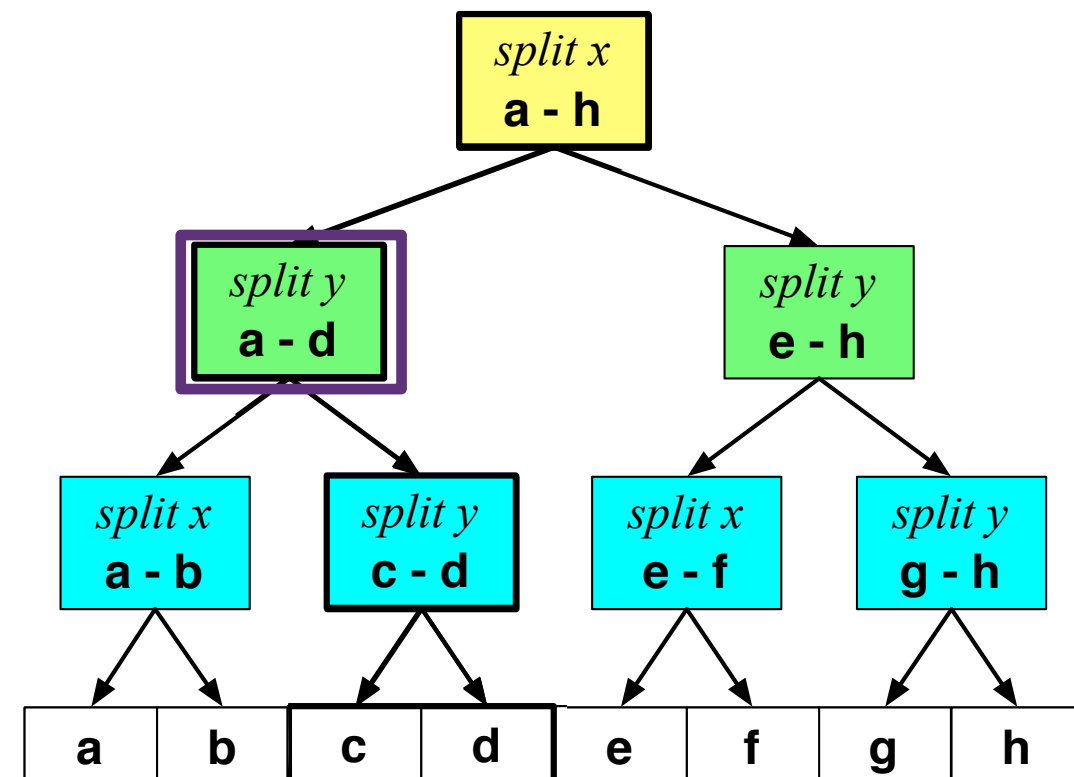
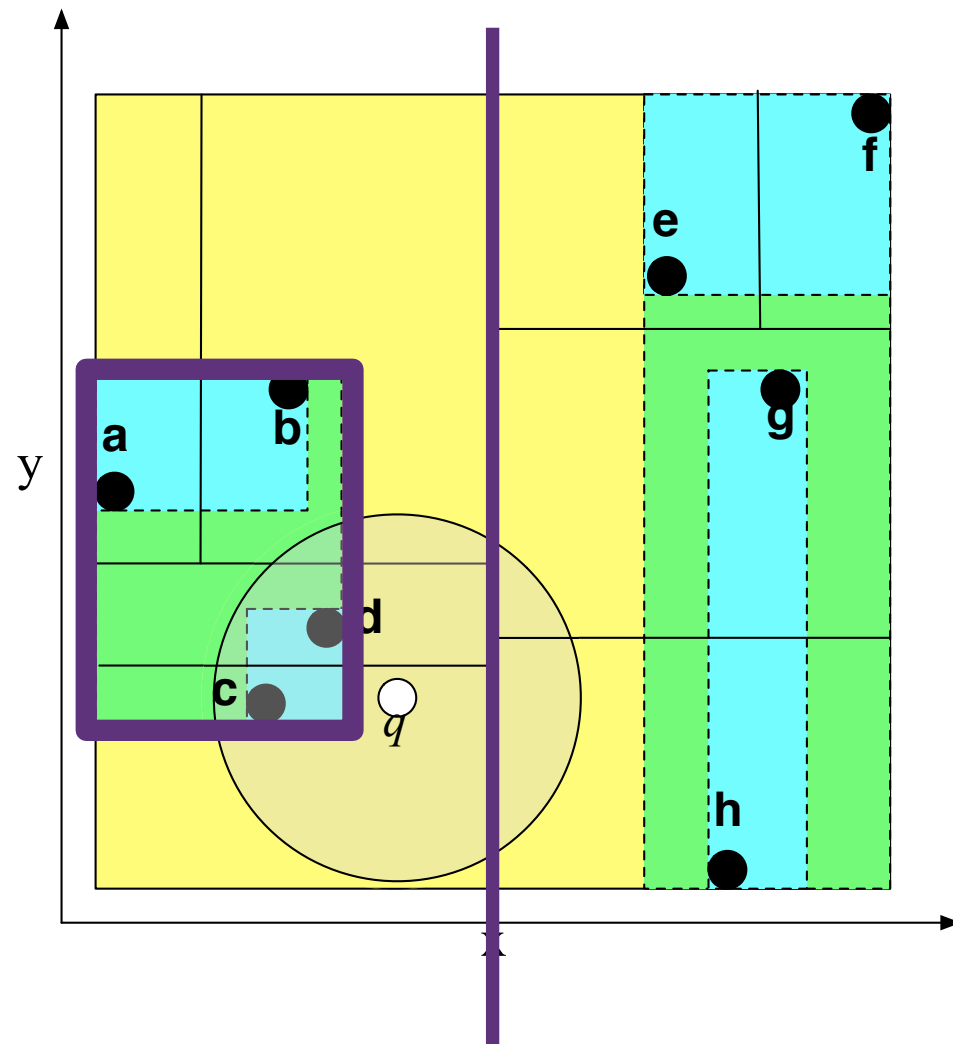
## Pharmer

## Efficient and Exact Pharmacophore Search



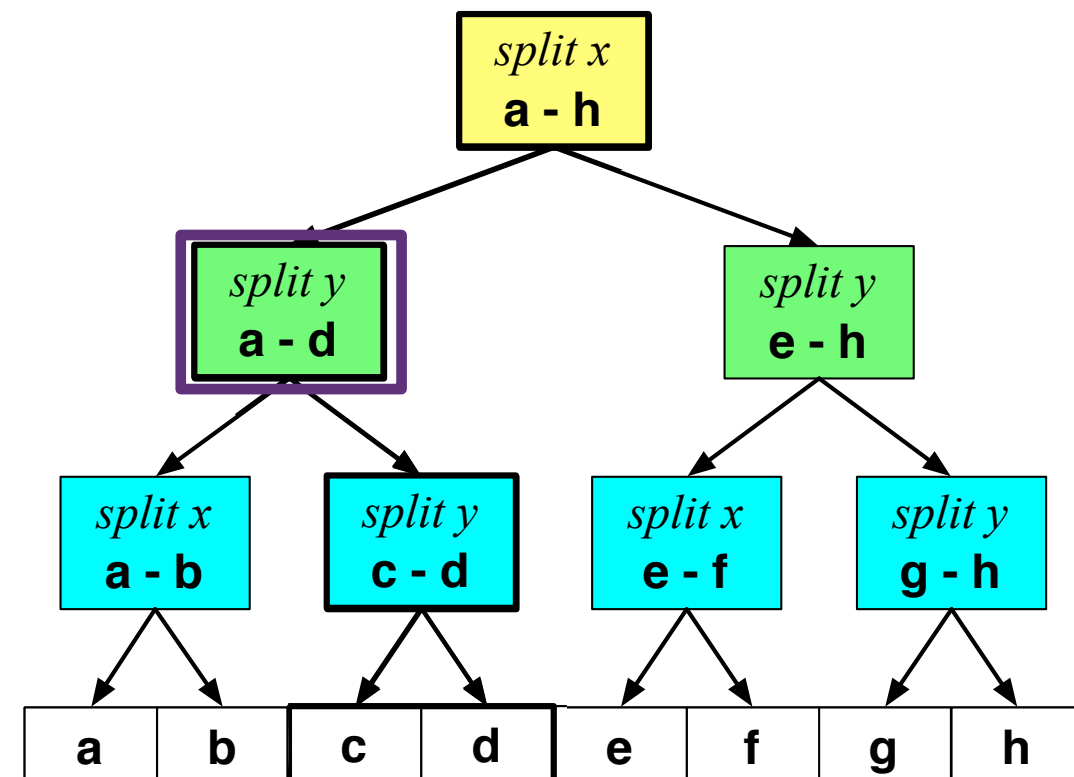
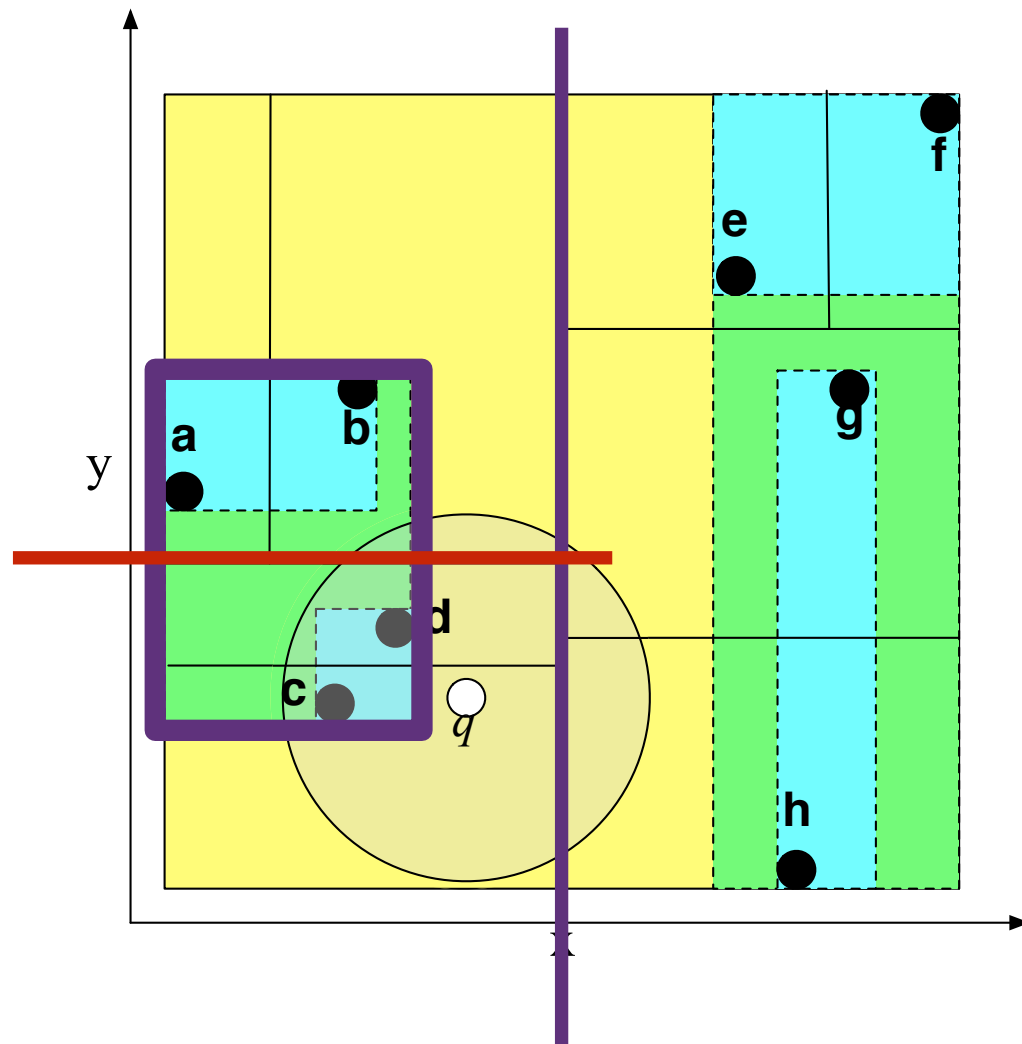
## Pharmer

## Efficient and Exact Pharmacophore Search



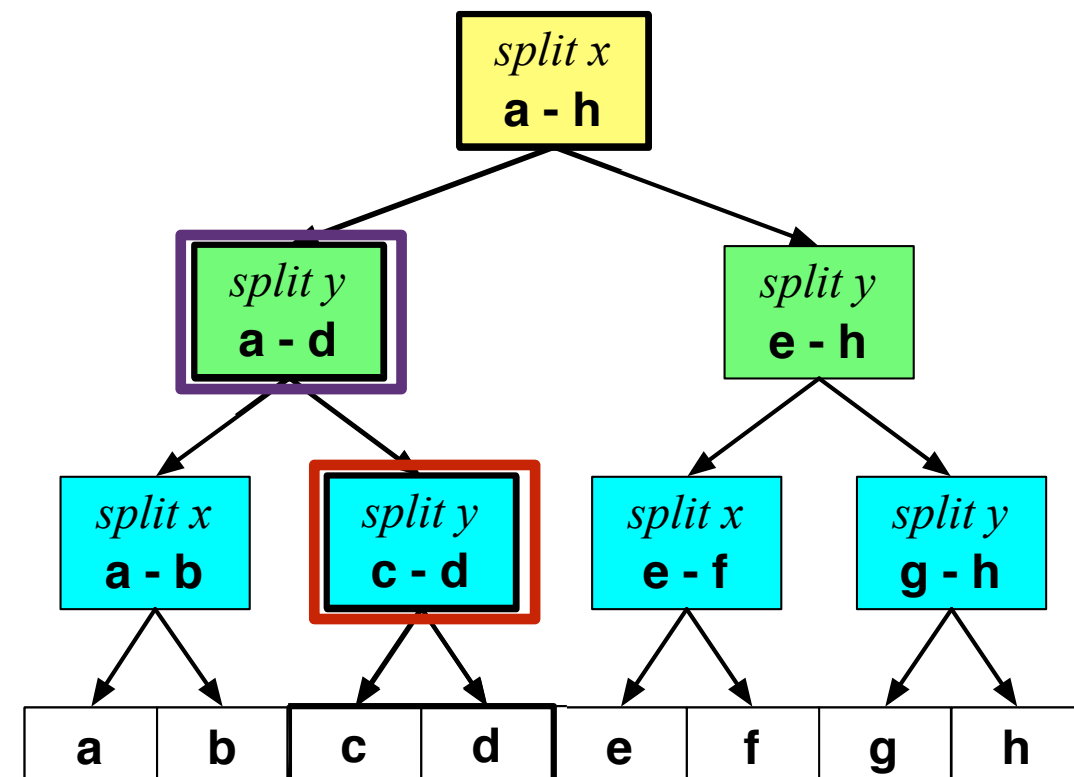
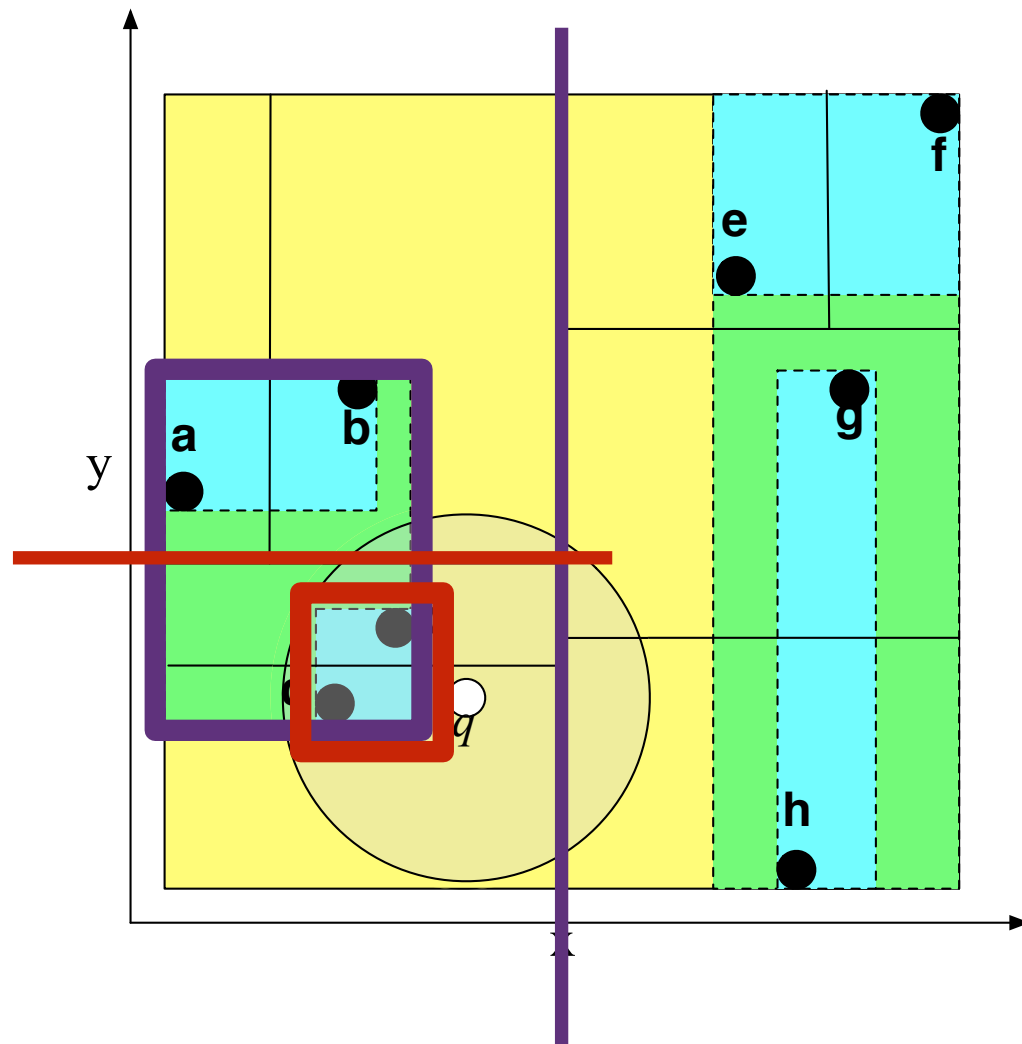
## Pharmer

## Efficient and Exact Pharmacophore Search



Pharmer

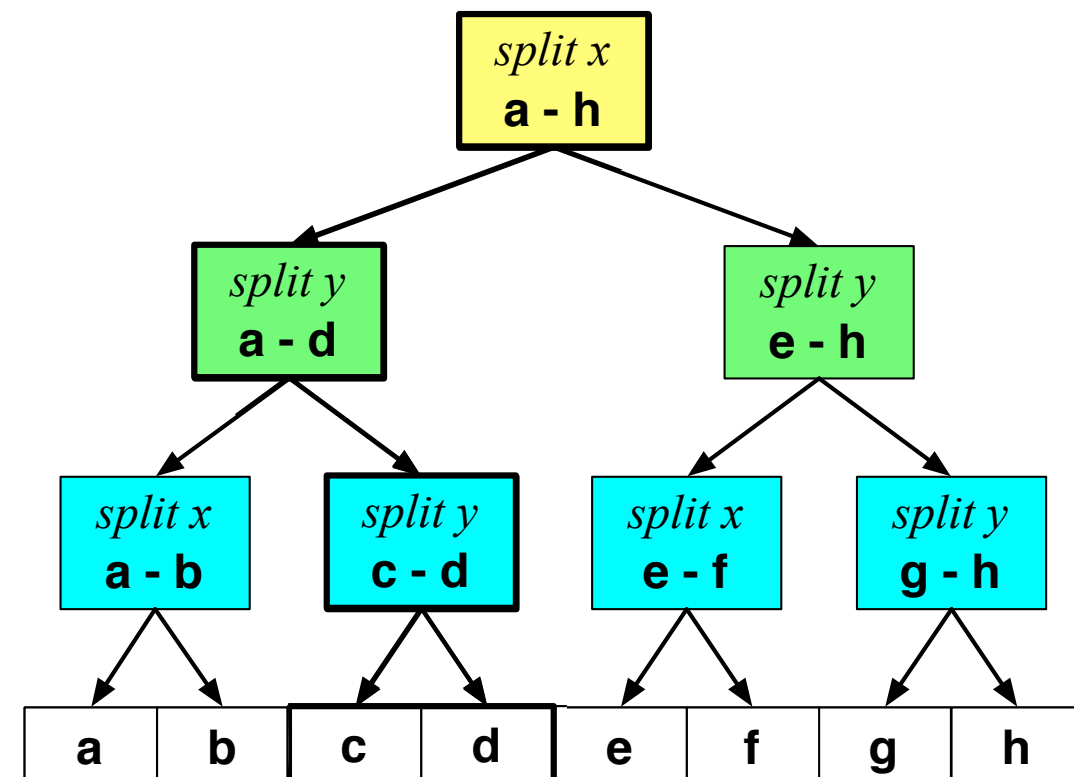
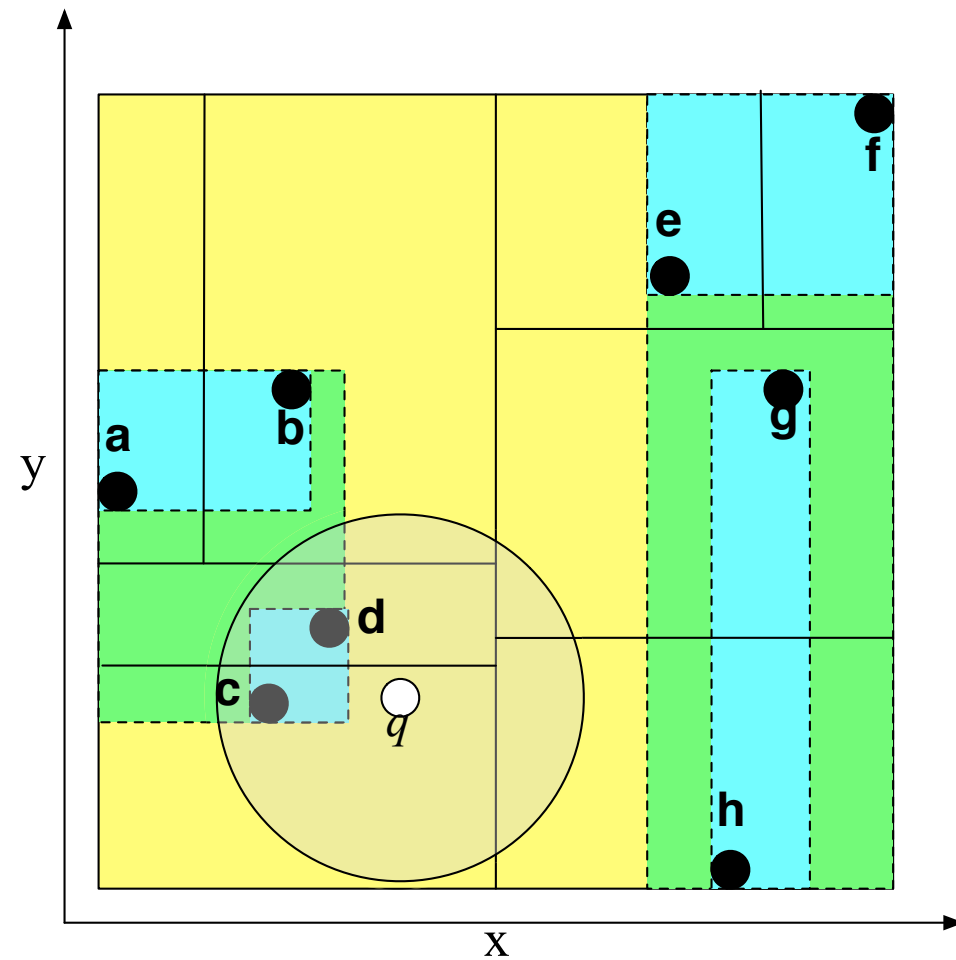
## Efficient and Exact Pharmacophore Search





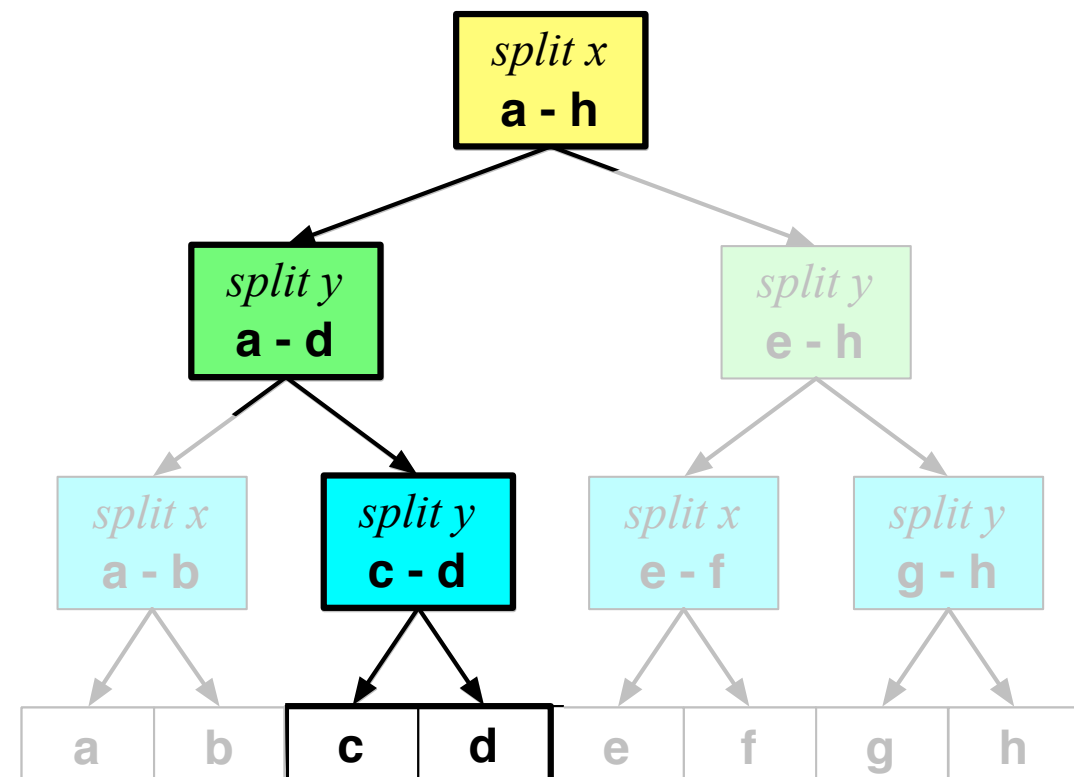
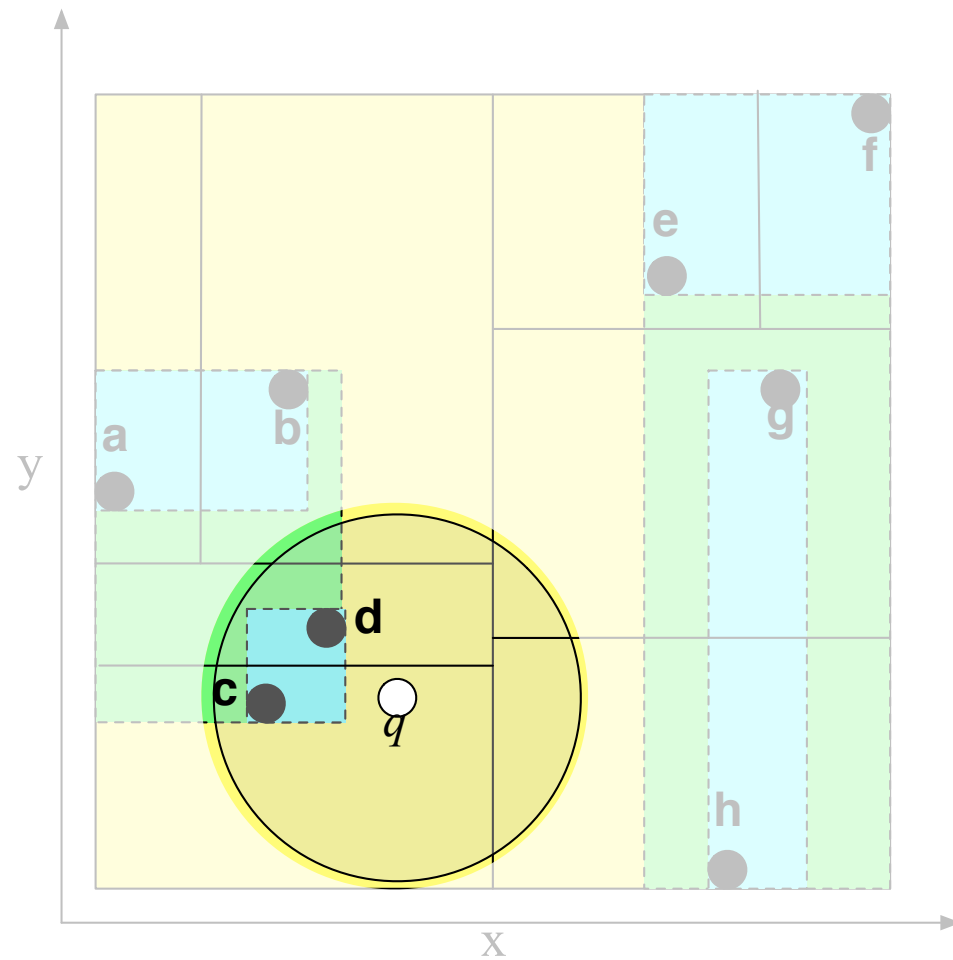
## Pharmer

## Efficient and Exact Pharmacophore Search



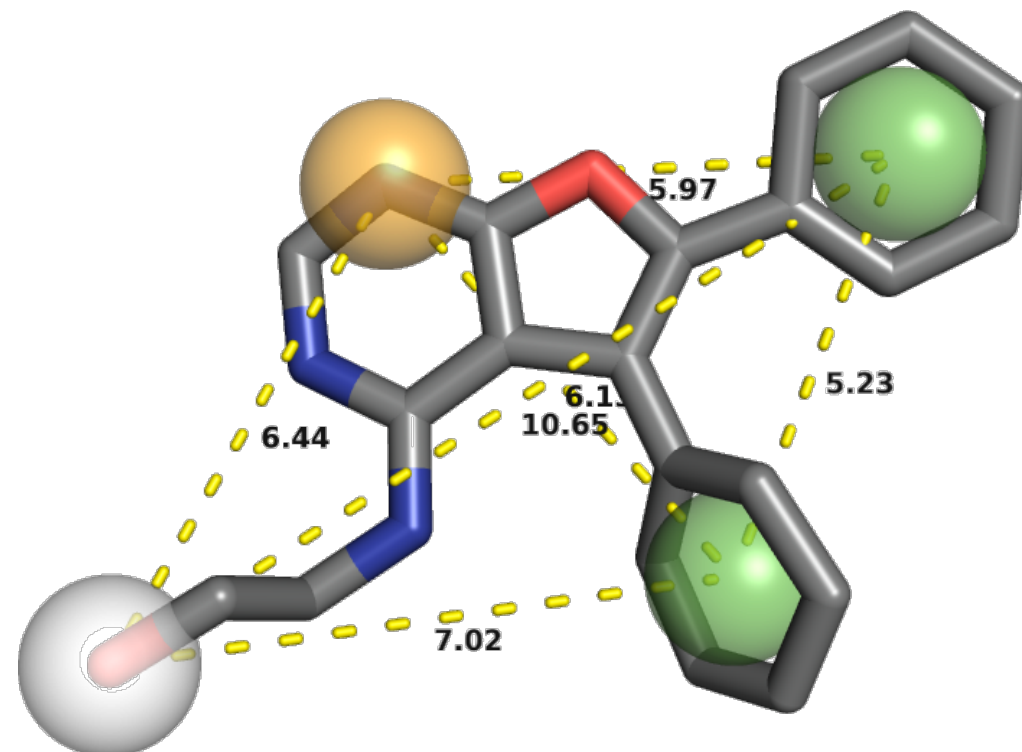
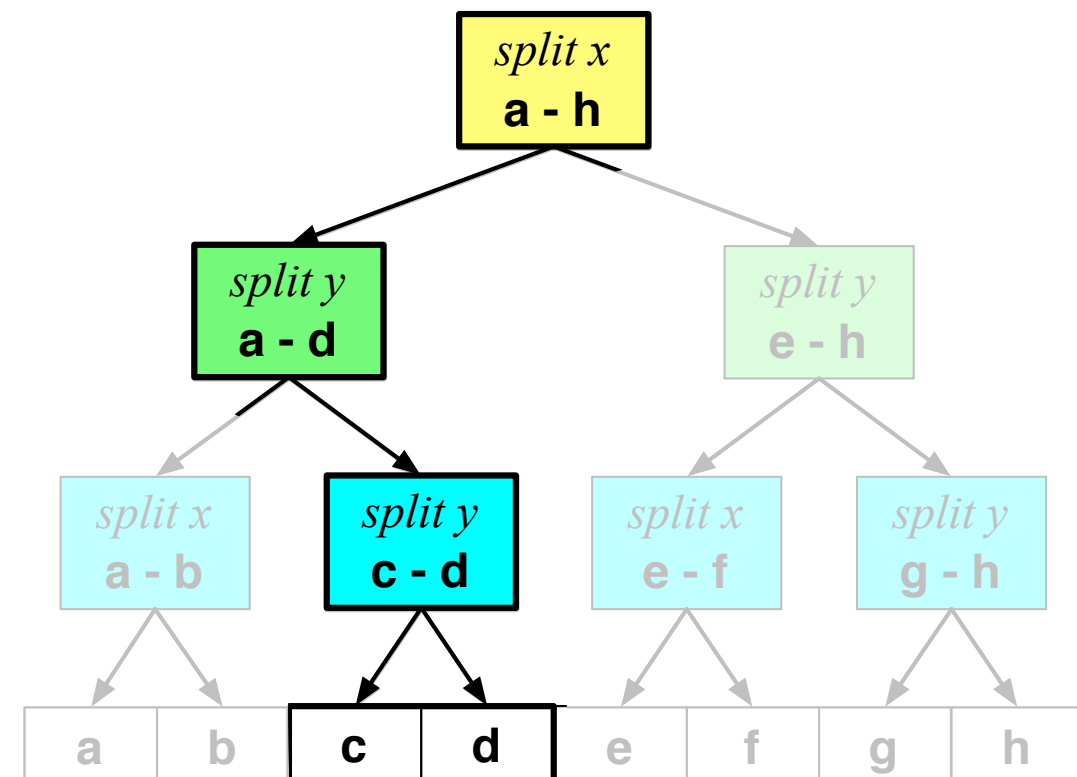
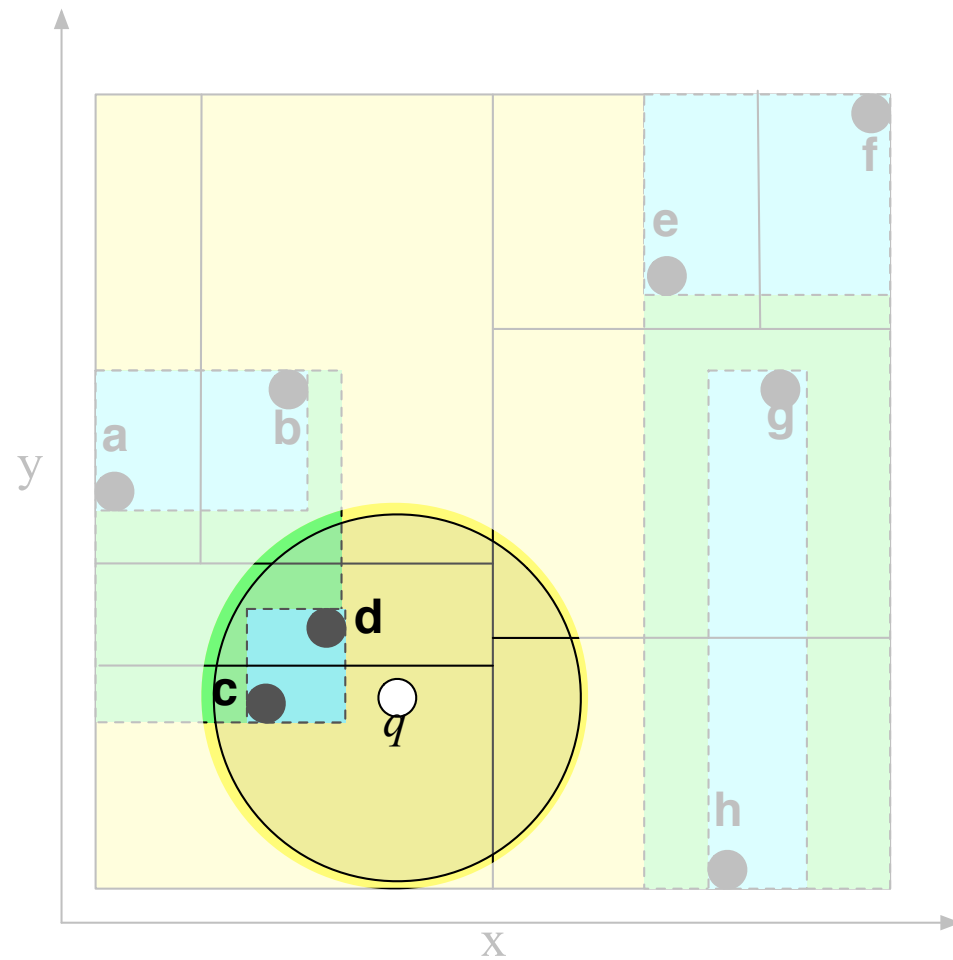
Pharmer

## Efficient and Exact Pharmacophore Search



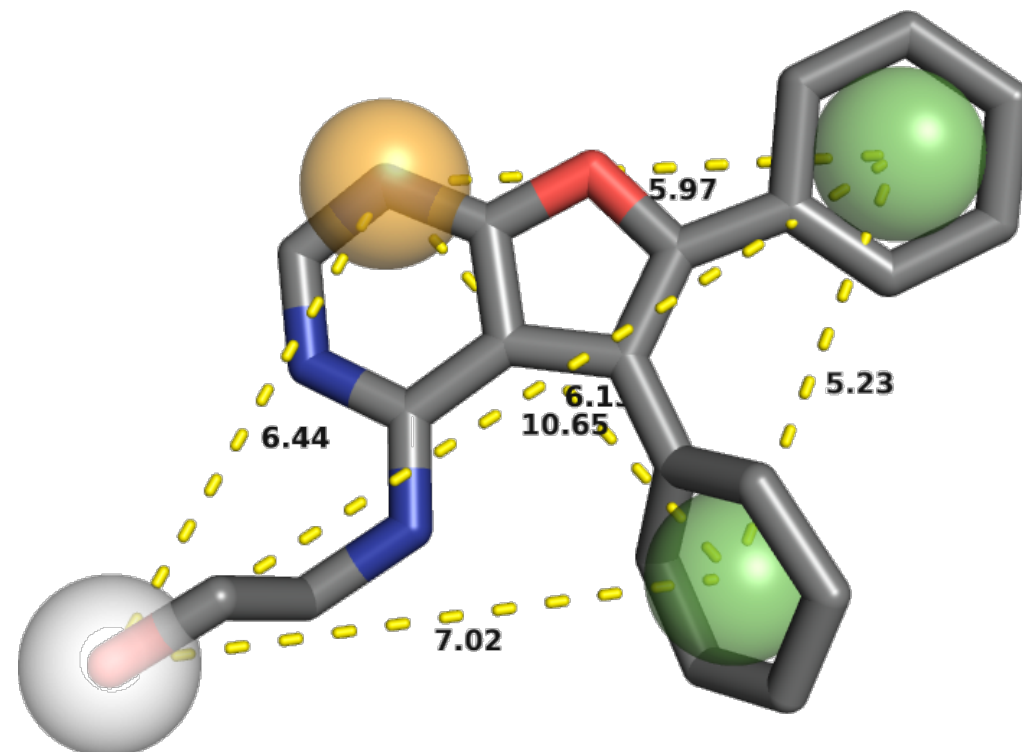
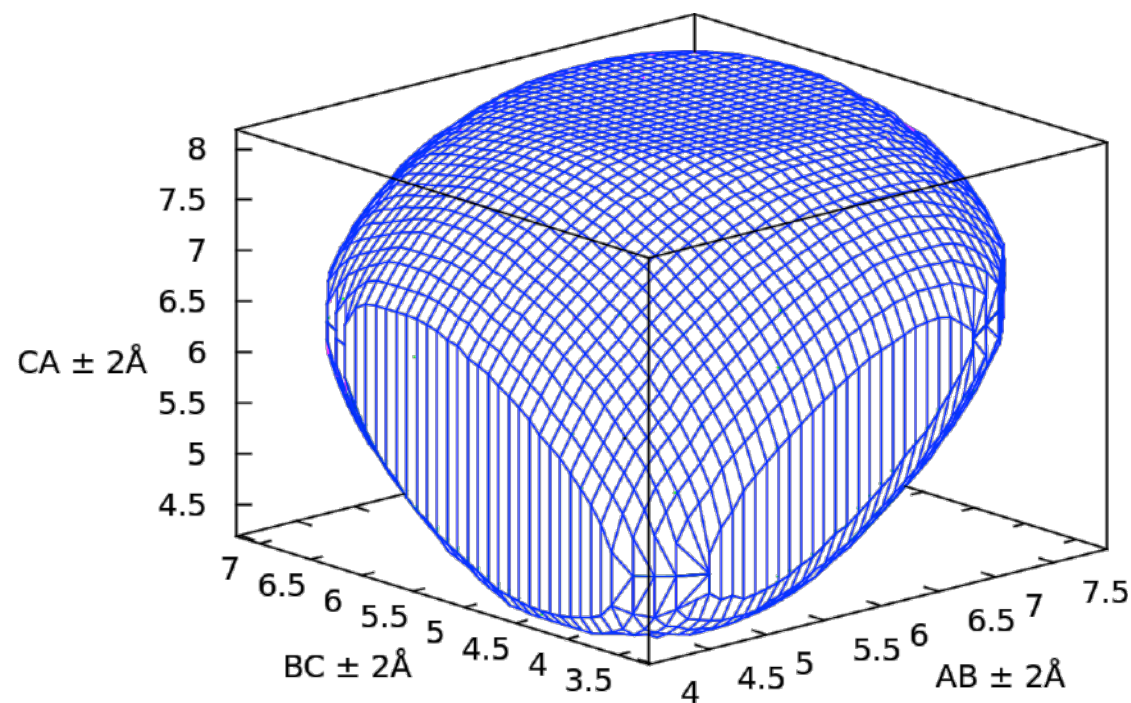
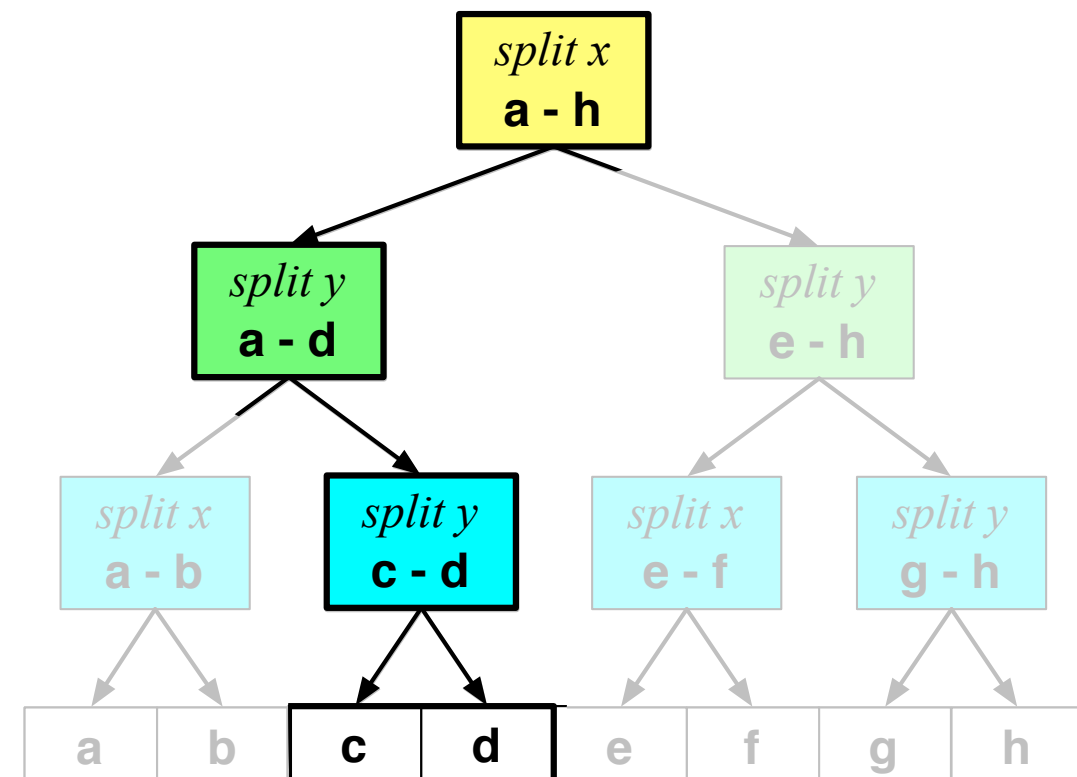
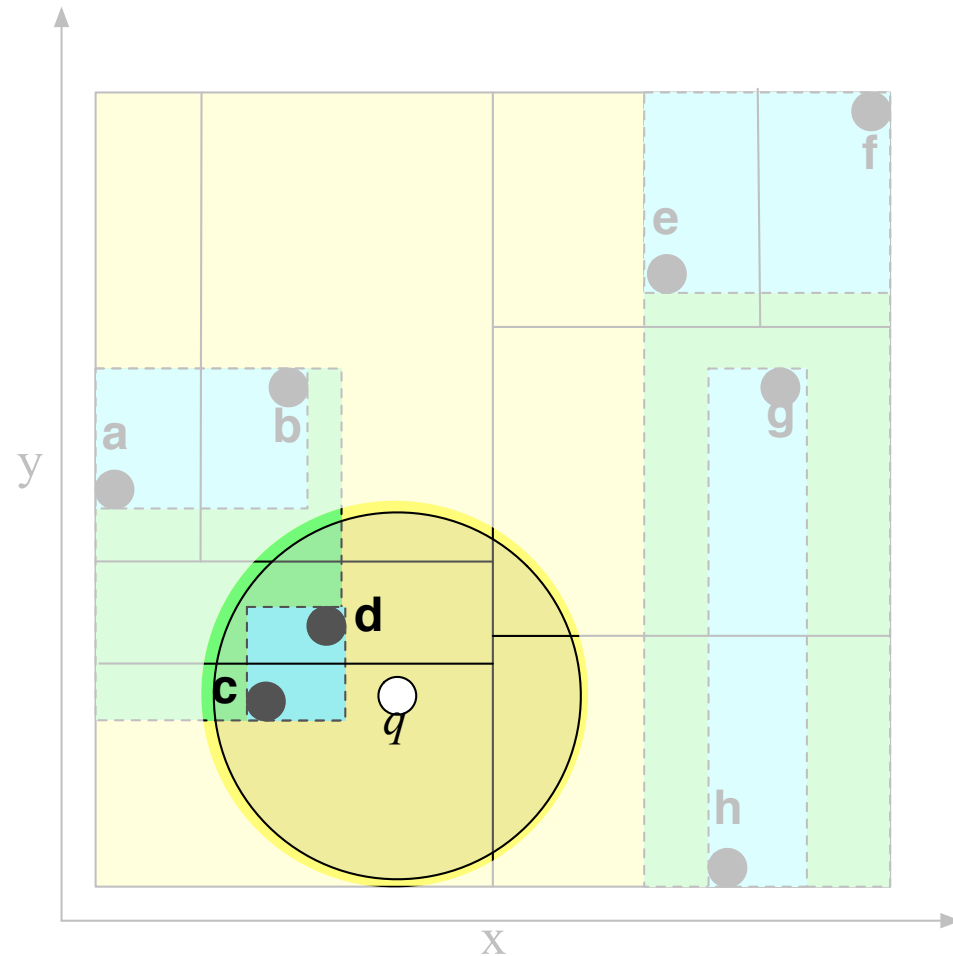
Pharmer

## Efficient and Exact Pharmacophore Search



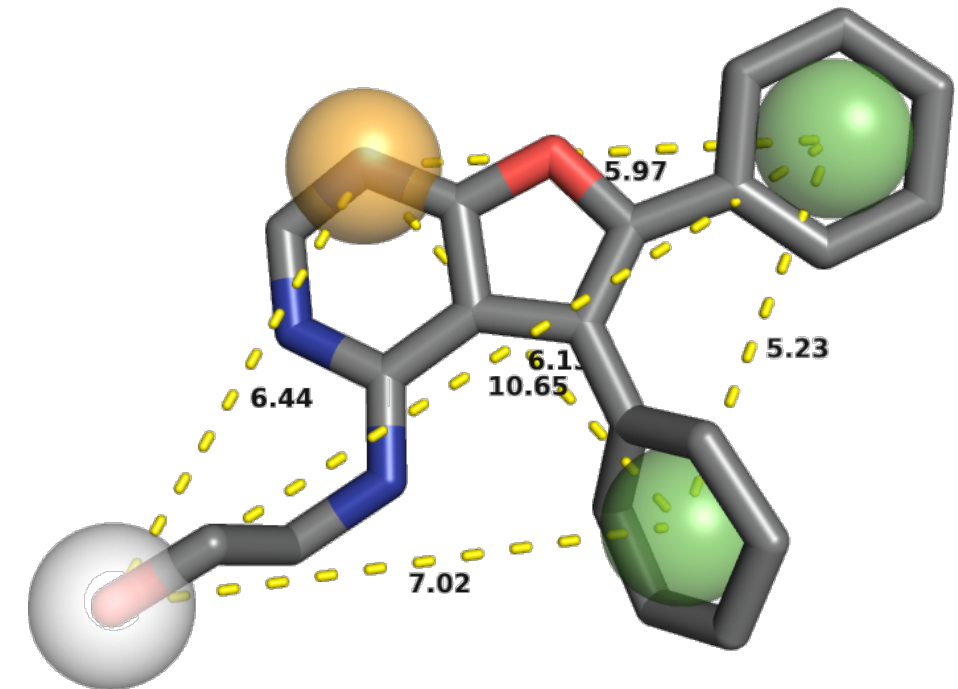
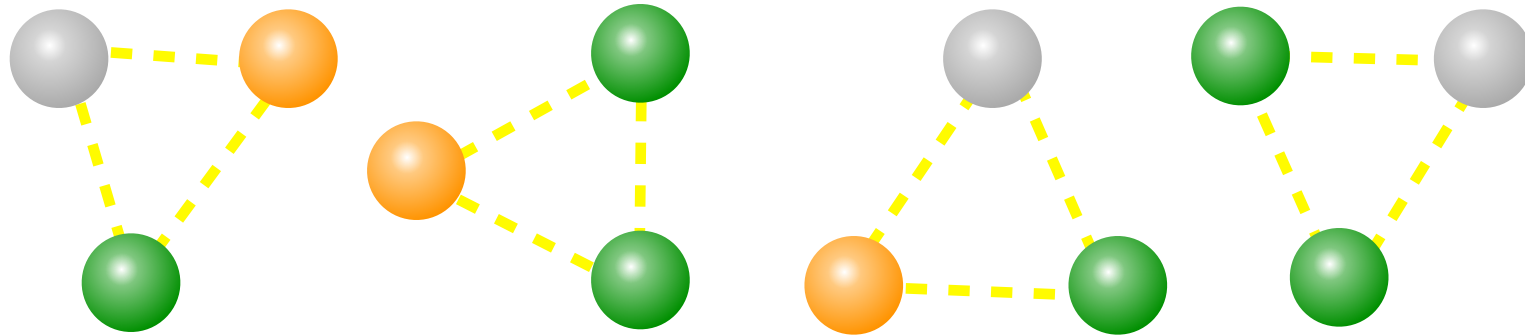
## Pharmer

## Efficient and Exact Pharmacophore Search



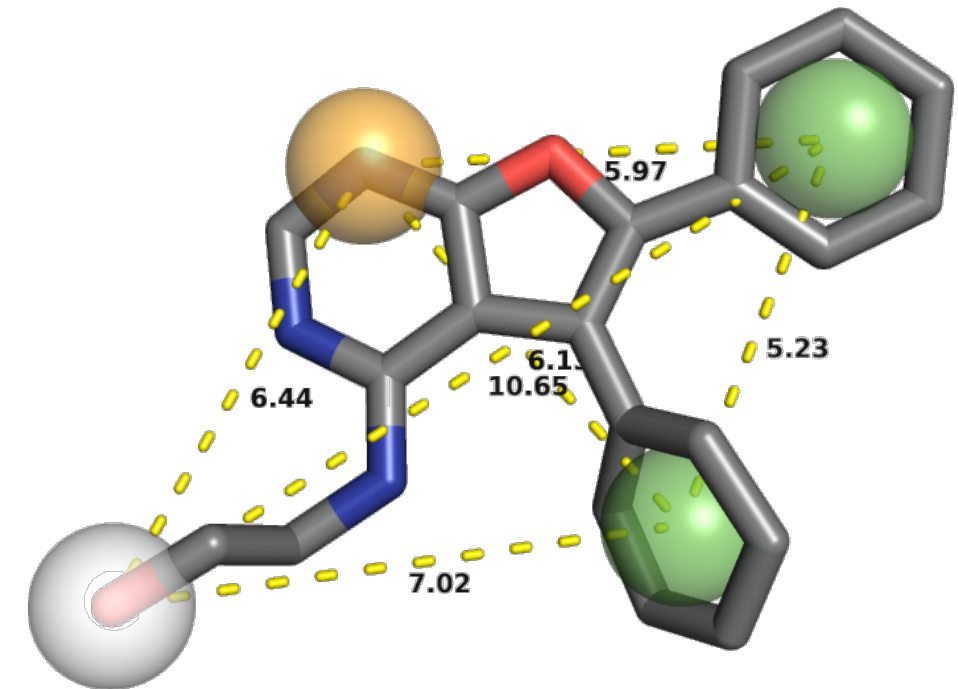
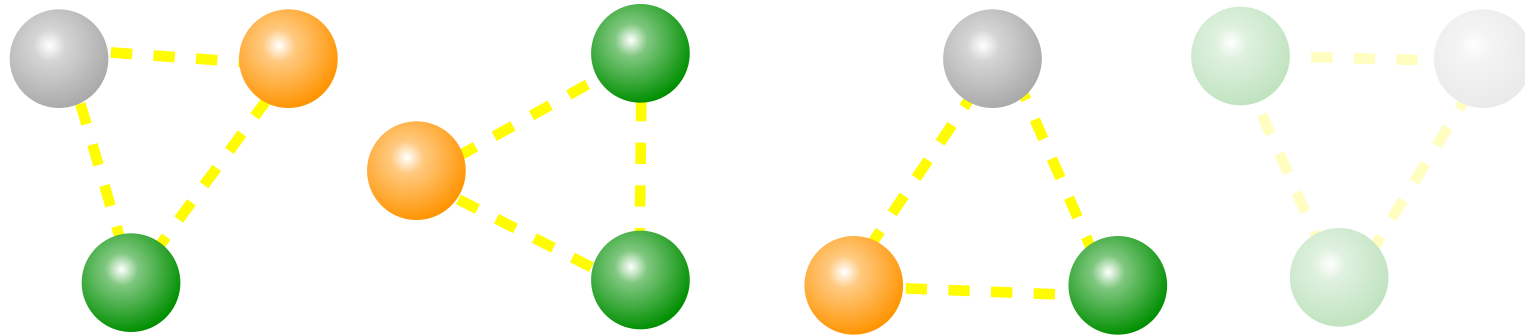
Pharmer

## Efficient and Exact Pharmacophore Search



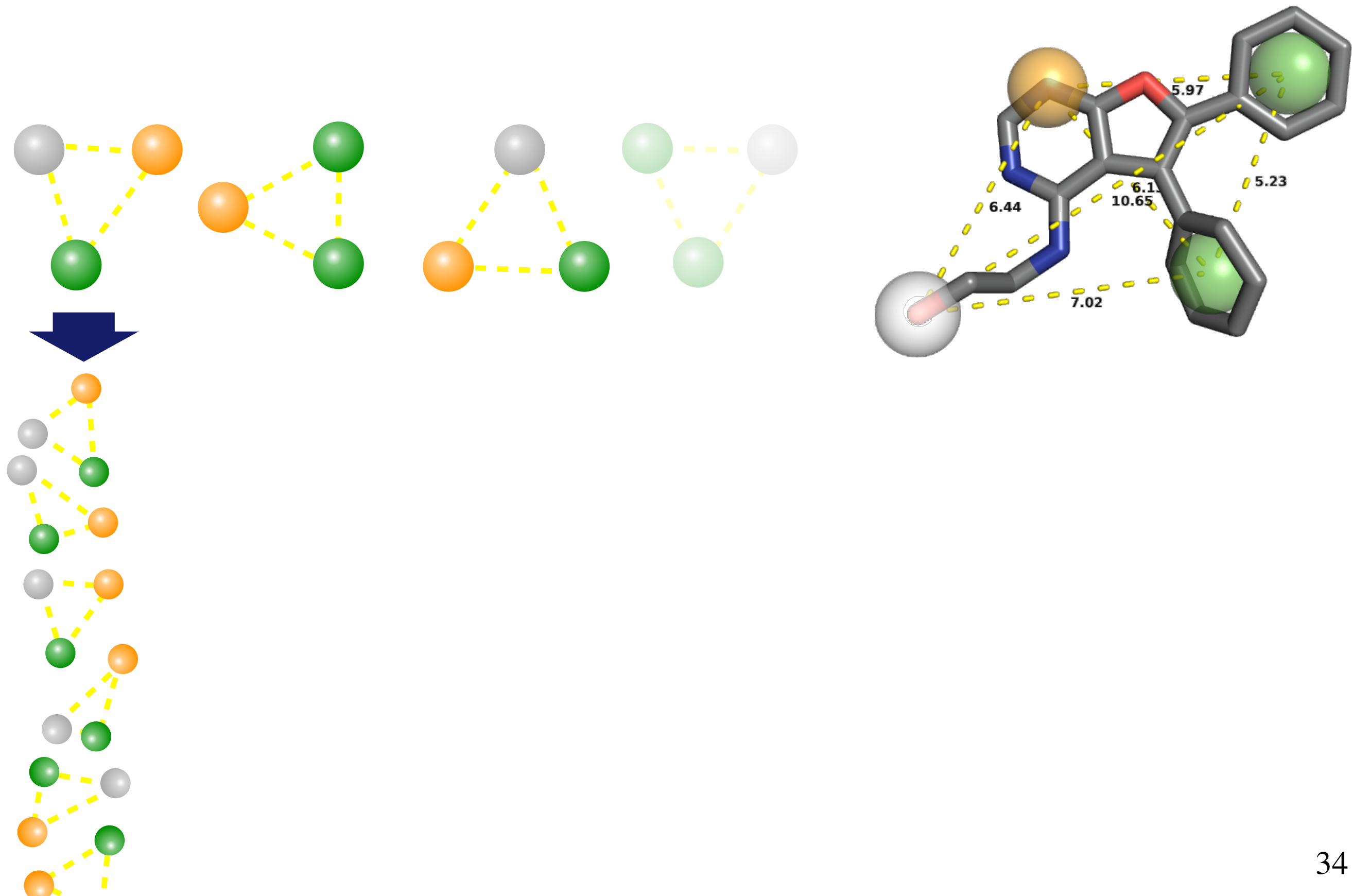
**Pharmer**

# Efficient and Exact Pharmacophore Search



**Pharmer**

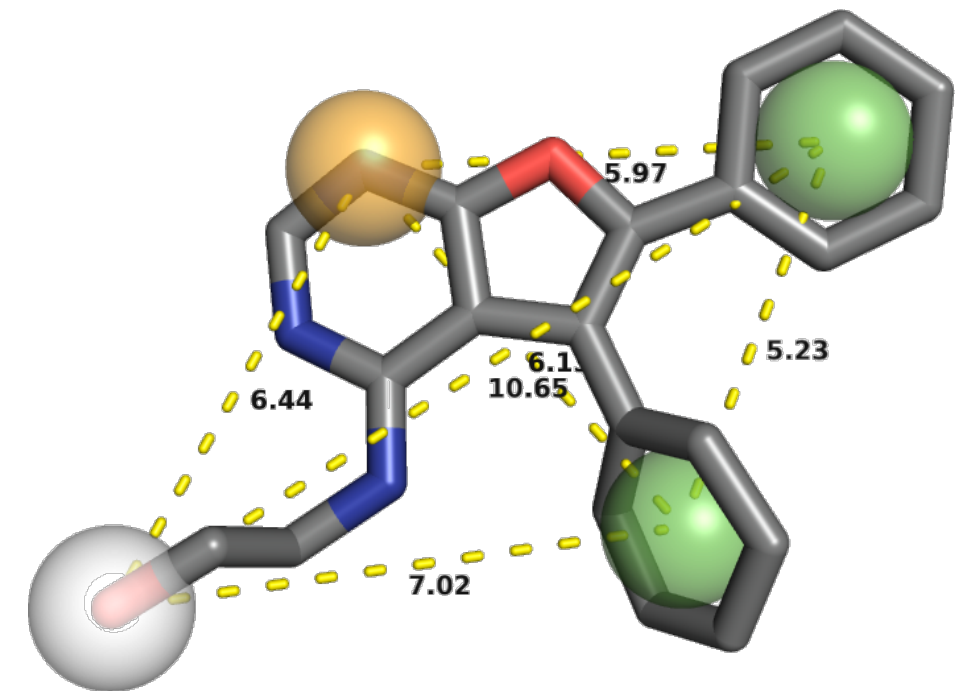
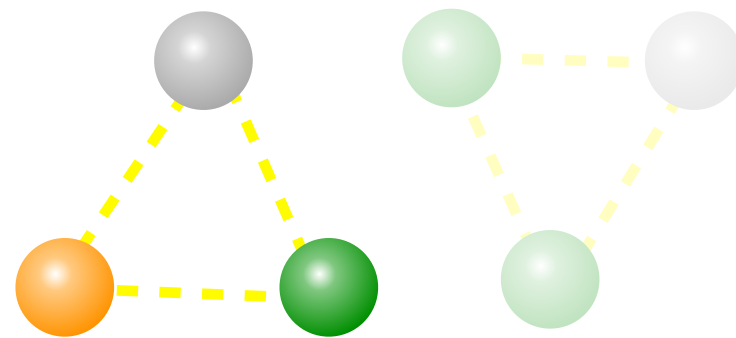
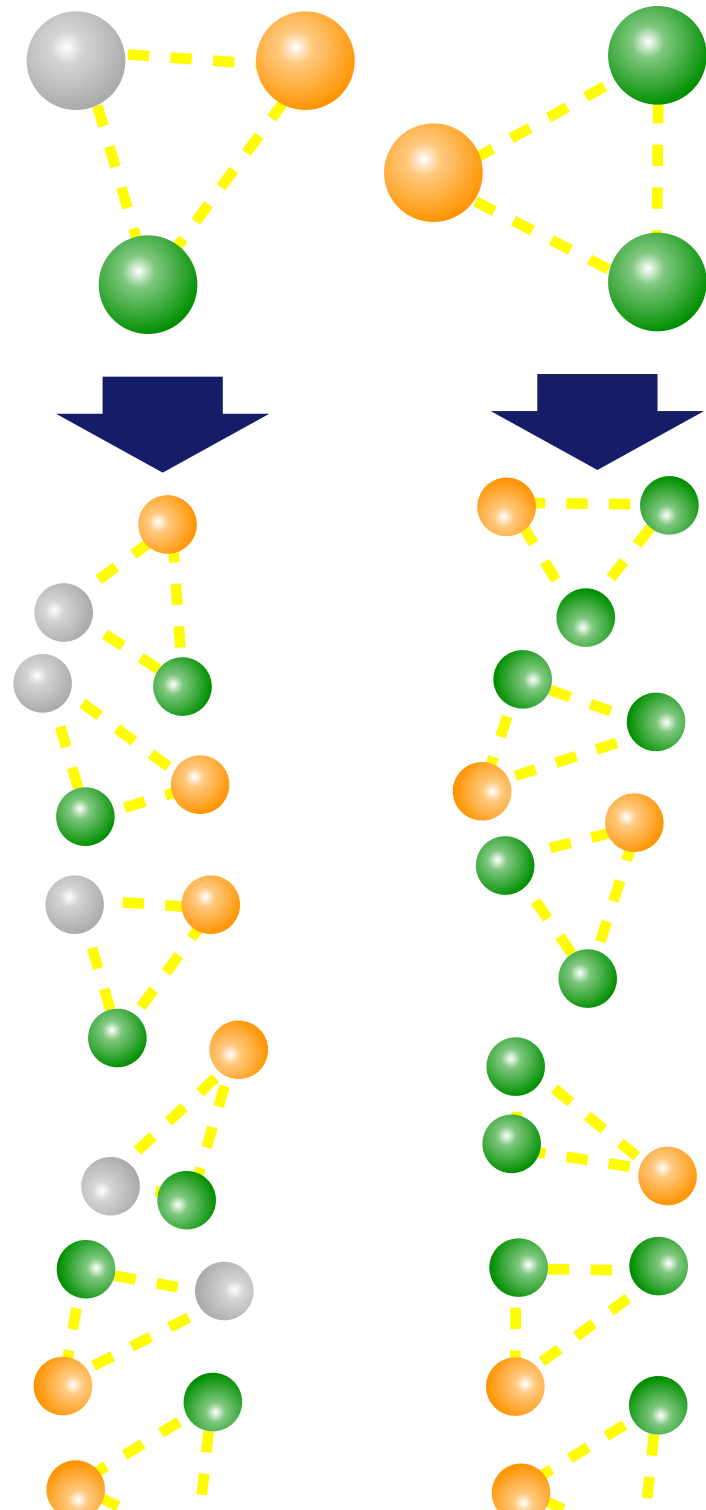
# Efficient and Exact Pharmacophore Search





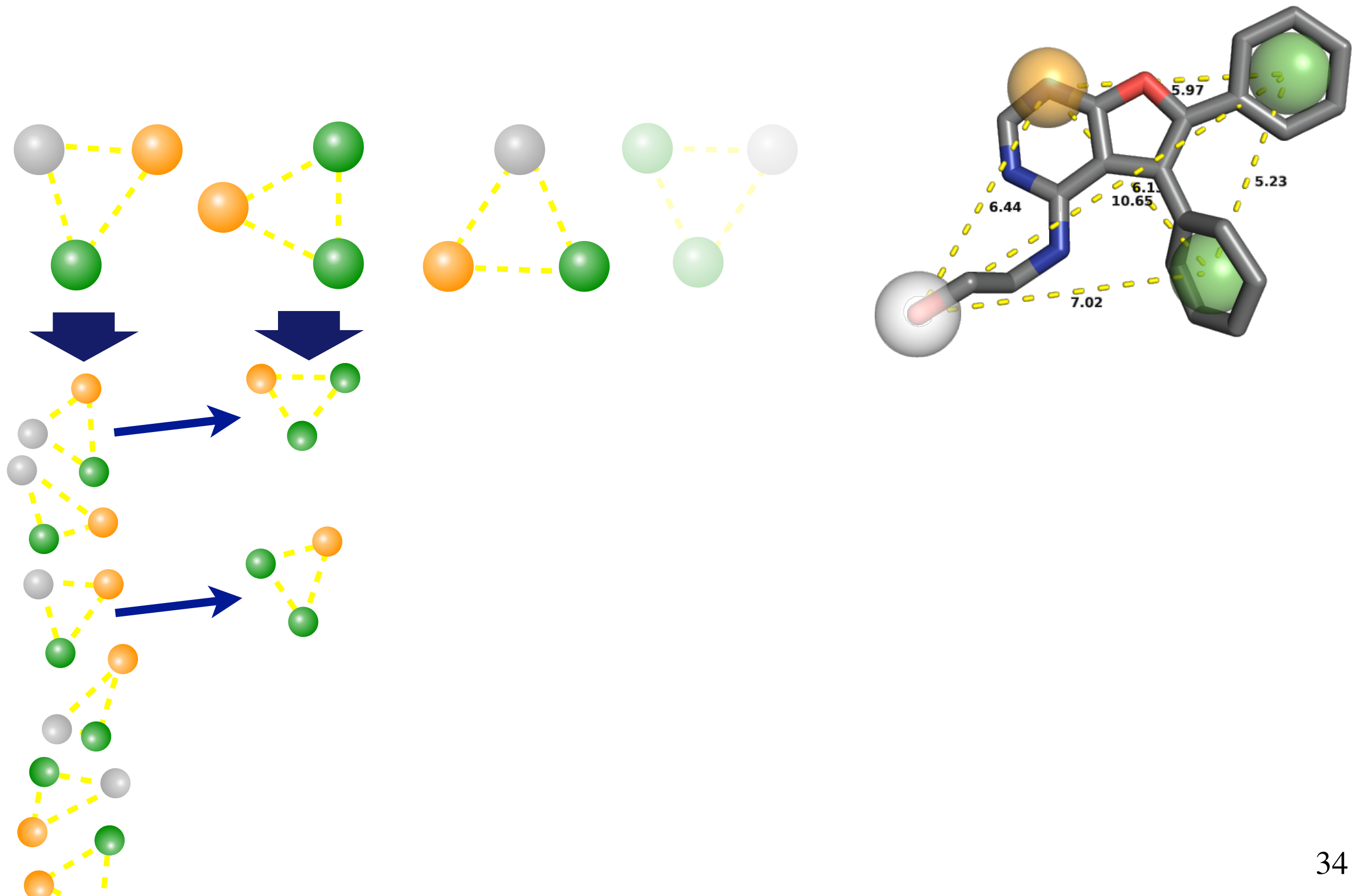
Pharmer

## Efficient and Exact Pharmacophore Search



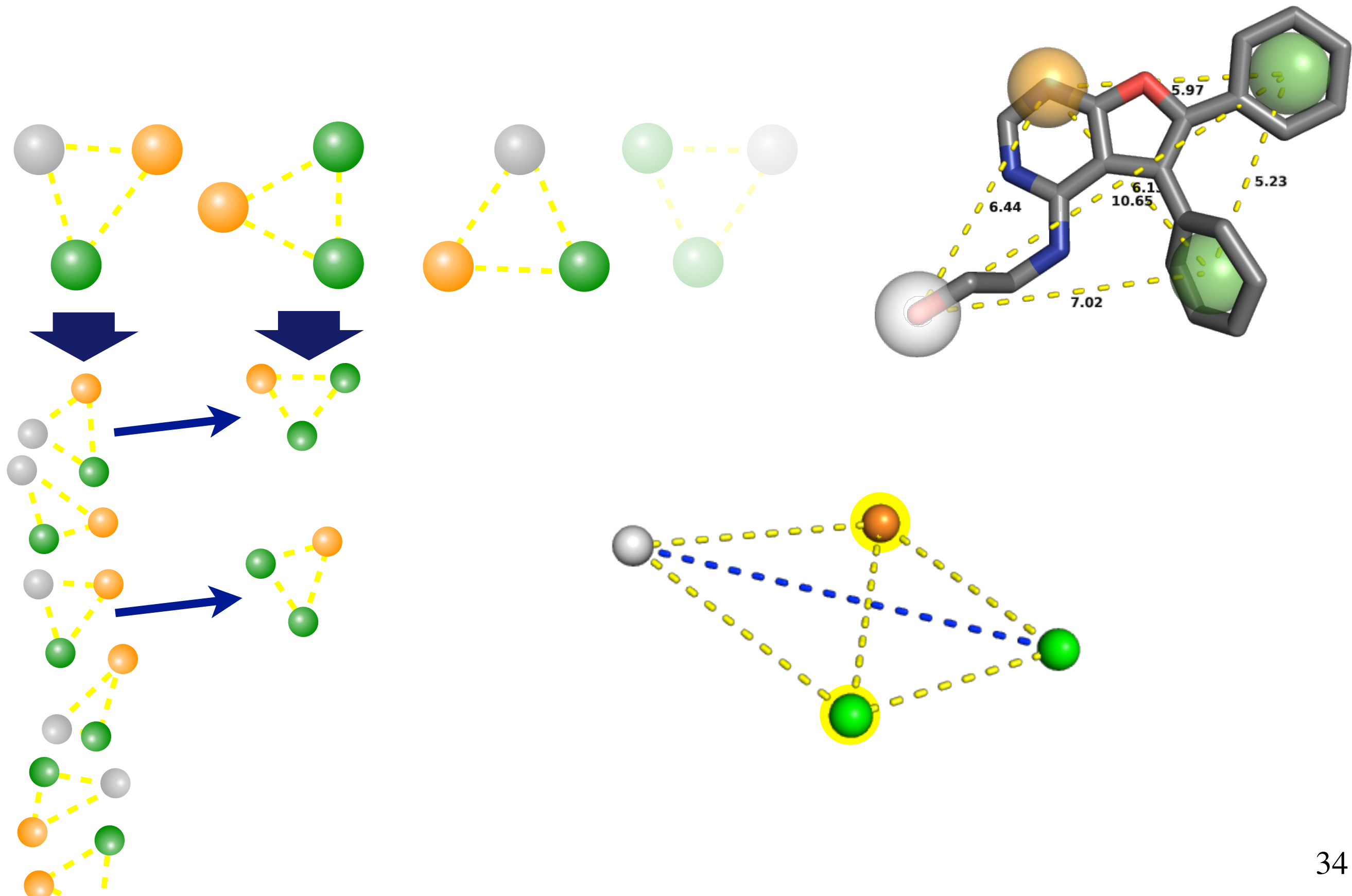
Pharmer

## Efficient and Exact Pharmacophore Search



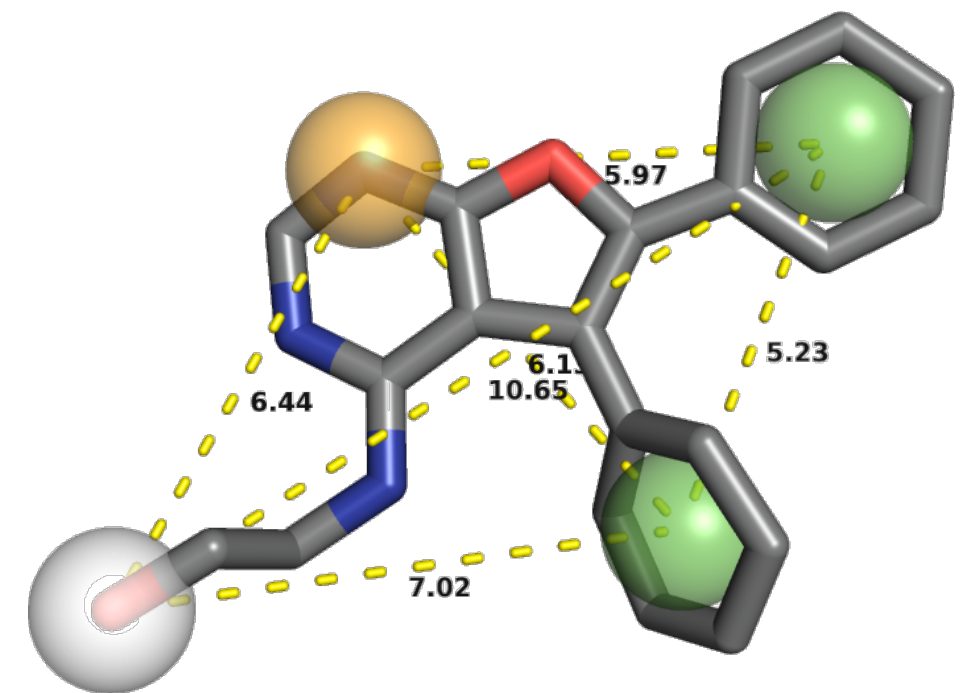
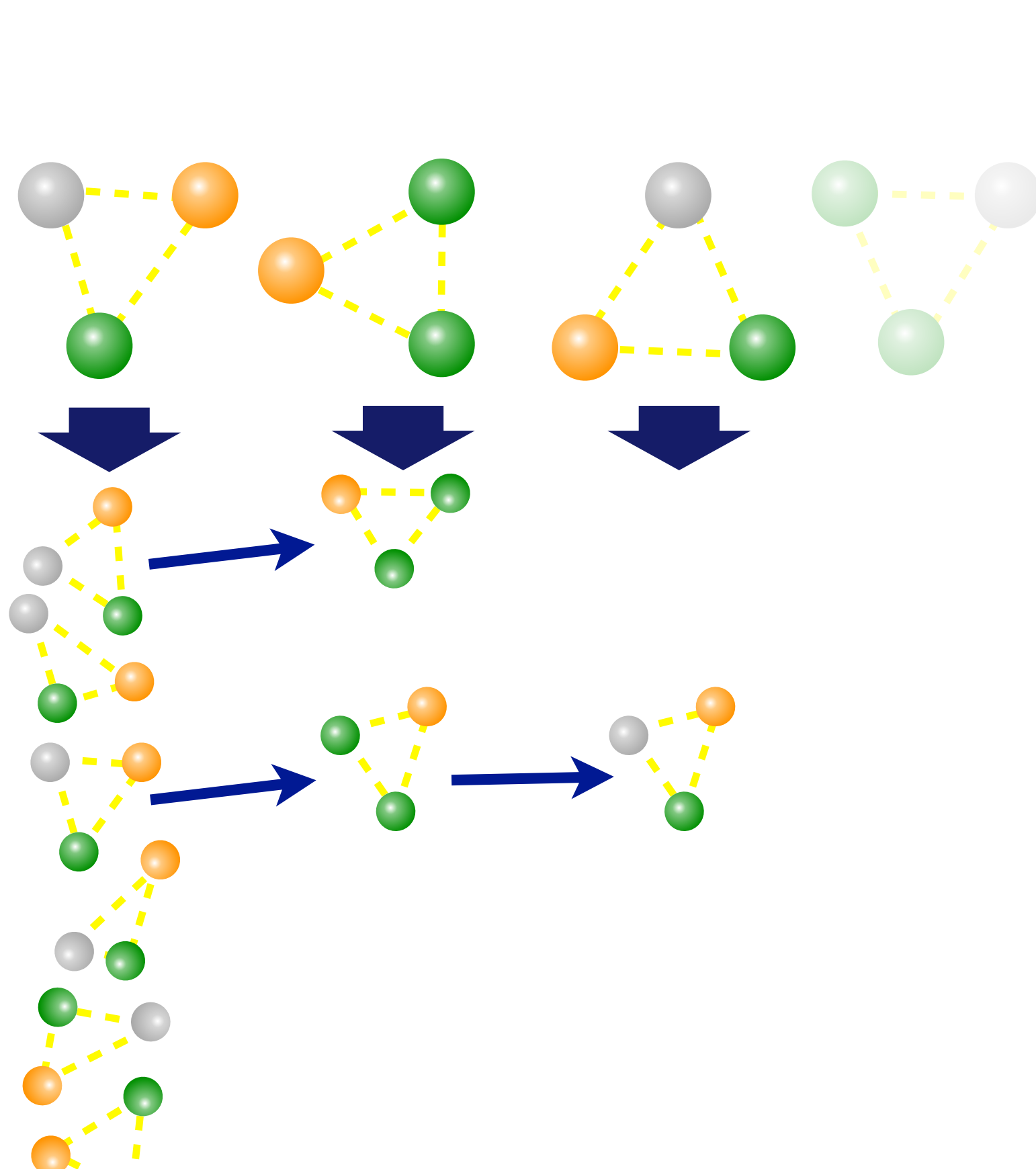
Pharmer

## Efficient and Exact Pharmacophore Search



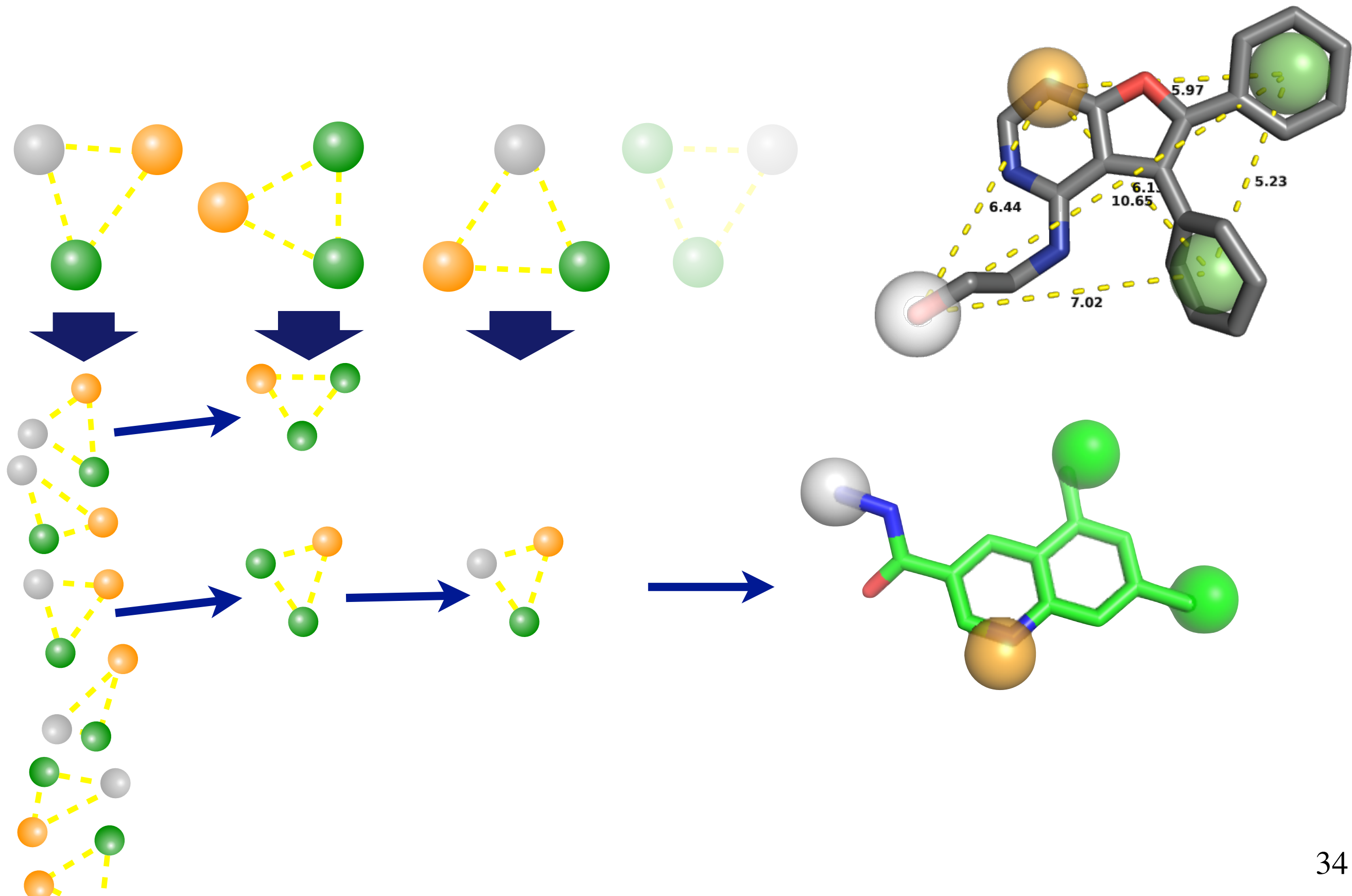
Pharmer

## Efficient and Exact Pharmacophore Search



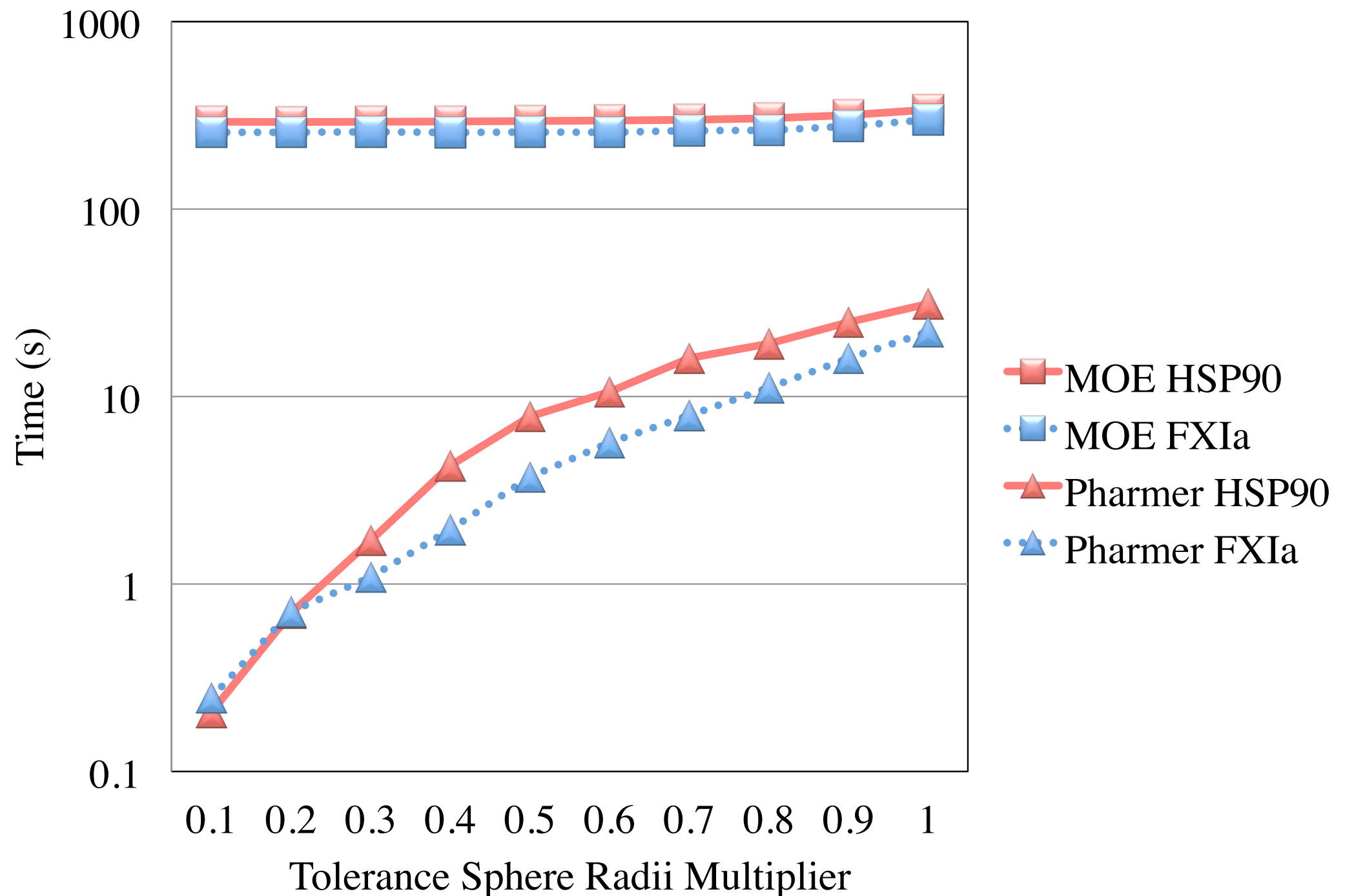
Pharmer

## Efficient and Exact Pharmacophore Search



Pharmer

## Efficient and Exact Pharmacophore Search





pharmit.csb.pitt.edu/search.html

Search PubChem

Pharmacophore Search -> Shape Filter

Load Receptor... Load Features...

### Pharmacophore

- ☒ **Aromatic**  
(48.19,39.88,-1.88) Radius 1.1
- ☒ **HydrogenAcceptor**  
(47.17,41.23,-5.87) Radius 0.5
- ☒ **HydrogenAcceptor**  
(49.17,40.46,-6.38) Radius 0.5
- ☒ **NegativeIon**  
(48.21,40.91,-5.92) Radius 0.75
- ☒ **Hydrophobic**  
(49.4,41.67,-2.93) Radius 1.0
- ☒ **Hydrophobic**  
(52.08,44.85,-2.15) Radius 1.0
- ☒ **Hydrophobic**  
(48.19,39.88,-1.88) Radius 1.0
- ☒ **Hydrophobic**  
(55.14,47.7,-1.04) Radius 1.0
- ☒ **Hydrophobic**  
(50.03,43.31,-5.25) Radius 1.0
- ☒ **Hydrophobic**  
(46.4,37.97,-1.96) Radius 1.0
- ☐ **Aromatic**  
(49.4,41.67,-2.93) Radius 1.1
- ☐ **Aromatic**  
(52.08,44.85,-2.15) Radius 1.1

Load Session... Save Session...

Display a menu

### Pharmacophore Results

| Name             | RMSD  | Mass | RBnds |
|------------------|-------|------|-------|
| PubChem-13960682 | 0.223 | 392  | 5     |
| PubChem-23673360 | 0.223 | 391  | 4     |
| PubChem-13960682 | 0.223 | 392  | 5     |
| PubChem-23673360 | 0.223 | 391  | 4     |
| PubChem-13960684 | 0.243 | 388  | 6     |
| PubChem-13960684 | 0.243 | 388  | 6     |
| PubChem-13960684 | 0.243 | 388  | 6     |
| PubChem-13960684 | 0.250 | 388  | 6     |
| PubChem-59810304 | 0.311 | 481  | 8     |
| PubChem-10000399 | 0.325 | 389  | 6     |
| PubChem-10000399 | 0.327 | 389  | 6     |
| PubChem-59081061 | 0.349 | 875  | 15    |
| PubChem-10250942 | 0.379 | 387  | 3     |
| PubChem-23686481 | 0.379 | 386  | 2     |
| PubChem-13960681 | 0.442 | 385  | 7     |
| PubChem-13960681 | 0.442 | 385  | 7     |
| PubChem-13960681 | 0.444 | 385  | 7     |
| PubChem-88181354 | 0.449 | 698  | 10    |
| PubChem-842716   | 0.462 | 319  | 8     |

Showing 1 to 19 of 38 hits

Previous 1 2 Next

Minimize Save...

<http://pharmit.csb.pitt.edu>



# Kinds of Virtual Screening

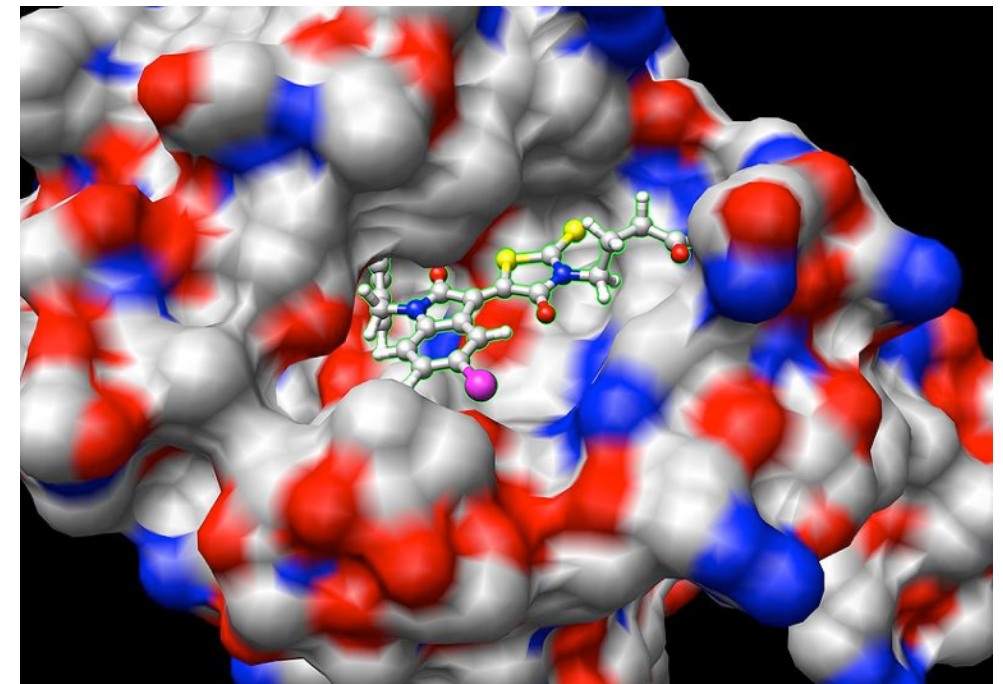
## ADMET

## Ligand Based

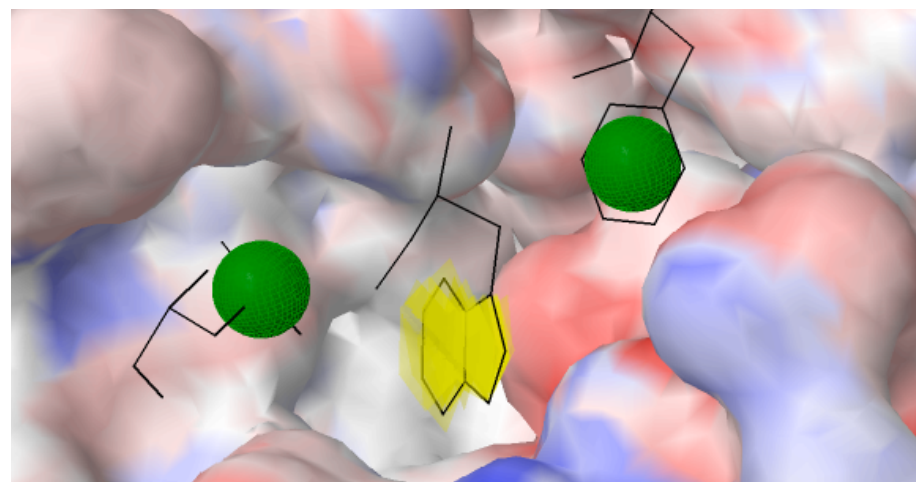
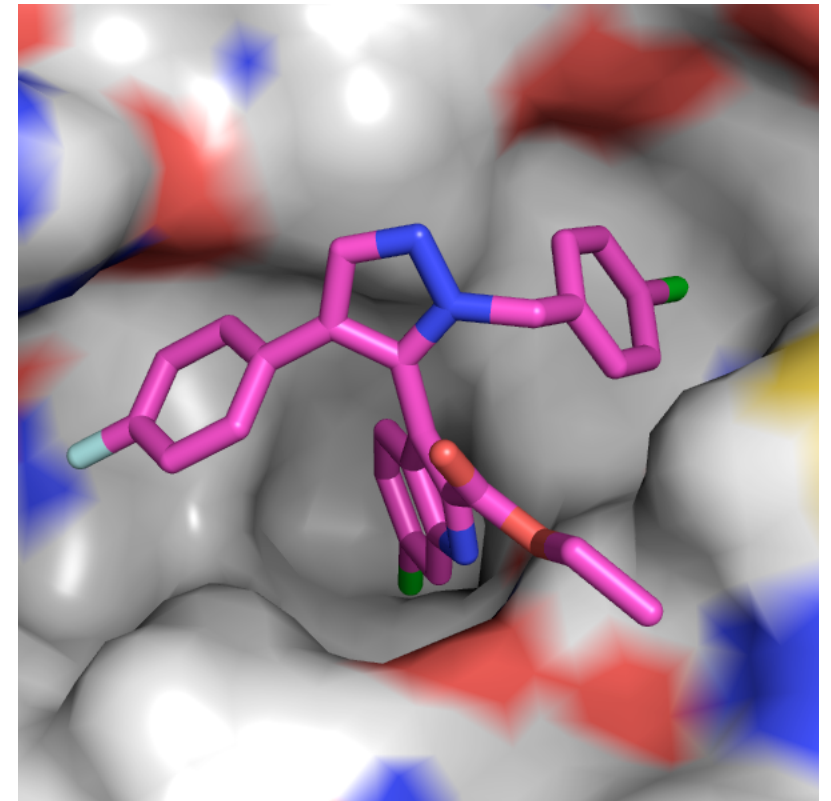
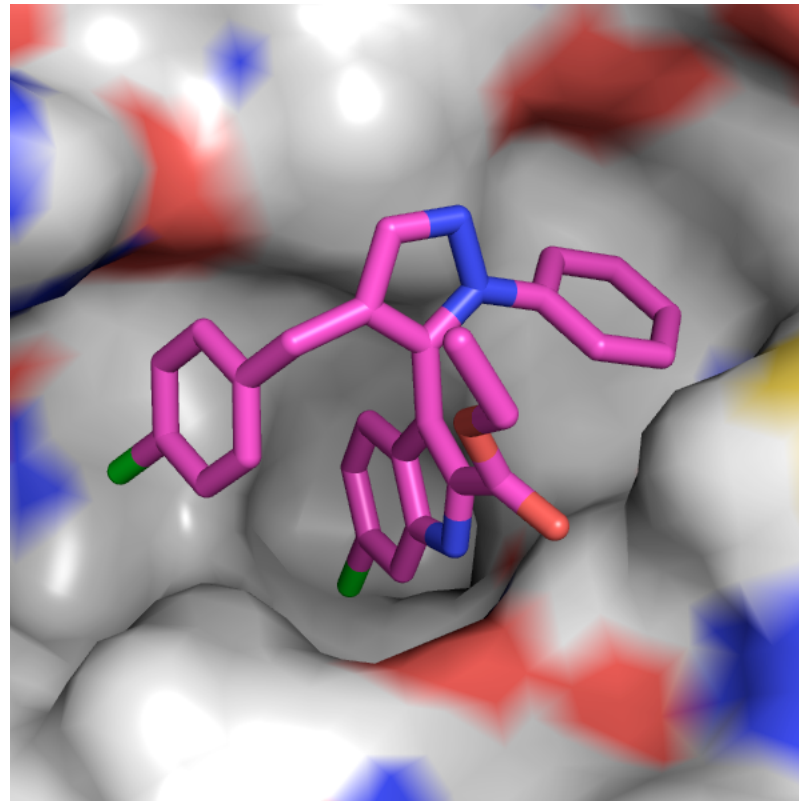
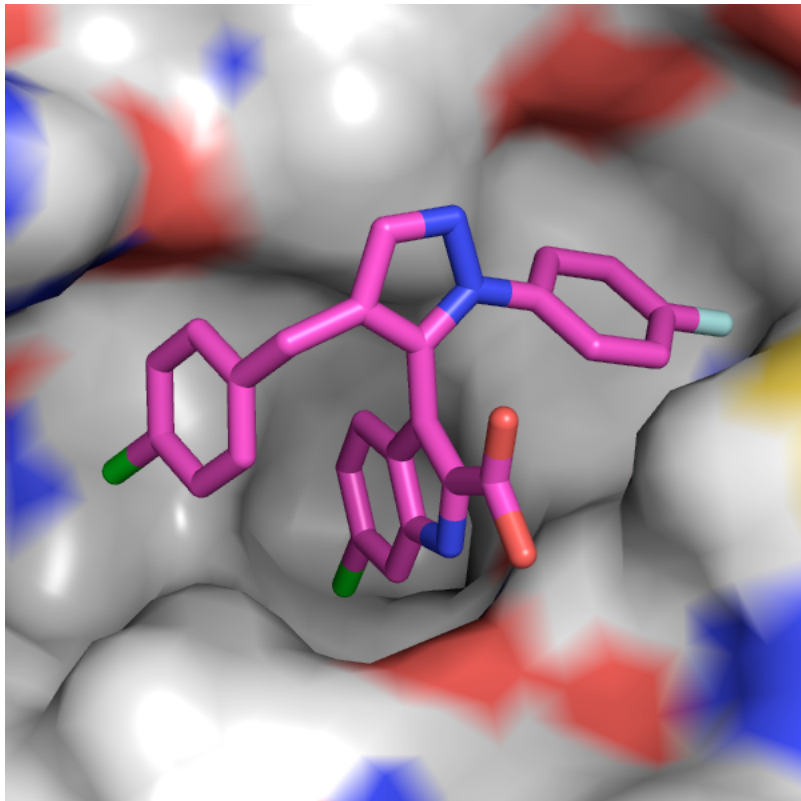
- similarity to known binder
- QSAR
- pharmacophore

## Receptor Based

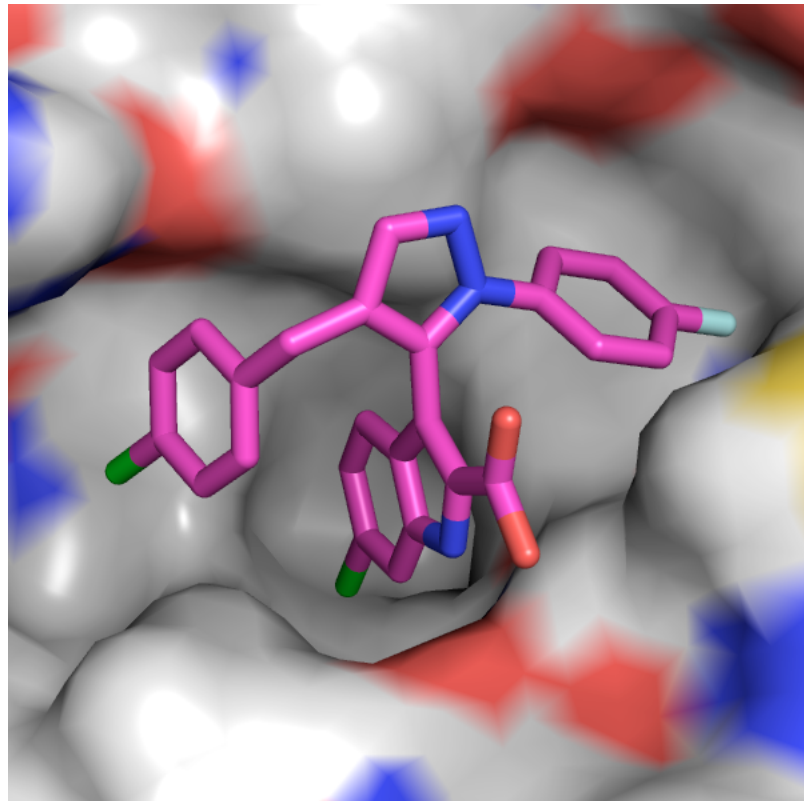
- **dock and score**



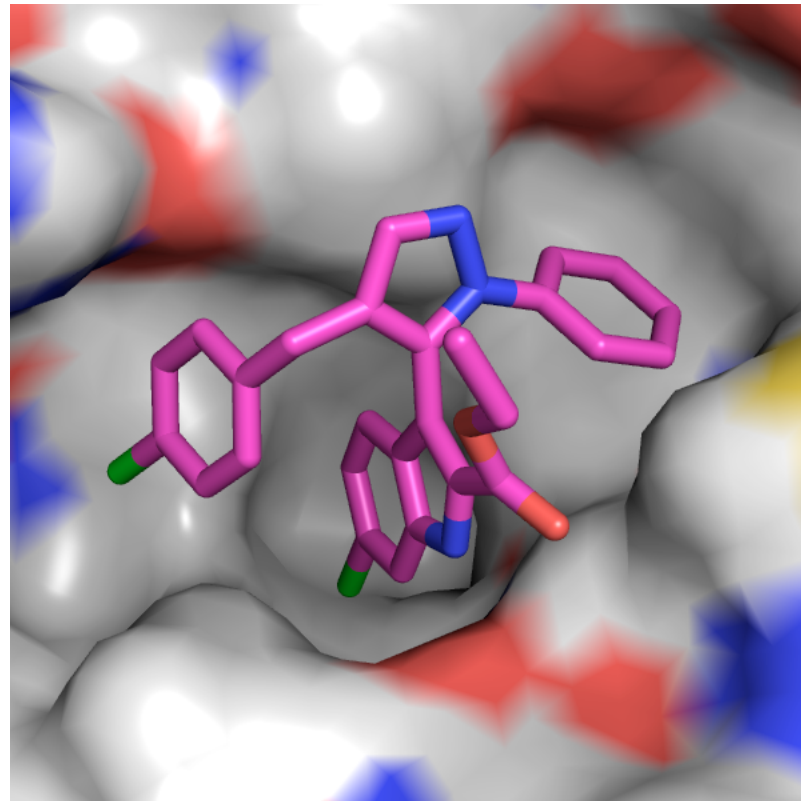
# Pharmacophores Aren't Enough



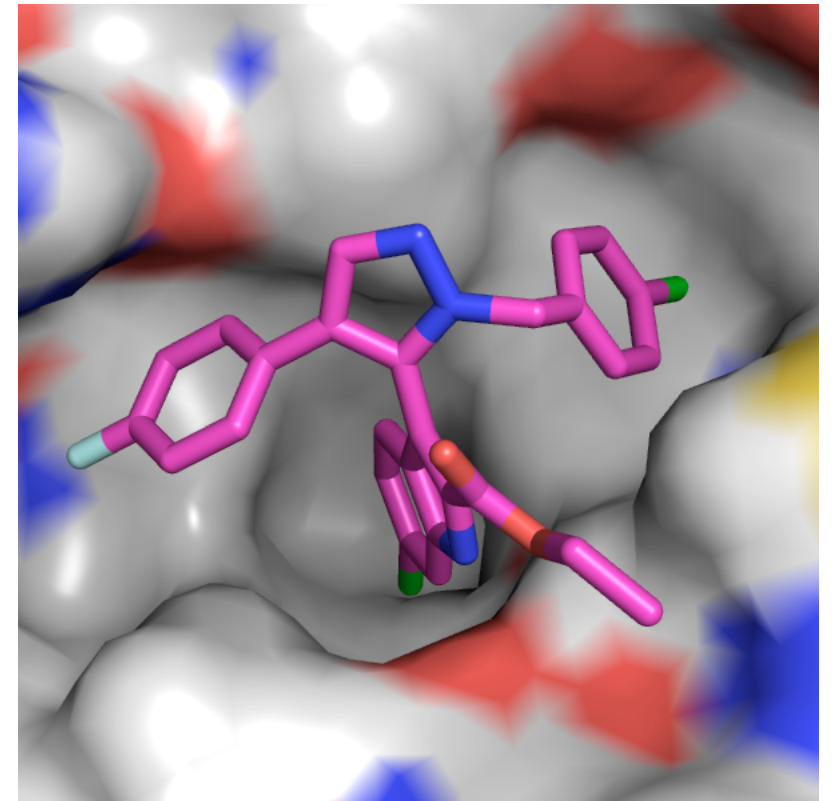
# Pharmacophores Aren't Enough



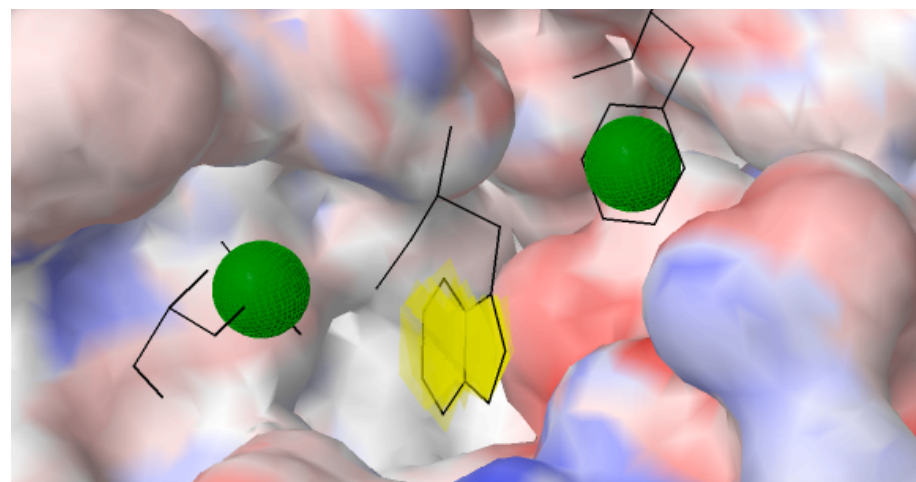
.2 $\mu$ M



50 $\mu$ M



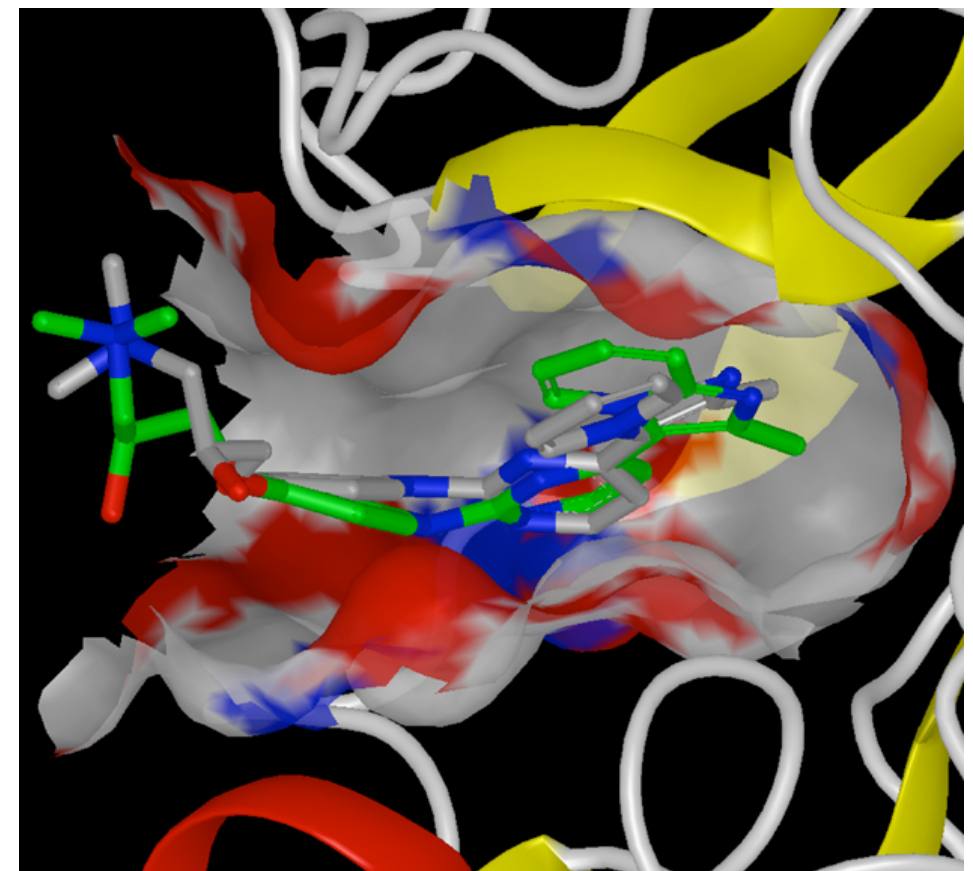
n.i.



# Docking

Determine the **conformation** and **pose** of a ligand at a docking site

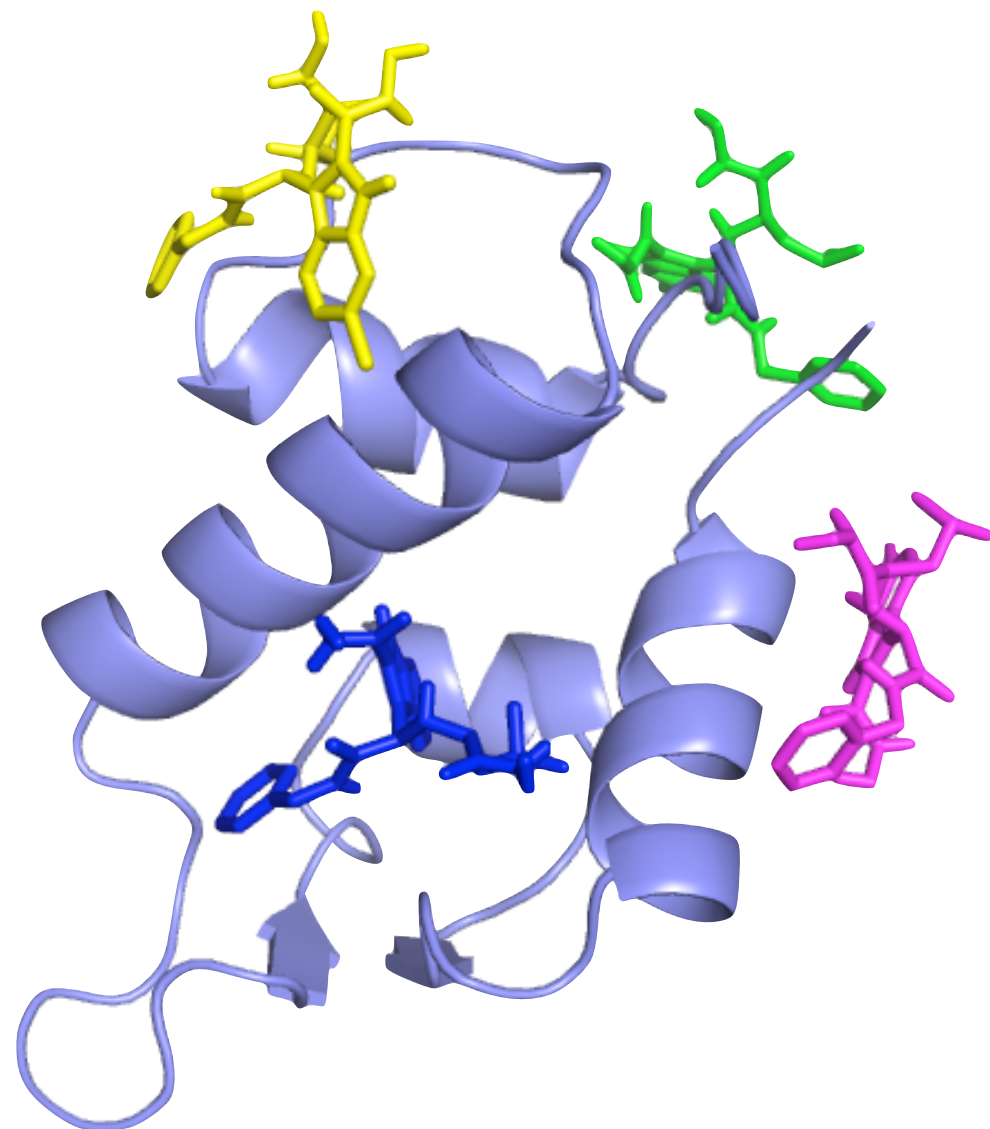
Challenge is to find conformation and pose with the best **score**





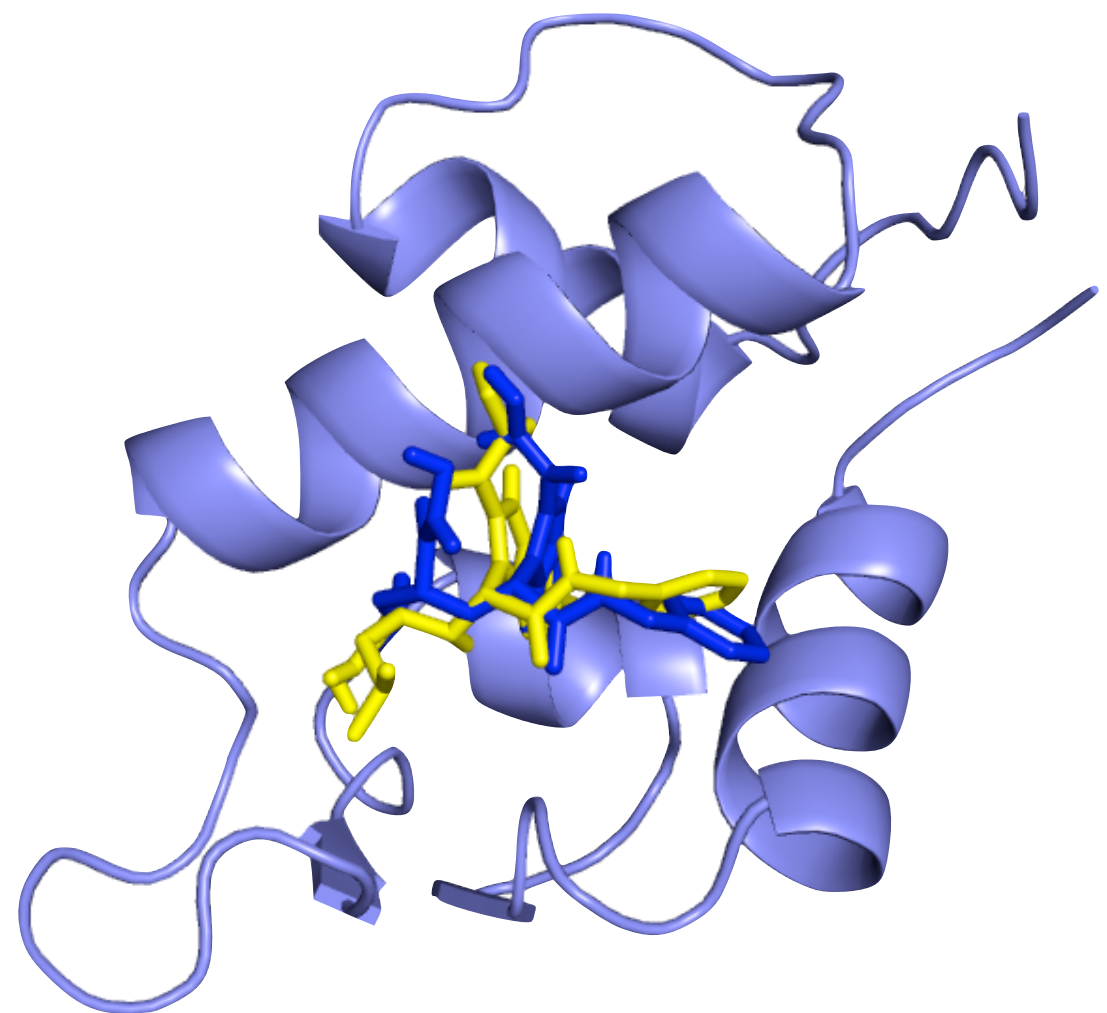
# Two Phase Docking

1. Global Pose Estimation



Stochastic

2. Local Refinement

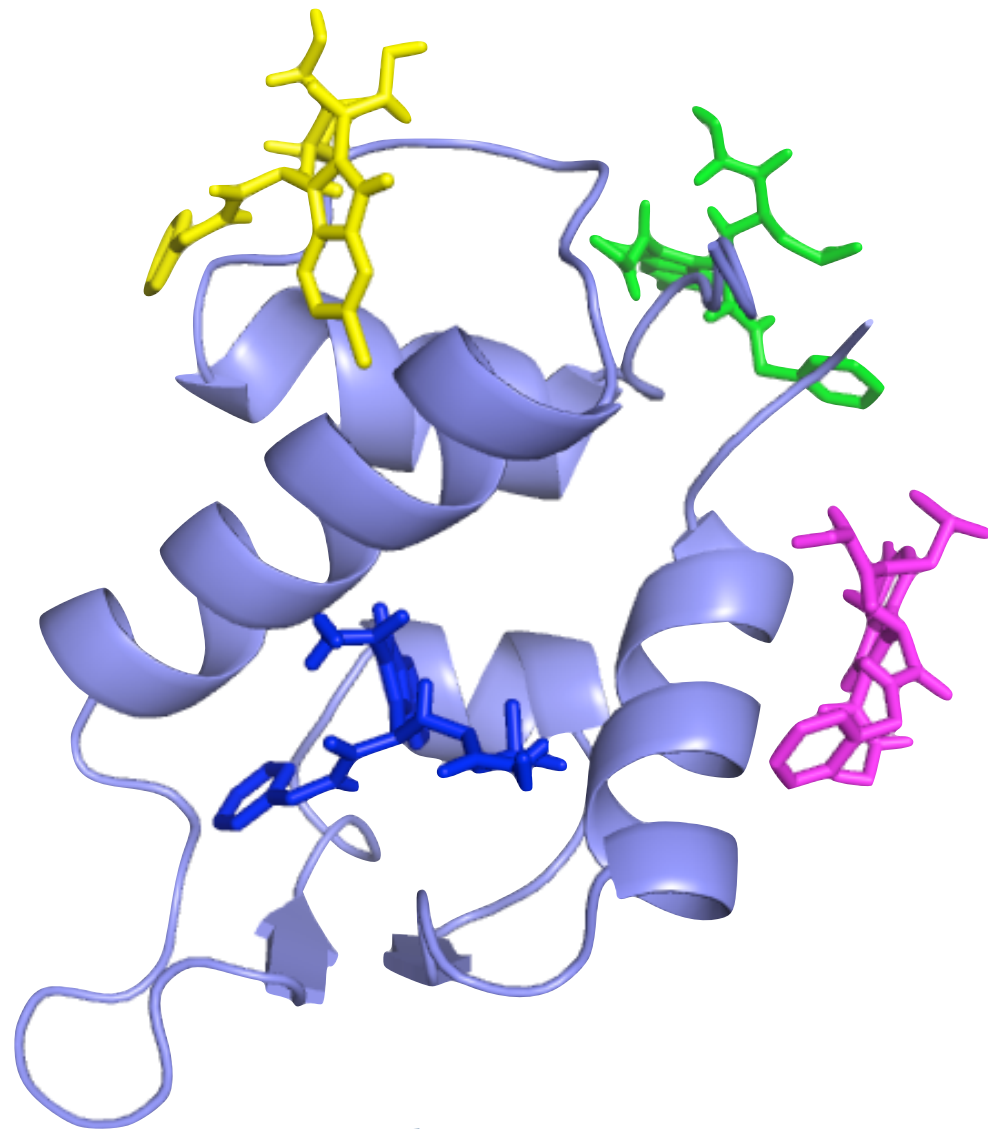


Minimization

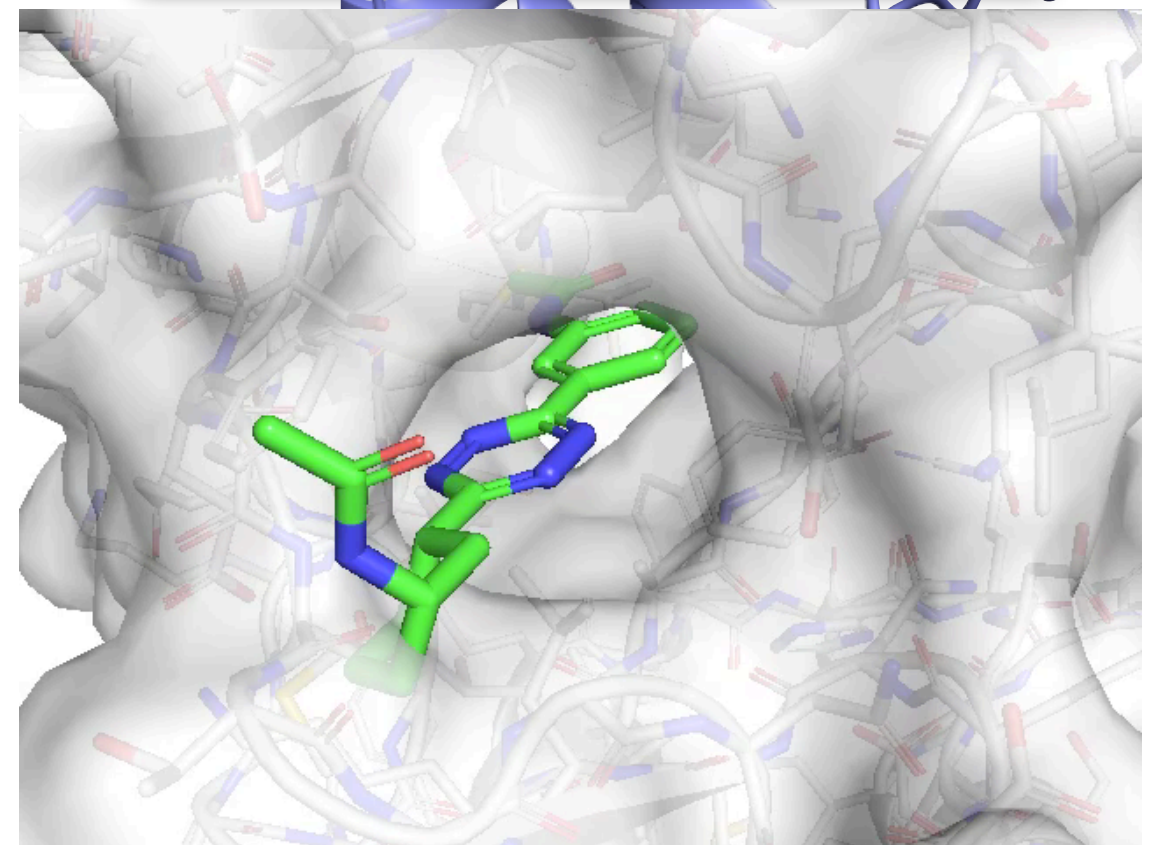
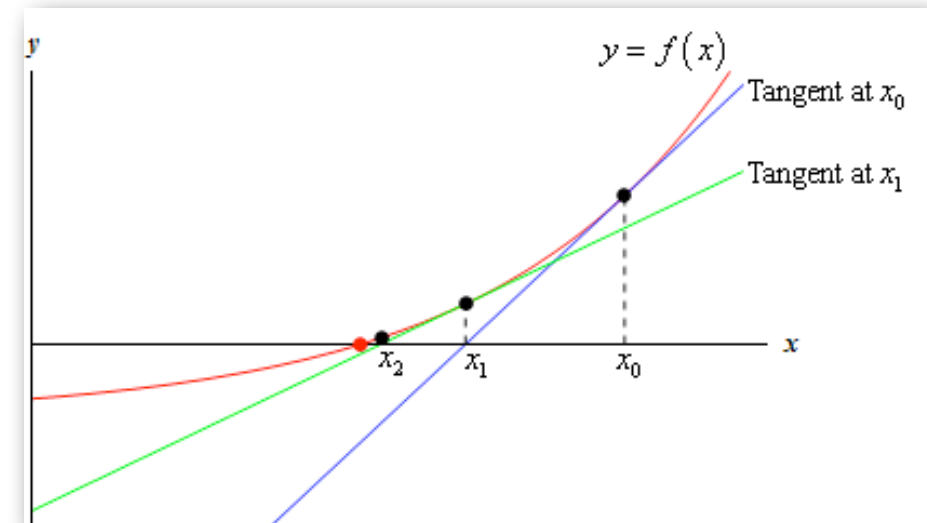


# Two Phase Docking

## 1. Global Pose Estimation



Stochastic



Minimization

# Scoring Goals

## Affinity Prediction

- how well does it bind?

## Inactive/Active Discrimination

- does it bind?

## Pose Prediction

- how does it bind?

# Scoring Goals

## Affinity Prediction

- how well does it bind?

## Inactive/Active Discrimination

- does it bind?

## Pose Prediction

- how does it bind?

# Speed

# Scoring Goals

## Affinity Prediction

- how well does it bind?

## Inactive/Active Discrimination

- does it bind?

## Pose Prediction

- how does it bind?

## Speed

### **Approximations:**

Rigid or semi-rigid receptor  
Implicit water model

# Scoring Types

## Force-field based

inter- and intra- molecular forces  
van der Waals, electrostatic, torsional

## Empirical

parameterized function is fit to binding energy data

## Knowledge based

scoring function based on known structure, not  
physical principles

## Consensus



# Force Field Scoring

|                    | Protein–ligand                                                                                                                                                                                                                                                                                                                                                   | Internal ligand                                                                                                                                                                                                                                                                                                                       |
|--------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>G-Score</b>     | $E_{vdW} + E_{H-bond} =$ $\sum_{prot} \sum_{lig} \left[ \left( \frac{A_{ij}}{d_{ij}^8} - \frac{B_{ij}}{d_{ij}^4} \right) + (E_{da} + E_{ww}) - (E_{dw} + E_{aw}) \right]$                                                                                                                                                                                        | $E_{vdw} + E_{torsion} =$ $\sum_{lig} \left( \frac{C_{ij}}{d_{ij}^{12}} - \frac{D_{ij}}{d_{ij}^6} \right) + \sum_{lig} \frac{1}{2} V \left[ 1 + \frac{n}{ n } \cos( n \omega) \right]$                                                                                                                                                |
| <b>D-Score</b>     | $E_{vdW} + E_{electrostatic} =$ $\sum_{prot} \sum_{lig} \left[ \left( \frac{A_{ij}}{d_{ij}^{12}} + \frac{B_{ij}}{d_{ij}^6} \right) + 332.0 \frac{q_i q_j}{\epsilon (d_{ij}) d_{ij}} \right]$                                                                                                                                                                     |                                                                                                                                                                                                                                                                                                                                       |
| <b>Gold</b>        | $E_{vdW} + E_{electrostatic} =$ $\sum_{prot} \sum_{lig} \left[ \left( \frac{A_{ij}}{d_{ij}^a} + \frac{B_{ij}}{d_{ij}^b} \right) + 332.0 \frac{q_i q_j}{\epsilon (d_{ij}) d_{ij}} \right]$                                                                                                                                                                        | $E_{vdW} + E_{electrostatic} =$ $\sum_{lig} \left[ \left( \frac{A_{ij}}{d_{ij}^a} + \frac{B_{ij}}{d_{ij}^b} \right) + 332.0 \frac{q_i q_j}{\epsilon (d_{ij}) d_{ij}} \right]$ <p>+ optional <math>E_{H-bond}</math></p>                                                                                                               |
| <b>AutoDock</b>    | $E_{vdW} + E_{H-bond} + E_{electrostatic} =$ $\sum_{prot} \sum_{lig} \left[ \left( \frac{A_{ij}}{d_{ij}^{12}} - \frac{B_{ij}}{d_{ij}^6} \right) + E(t) \times \left( \frac{C_{ij}}{d_{ij}^{12}} - \frac{D_{ij}}{d_{ij}^{10}} \right) + \right.$ $\left. 332.0 \frac{q_i q_j}{\epsilon (d_{ij}) d_{ij}} \right]$ <p><math>E(t)</math> = angular weight factor</p> | $E_{vdW} + E_{H-bond} + E_{electrostatic} =$ $\sum_{lig} \left[ \left( \frac{A_{ij}}{d_{ij}^{12}} - \frac{B_{ij}}{d_{ij}^6} \right) + E(t) \left( \frac{C_{ij}}{d_{ij}^{12}} - \frac{D_{ij}}{d_{ij}^{10}} \right) + \right.$ $\left. 332.0 \frac{q_i q_j}{4(d_{ij}) d_{ij}} \right]$ <p><math>E(t)</math> = angular weight factor</p> |
| <b>DOCK (v4.0)</b> | $E_{vdW} + E_{electrostatic} =$ $\sum_{prot} \sum_{lig} \left[ \left( \frac{A_{ij}}{d_{ij}^a} + \frac{B_{ij}}{d_{ij}^b} \right) + 332.0 \frac{q_i q_j}{\epsilon (d_{ij}) d_{ij}} \right]$                                                                                                                                                                        |                                                                                                                                                                                                                                                                                                                                       |

# Dock 4.0

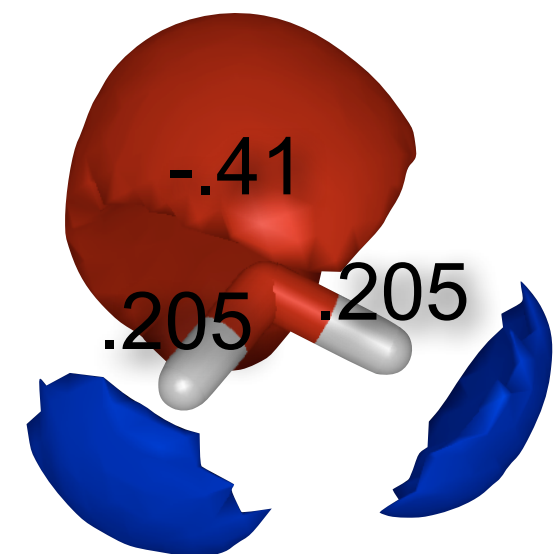
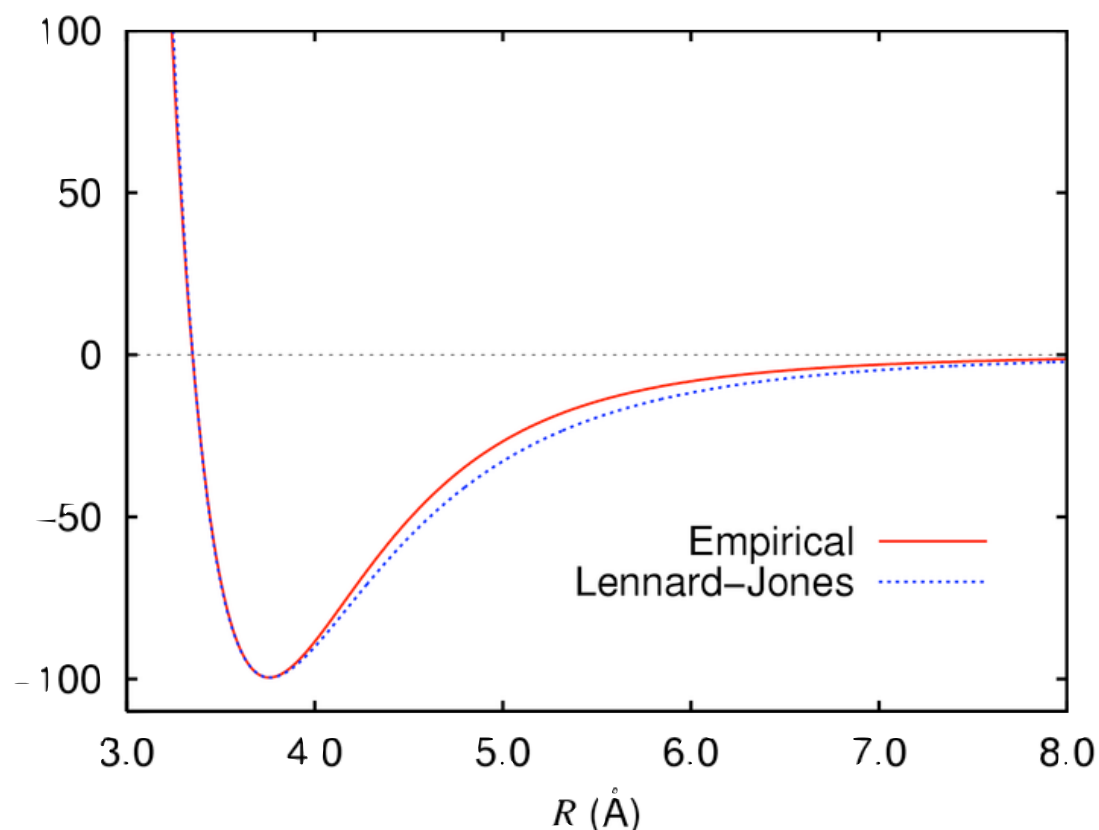
Coulomb's Law  
 q: partial charges  
 D: dielectric constant

$$E = \sum_{i=1}^{lig} \sum_{j=1}^{rec} \left( \frac{A_{ij}}{r_{ij}^a} - \frac{B_{ij}}{r_{ij}^b} + 332 \frac{q_i q_j}{D r_{ij}} \right)$$

van der Waals

a = 12, b = 6

Lennard-Jones potential



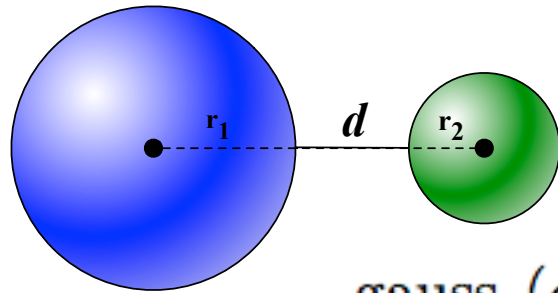
# Empirical Scoring

|                   | Functional form                                                                                                                                                                                                                                                                                                       |
|-------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>LUDI</b>       | $\Delta G_{bind} = \Delta G_{H-bond} \sum_{H-bond} f(\Delta R, \Delta \alpha) + \Delta G_{ionic} \sum_{ionic} f(\Delta R, \Delta \alpha) +$ $\Delta G_{hydrophobic} \sum_{hydrophobic}  A_{hydrophobic}  + \Delta G_{rotor} N_{rotor} + \Delta G_0$ <p><math>A_{hydrophobic}</math> = molecular surface area</p>      |
| <b>F-Score</b>    | $\Delta G_{bind} = \Delta G_{H-bond} \sum_{H-bond} f(\Delta R, \Delta \alpha) + \Delta G_{ionic} \sum_{ionic} f(\Delta R, \Delta \alpha) + \Delta G_{aromatic} \sum_{aromatic} f(\Delta R, \Delta \alpha)$ $+ \Delta G_{contact} \sum_{contact} f(\Delta R, \Delta \alpha) + \Delta G_{rotor} N_{rotor} + \Delta G_0$ |
| <b>Chem-Score</b> | $\Delta G_{bind} = \Delta G_{H-bond} \sum_{H-bond} f(\Delta R, \Delta \alpha) + \Delta G_{metal} \sum_{metal} f(\Delta R, \Delta \alpha) +$ $\Delta G_{lipo} \sum_{lipo} f(\Delta R) + \Delta G_{rotor} \sum_{rotor} f(P_{nl}, P'_{nl}) + \Delta G_0$                                                                 |

# Empirical Scoring

|                   | Functional form                                                                                                                                                                                                                                                                                                                                |
|-------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>LUDI</b>       | $\Delta G_{bind} = \Delta G_{H-bond} \sum_{H-bond} f(\Delta R, \Delta \alpha) + \Delta G_{ionic} \sum_{ionic} f(\Delta R, \Delta \alpha) +$ $\Delta G_{hydrophobic} \sum_{hydrophobic}  A_{hydrophobic}  + \Delta G_{rotor} N_{rotor} + \Delta G_0$ <p><math>A_{hydrophobic}</math> = molecular surface area</p> <p>regression coefficient</p> |
| <b>F-Score</b>    | $\Delta G_{bind} = \Delta G_{H-bond} \sum_{H-bond} f(\Delta R, \Delta \alpha) + \Delta G_{ionic} \sum_{ionic} f(\Delta R, \Delta \alpha) + \Delta G_{aromatic} \sum_{aromatic} f(\Delta R, \Delta \alpha)$ $+ \Delta G_{contact} \sum_{contact} f(\Delta R, \Delta \alpha) + \Delta G_{rotor} N_{rotor} + \Delta G_0$                          |
| <b>Chem-Score</b> | $\Delta G_{bind} = \Delta G_{H-bond} \sum_{H-bond} f(\Delta R, \Delta \alpha) + \Delta G_{metal} \sum_{metal} f(\Delta R, \Delta \alpha) +$ $\Delta G_{lipo} \sum_{lipo} f(\Delta R) + \Delta G_{rotor} \sum_{rotor} f(P_{nl}, P'_{nl}) + \Delta G_0$                                                                                          |

# AutoDock Vina



$$\text{gauss}_1(d) = w_{\text{gauss}_1} e^{-(d/0.5)^2}$$

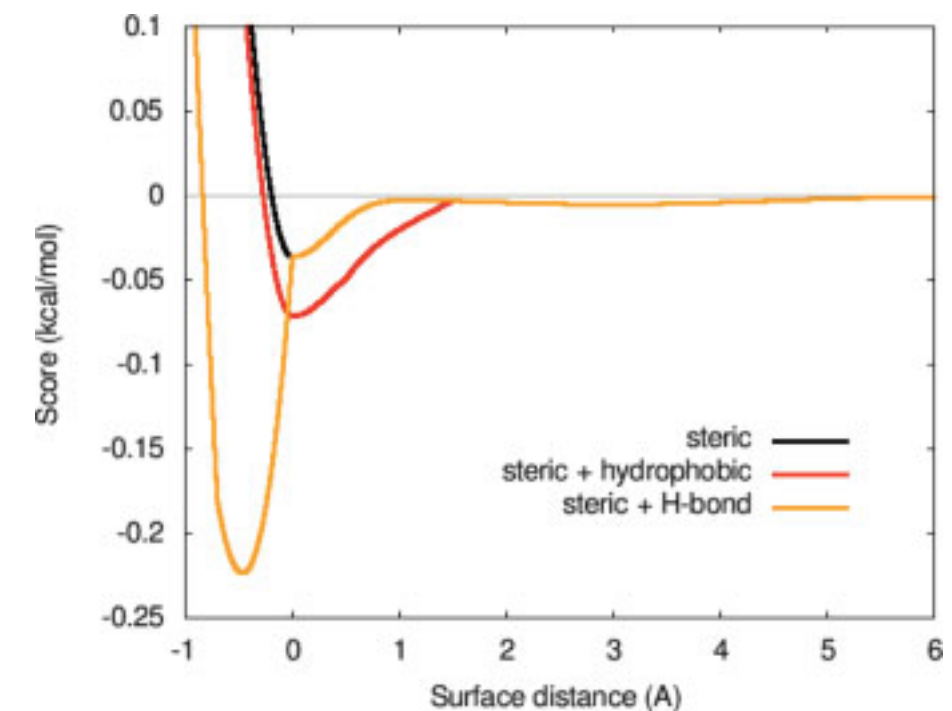
$$\text{gauss}_2(d) = w_{\text{gauss}_2} e^{-((d-3)/2)^2}$$

$$\text{repulsion}(d) = \begin{cases} w_{\text{repulsion}} d^2 & d < 0 \\ 0 & d \geq 0 \end{cases}$$

$$\text{hydrophobic}(d) = \begin{cases} w_{\text{hydrophobic}} & d < 0.5 \\ 0 & d > 1.5 \\ w_{\text{hydrophobic}}(1.5 - d) & \text{otherwise} \end{cases}$$

$$\text{hbond}(d) = \begin{cases} w_{\text{hbond}} & d < -0.7 \\ 0 & d > 0 \\ w_{\text{hbond}}(-\frac{10}{7}d) & \text{otherwise} \end{cases}$$

| Weight   | Term               |
|----------|--------------------|
| -0.0356  | gauss <sub>1</sub> |
| -0.00516 | gauss <sub>2</sub> |
| 0.840    | Repulsion          |
| -0.0351  | Hydrophobic        |
| -0.587   | Hydrogen bonding   |
| 0.0585   | $N_{\text{rot}}$   |



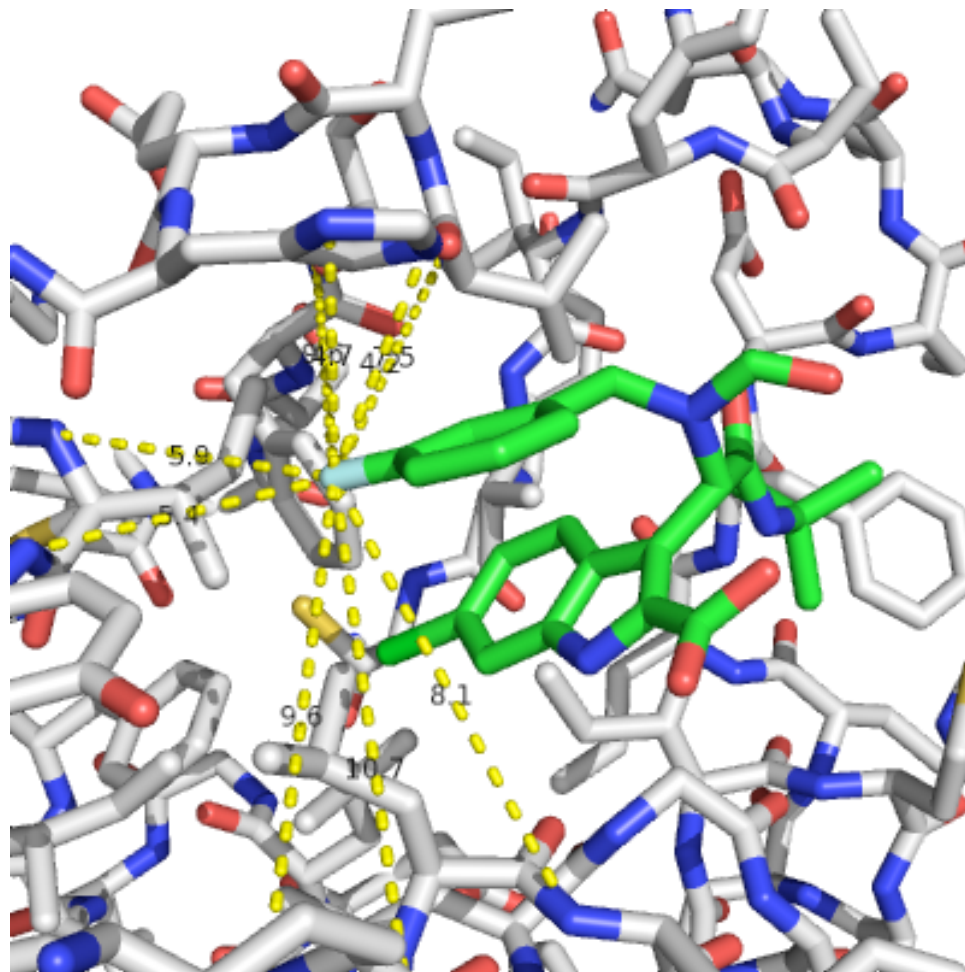


# Knowledge Based

|                         | Functional form                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |
|-------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>PMF</b>              | <p>Parametrized pairwise potential PMF score :</p> $PMF = \sum_{prot} \sum_{lig} A_{ij}(d_{ij}) \quad A_{ij}(d_{ij}) = -k_B T \ln \left[ f_{Vol\_corr}^j(r) \frac{\rho_{seg}^{ij}(r)}{\rho_{bulk}^{ij}} \right]$ <p>where <math>k_B</math> is the Boltzmann constant, <math>f_{Vol\_corr}^j(r)</math> is a ligand volume correction factor</p> <p>and <math>\frac{\rho_{seg}^{ij}(r)}{\rho_{bulk}^{ij}}</math> indicates a radial distribution function for a protein atom <math>i</math> and a ligand atom <math>j</math>.</p> |
| <b>DrugScore (v1.2)</b> | $\Delta W = \gamma \sum_{prot} \sum_{lig} \Delta W_{ij}(r) + (1 - \gamma) \times \left[ \sum_{lig} \Delta W_i(SAS, SAS_0) + \sum_{prot} \Delta W_j(SAS, SAS_0) \right]$ <p><math>SAS</math> = Solvent accessible surface area terms, <math>W_{ij}</math> = distance dependent pairwise potential</p>                                                                                                                                                                                                                            |
| <b>SMoG</b>             | $G = \sum_{ij} g_{ij} \Delta_{ij}; \quad \Delta_{ij} = \begin{cases} 0 & (i, j \text{ more than } 5 \text{ \AA}) \\ 1 & (i, j \text{ within } 5 \text{ \AA}) \end{cases}; \quad g_{ij} = -kT \log \left[ \frac{p_{ij}}{\bar{p}} \right];$ <p><math>p_{ij}</math> and <math>\bar{p}</math> are interatomic and averaged interatomic interactions</p>                                                                                                                                                                             |

# RF-Score

Pairwise Distance Counts (<12Å)



Protein

Ligand

|    | C | N | O | S |
|----|---|---|---|---|
| C  |   |   |   |   |
| N  |   |   |   |   |
| O  |   |   |   |   |
| S  |   |   |   |   |
| P  |   |   |   |   |
| F  |   | 9 |   |   |
| Cl |   |   |   |   |
| Br |   |   |   |   |
| I  |   |   |   |   |

Random Forest

**BIOINFORMATICS ORIGINAL PAPER**

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doi:10.1093/bioinformatics/btq112

Structural bioinformatics

Advance Access publication March 17, 2010

**A machine learning approach to predicting protein–ligand binding affinity with applications to molecular docking**

Pedro J. Ballester<sup>1,\*†</sup> and John B. O. Mitchell<sup>2,\*</sup>

<sup>1</sup>Unilever Centre for Molecular Science Informatics, Department of Chemistry, University of Cambridge, Lensfield Road, Cambridge CB2 1EW and <sup>2</sup>Centre for Biomolecular Sciences, University of St Andrews, North Haugh, St Andrews KY16 9ST, UK

Associate Editor: Burkhard Rost

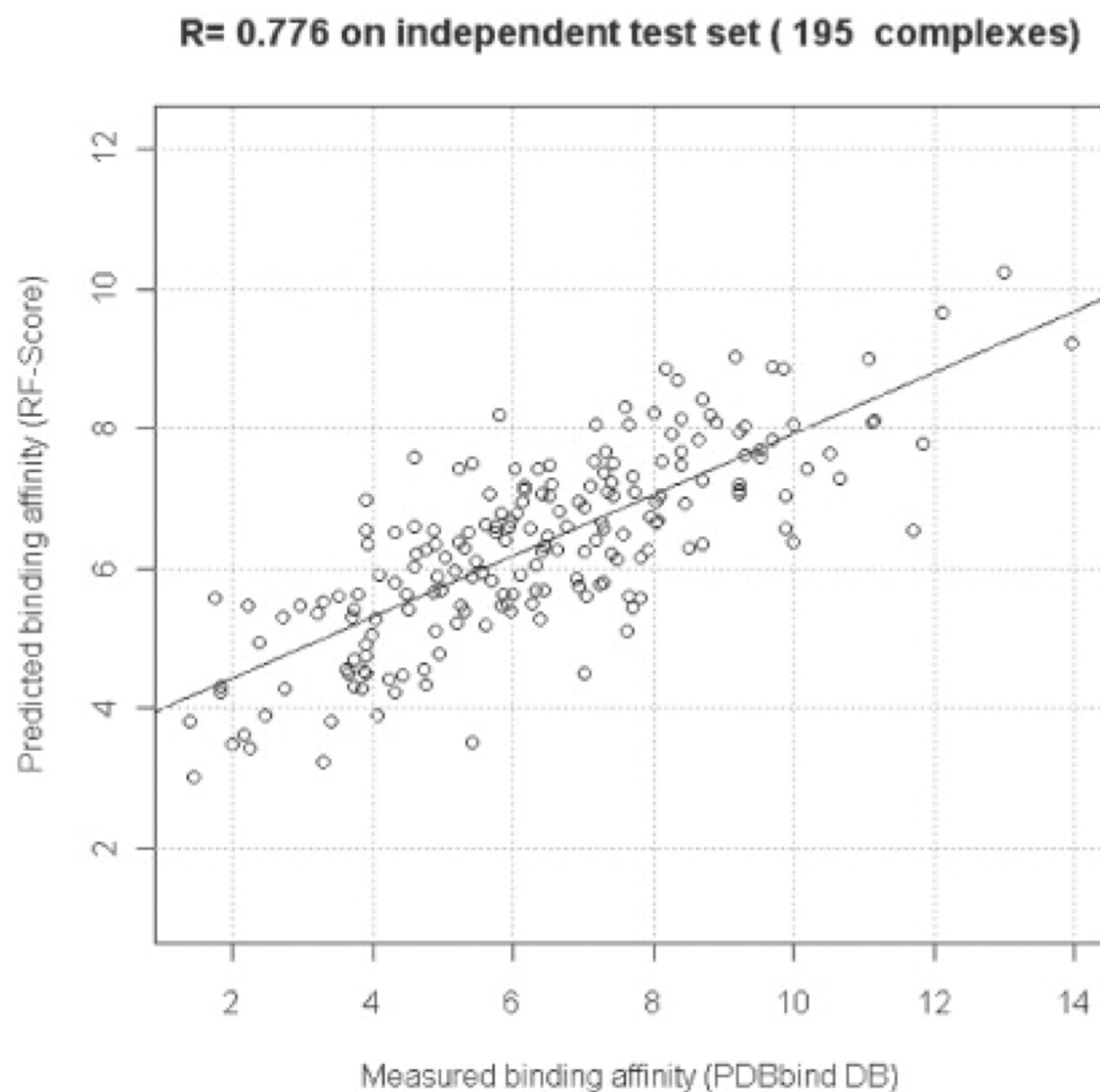
# RF-Score Output



**RMSE = 1.58**

| Scoring function         | R            | Rs           | RMSE        |
|--------------------------|--------------|--------------|-------------|
| <b>RF-Score</b>          | <b>0.776</b> | <b>0.762</b> | <b>1.58</b> |
| X-Score::HMScore         | 0.644        | 0.705        | 1.83        |
| DrugScore <sup>CSD</sup> | 0.569        | 0.627        | 1.96        |
| SYBYL::ChemScore         | 0.555        | 0.585        | 1.98        |
| DS::PLP1                 | 0.545        | 0.588        | 2           |
| GOLD::ASP                | 0.534        | 0.577        | 2.02        |
| SYBYL::G-Score           | 0.492        | 0.536        | 2.08        |
| DS::LUDI3                | 0.487        | 0.478        | 2.09        |
| DS::LigScore2            | 0.464        | 0.507        | 2.12        |
| GlideScore-XP            | 0.457        | 0.435        | 2.14        |
| DS::PMF                  | 0.445        | 0.448        | 2.14        |
| GOLD::ChemScore          | 0.441        | 0.452        | 2.15        |
| SYBYL::D-Score           | 0.392        | 0.447        | 2.19        |
| DS::Jain                 | 0.316        | 0.346        | 2.24        |
| GOLD::GoldScore          | 0.295        | 0.322        | 2.29        |
| SYBYL::PMF-Score         | 0.268        | 0.273        | 2.29        |
| SYBYL::F-Score           | 0.216        | 0.243        | 2.35        |

# RF-Score Output

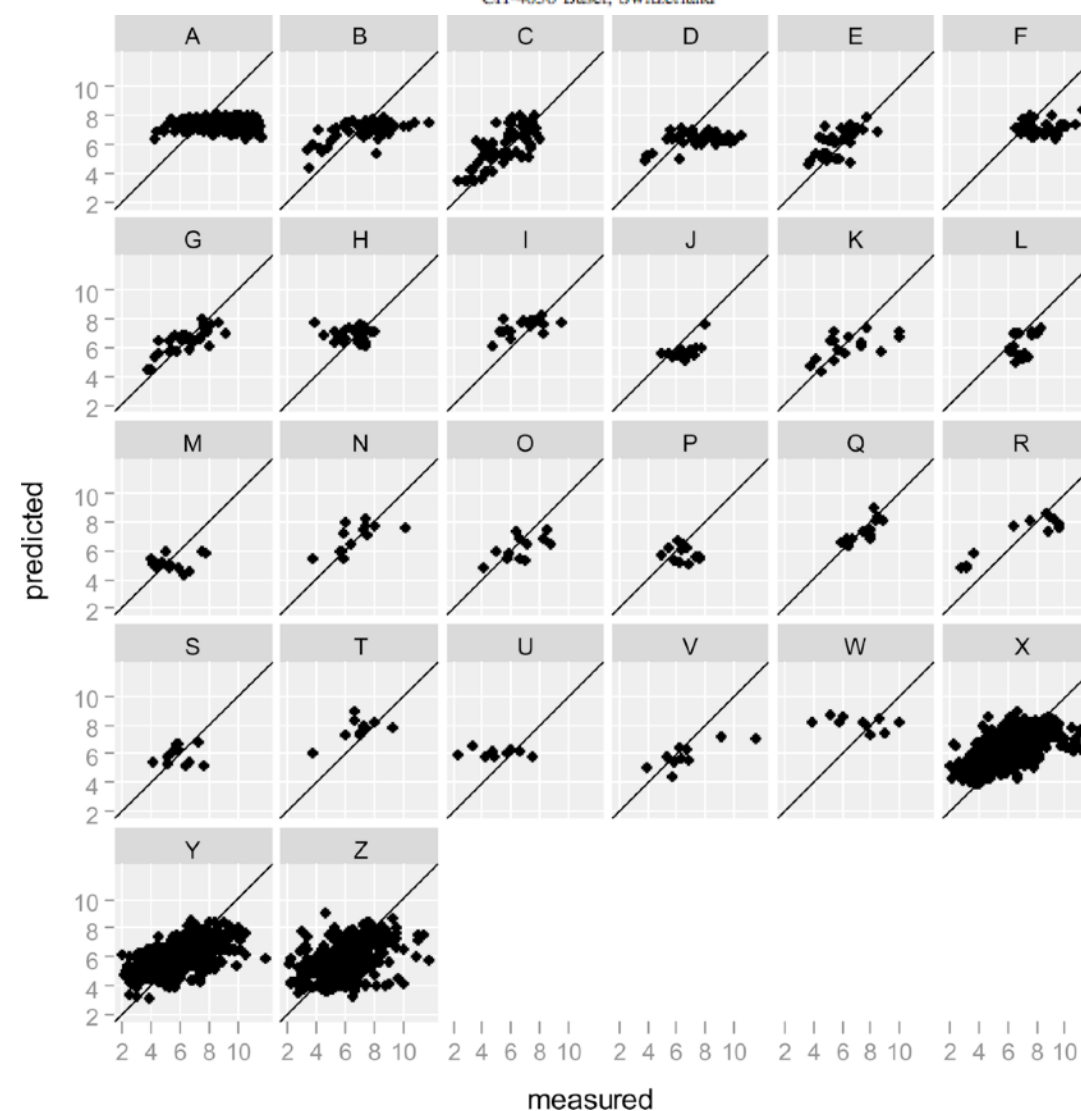


**RMSE = 1.58**

## Leave-Cluster-Out Cross-Validation Is Appropriate for Scoring Functions Derived from Diverse Protein Data Sets

Christian Kramer\* and Peter Gedeck

Novartis Institutes for BioMedical Research, Novartis Pharma AG, Forum 1, Novartis Campus, CH-4056 Basel, Switzerland

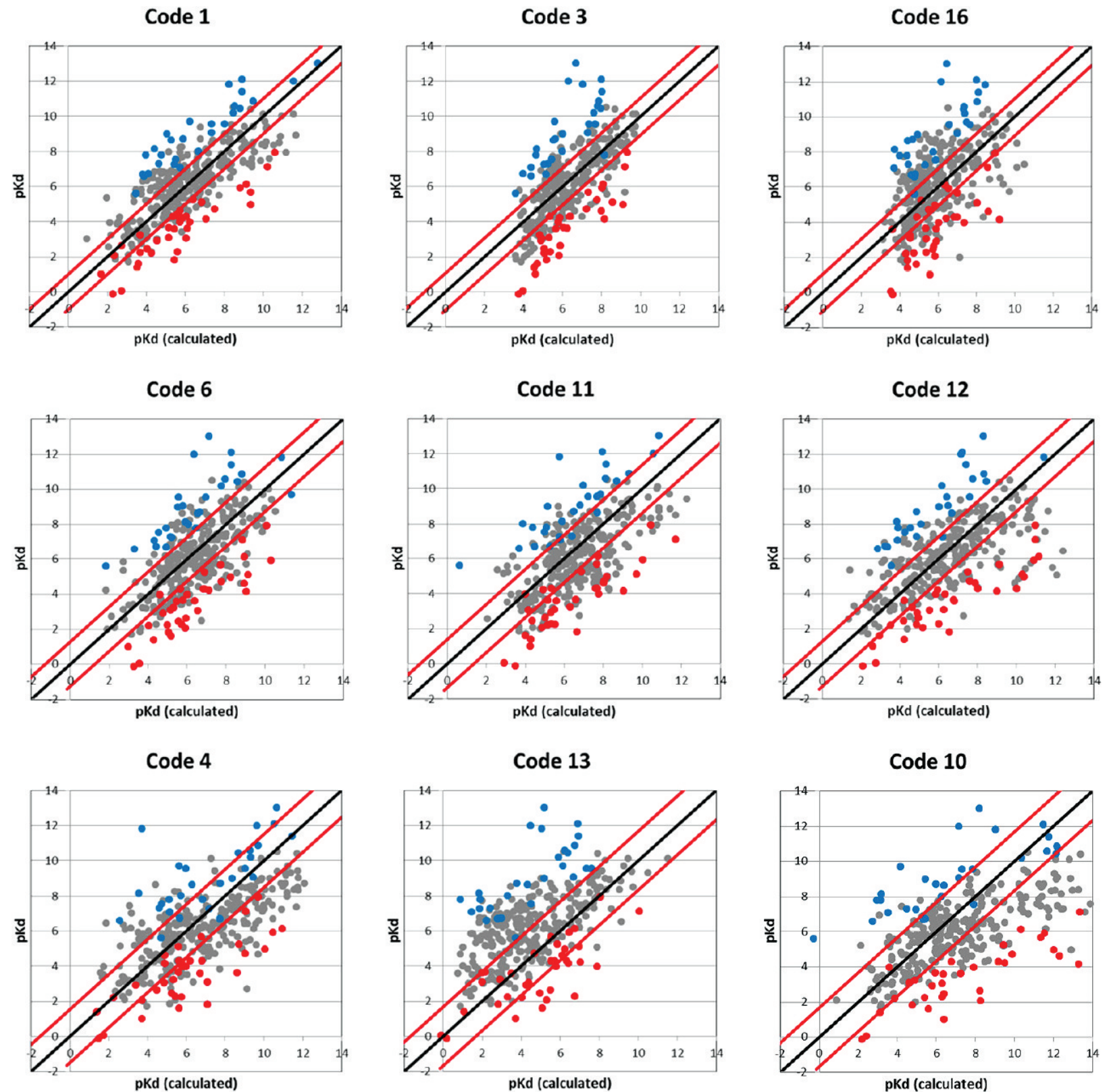


**R = 0.46; RMSE = 1.6**



# Scoring

Ideally, score would equal affinity – but this is an unsolved problem.

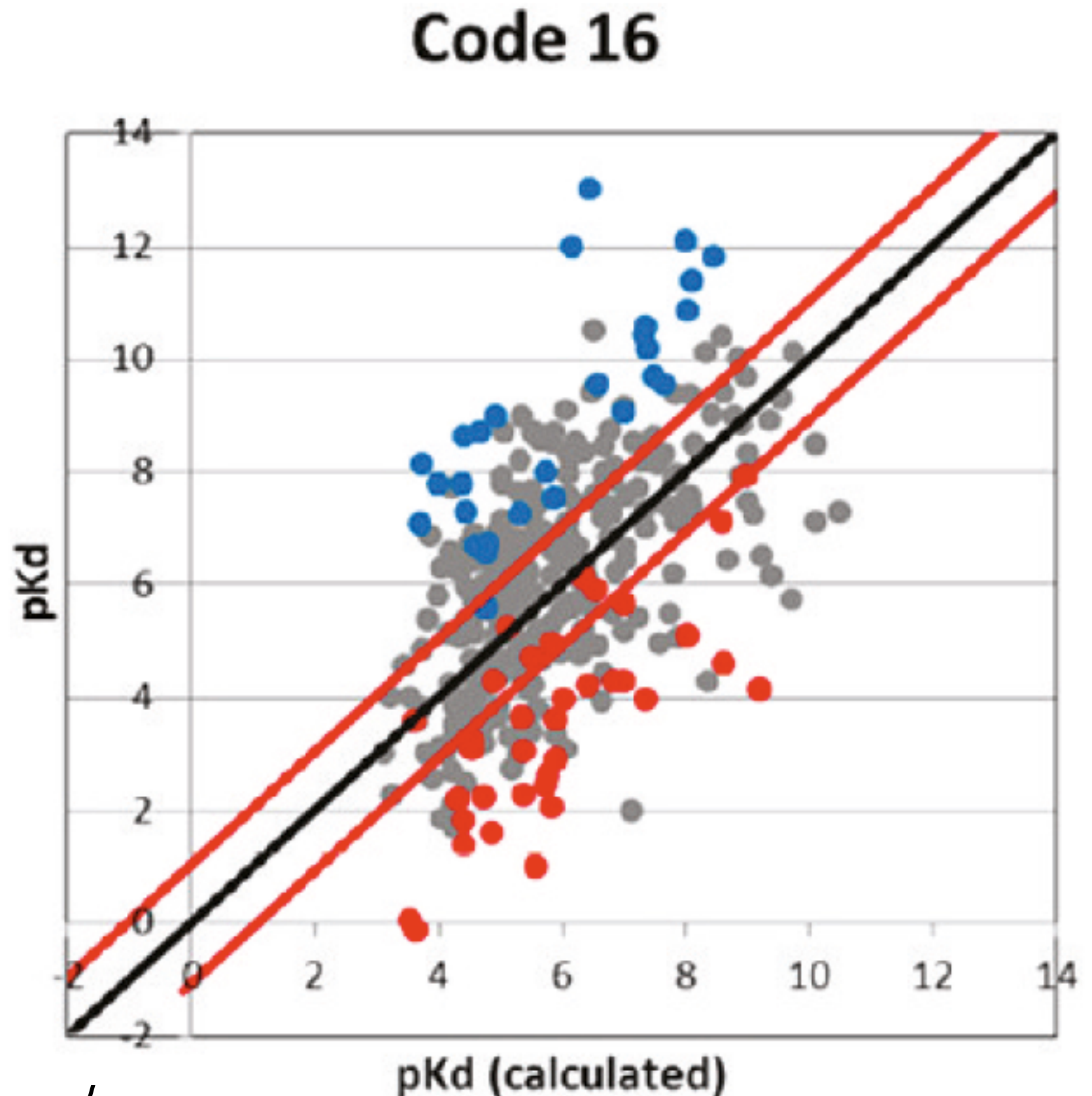




# Scoring

Ideally, score would equal affinity – but this is an unsolved problem.

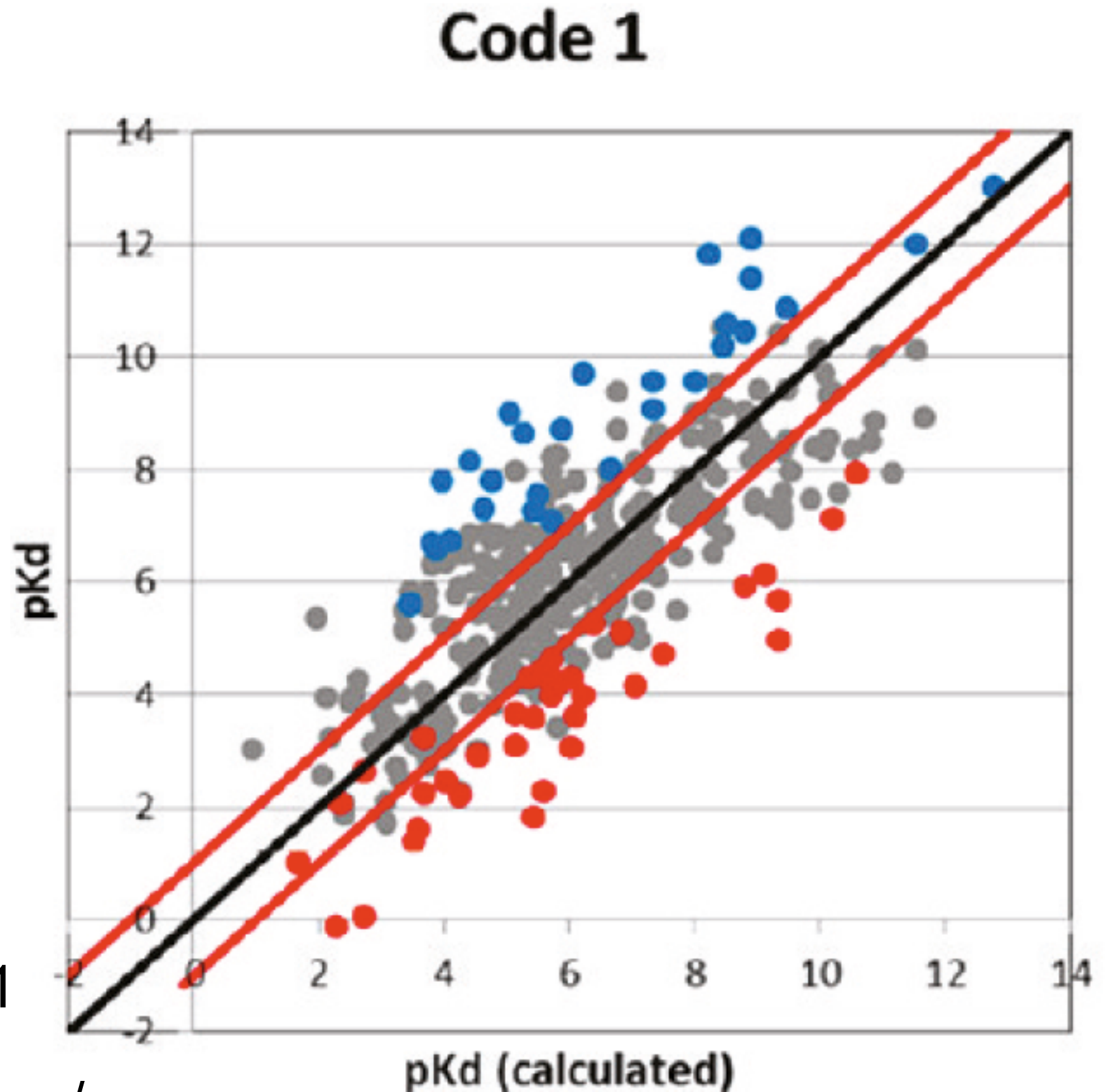
$R^2 = 0.28$   
RMSE = 1.9



# Scoring

Ideally, score would equal affinity – but this is an unsolved problem.

$R^2 = 0.58$   
RMSE = 1.51



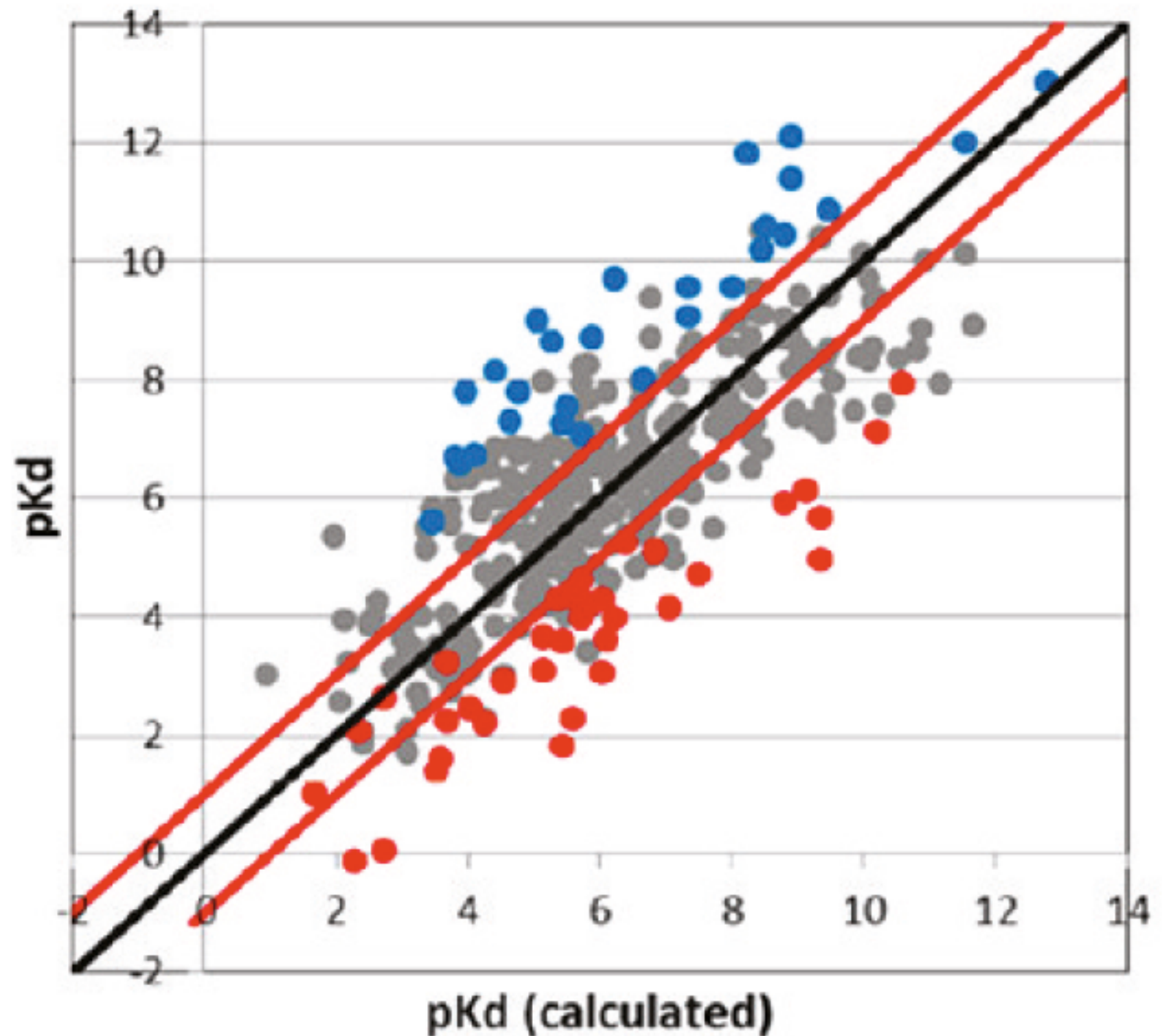
# Scoring

Ideally, score would equal affinity – but this is an unsolved problem.

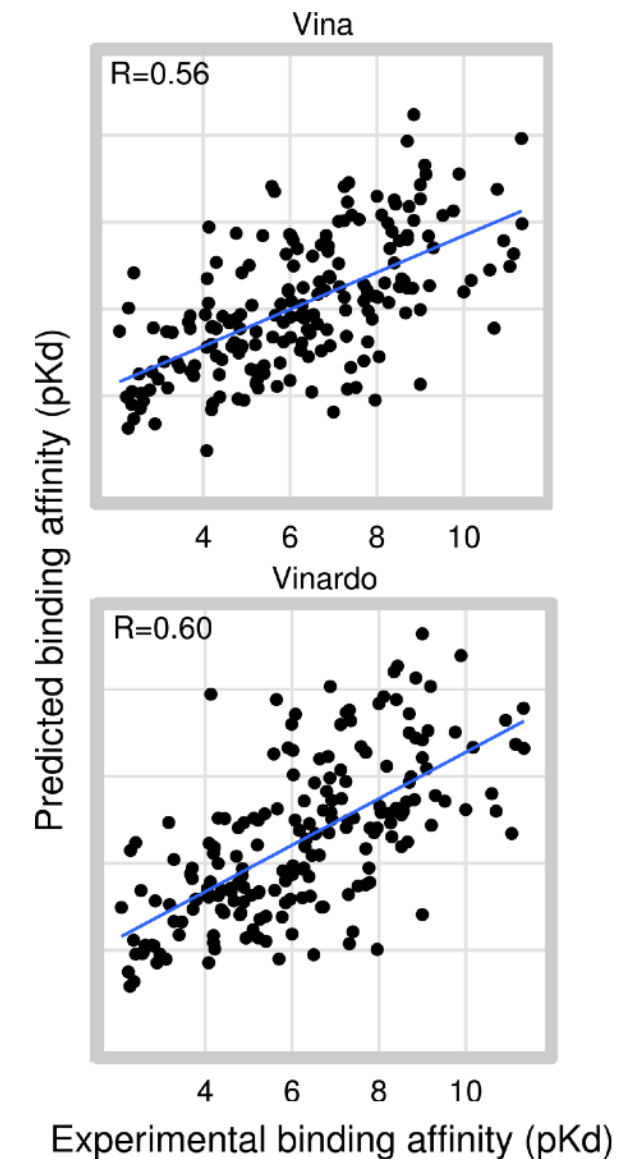
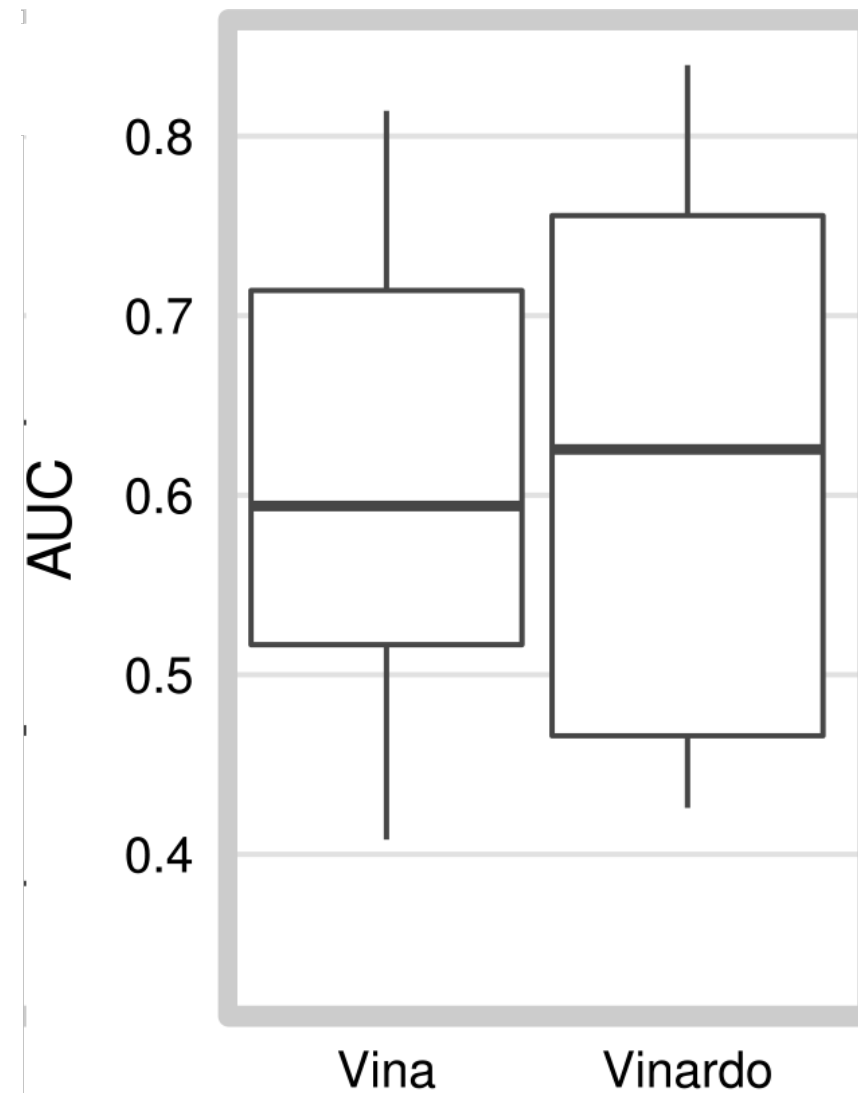
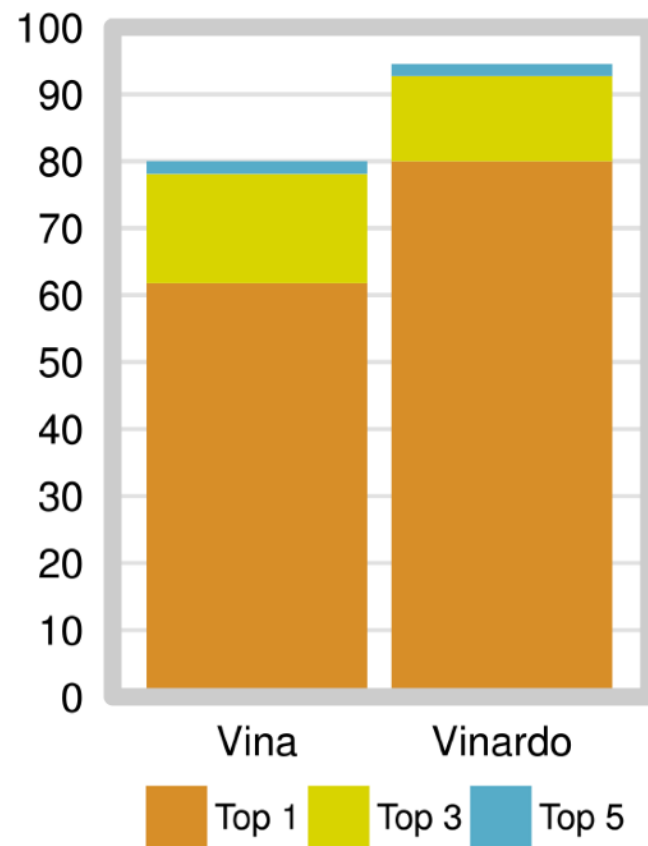
$$R^2 = 0.58$$
$$\text{RMSE} = 1.51$$

<http://www.csardock.org/>

## Code 1



# Scoring State of the Art



Pose Prediction

Binding Discrimination

Affinity Prediction



# Can we do better?

Accurate pose prediction, binding discrimination, **and** affinity prediction without sacrificing performance?





# Can we do better?

Accurate pose prediction, binding discrimination, **and** affinity prediction without sacrificing performance?

**Key Idea:** Leverage “big data”

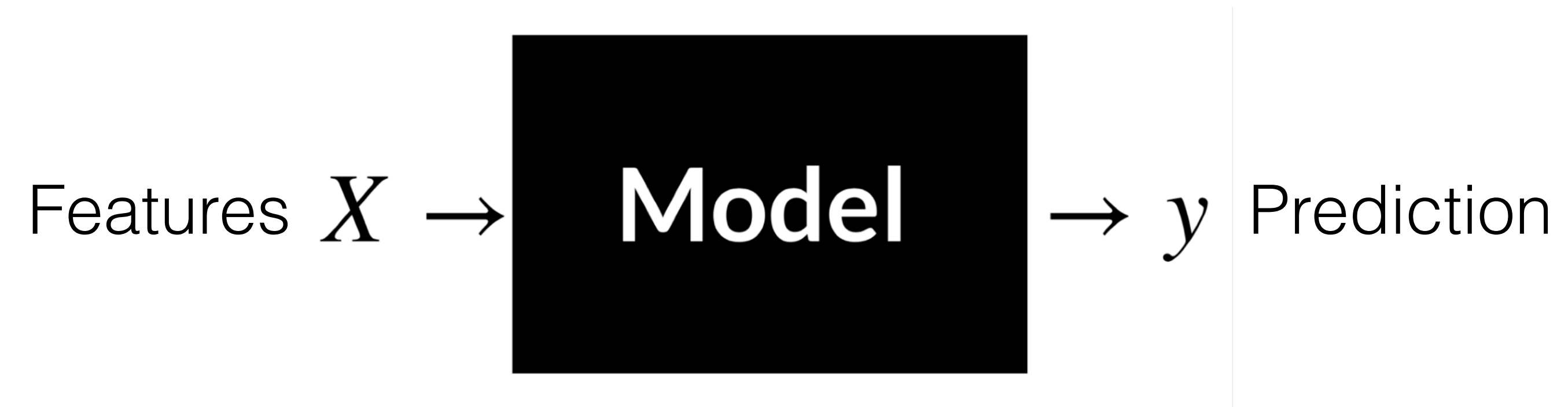
231,655,275 bioactivities in PubCher

125,526 structures in the PDB

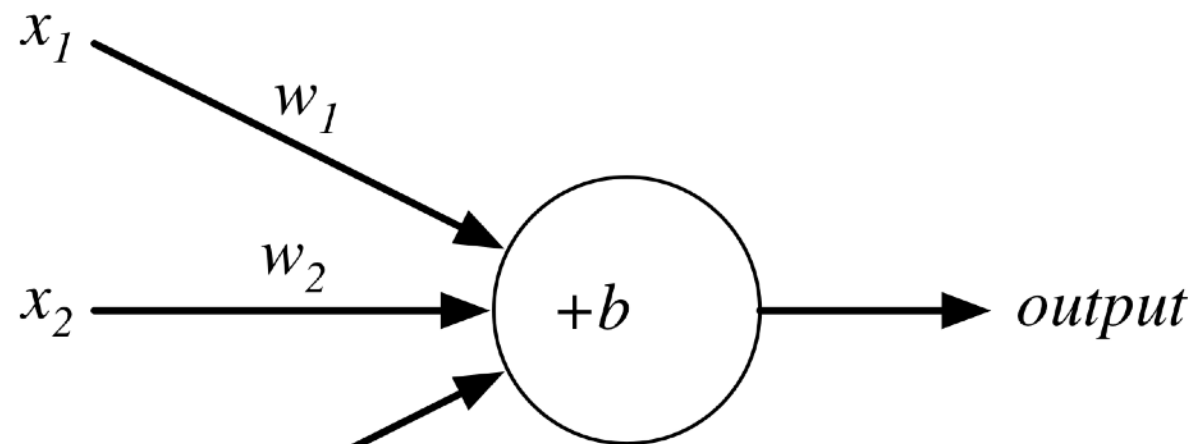
16,179 annotated complexes in PDBbind



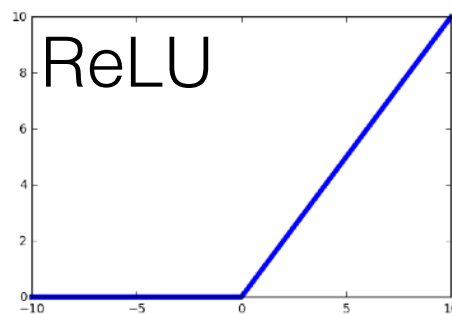
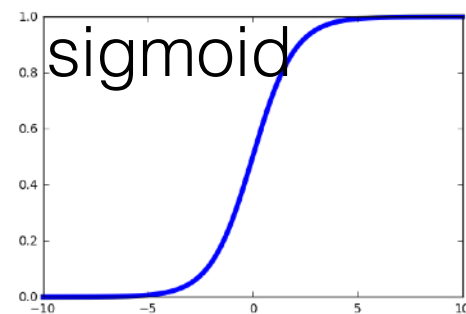
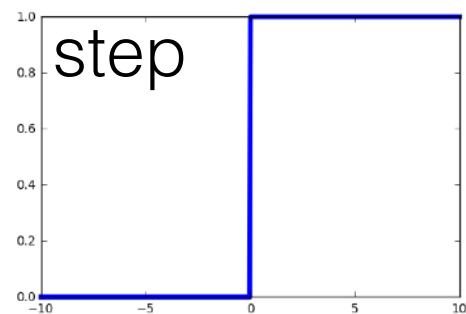
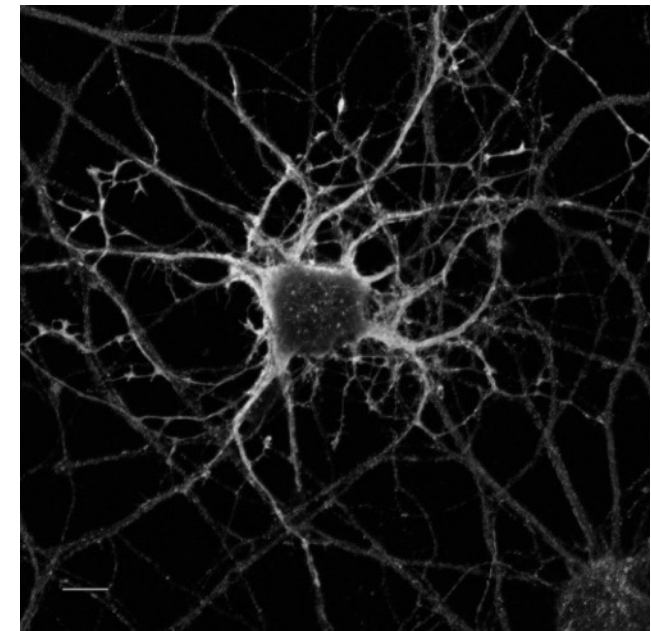
# Machine Learning



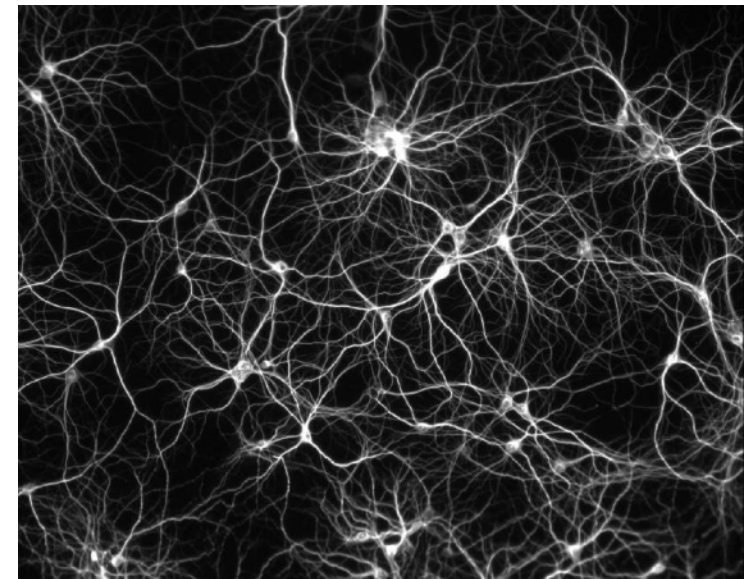
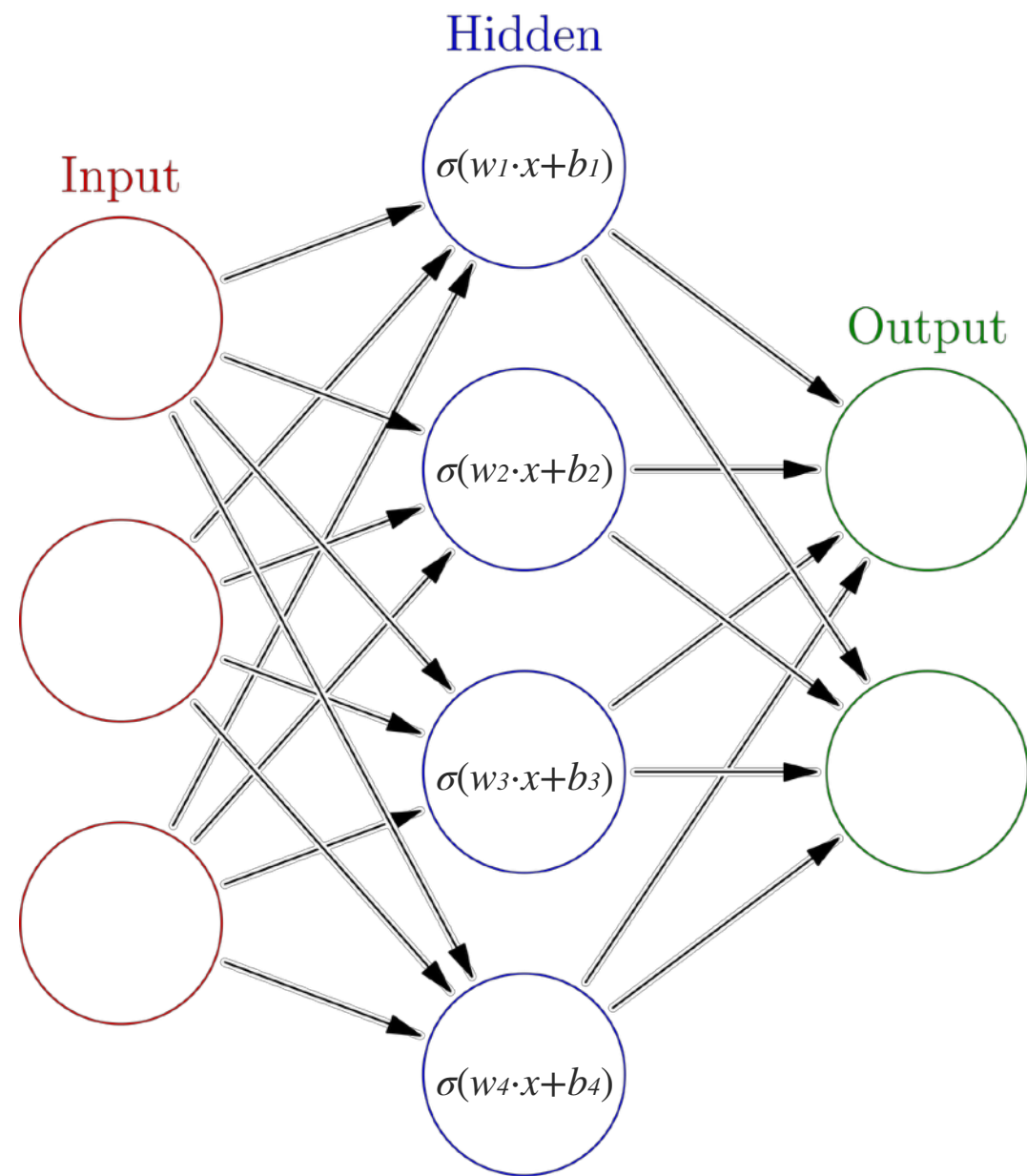
# Neural Networks



$$output = \sigma \left( \sum_i w_i x_i + b \right)$$



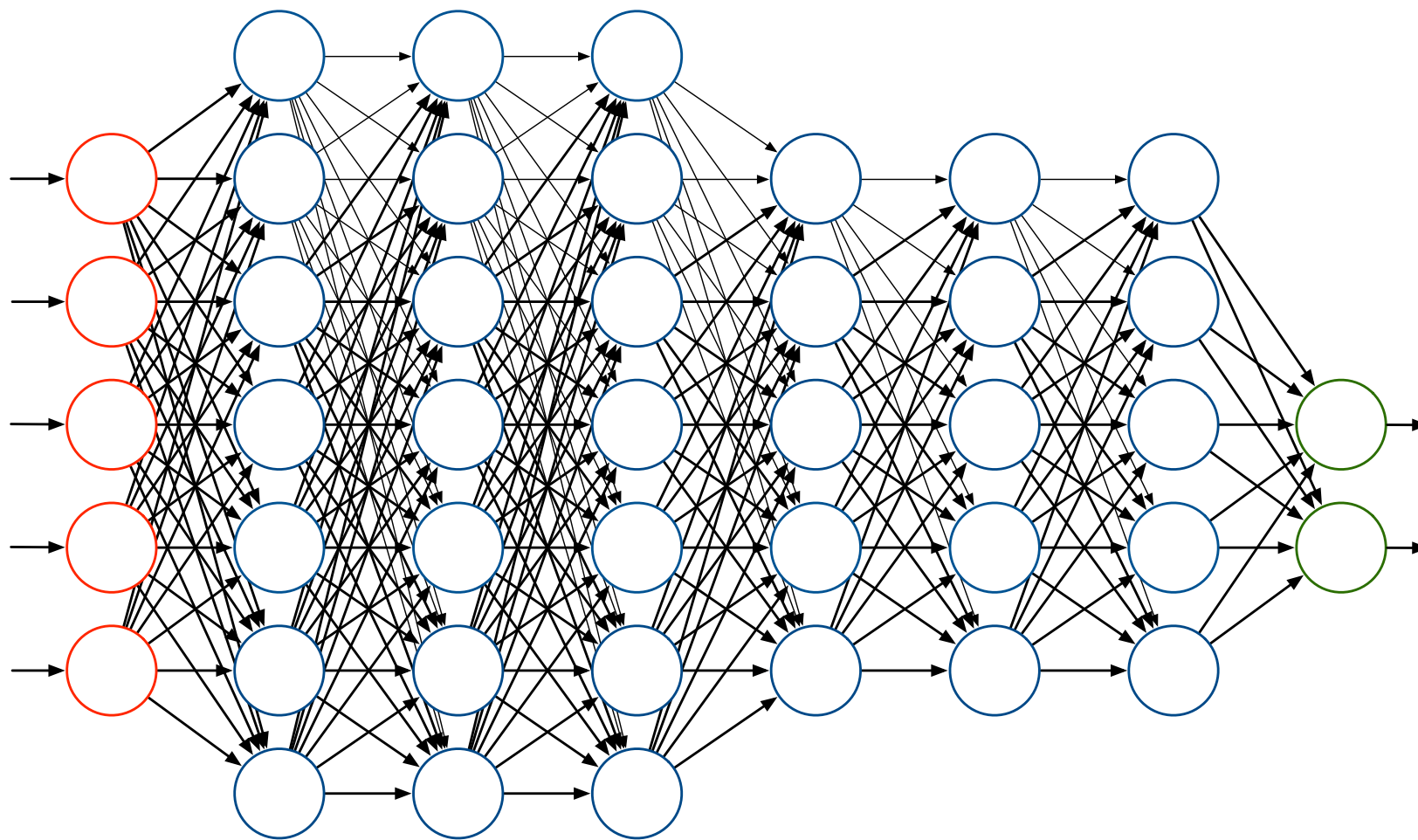
# Neural Networks



The **universal approximation theorem** states that, under reasonable assumptions, a feedforward **neural network** with a finite number of nodes **can approximate any continuous** function to within a given error over a bounded input domain.

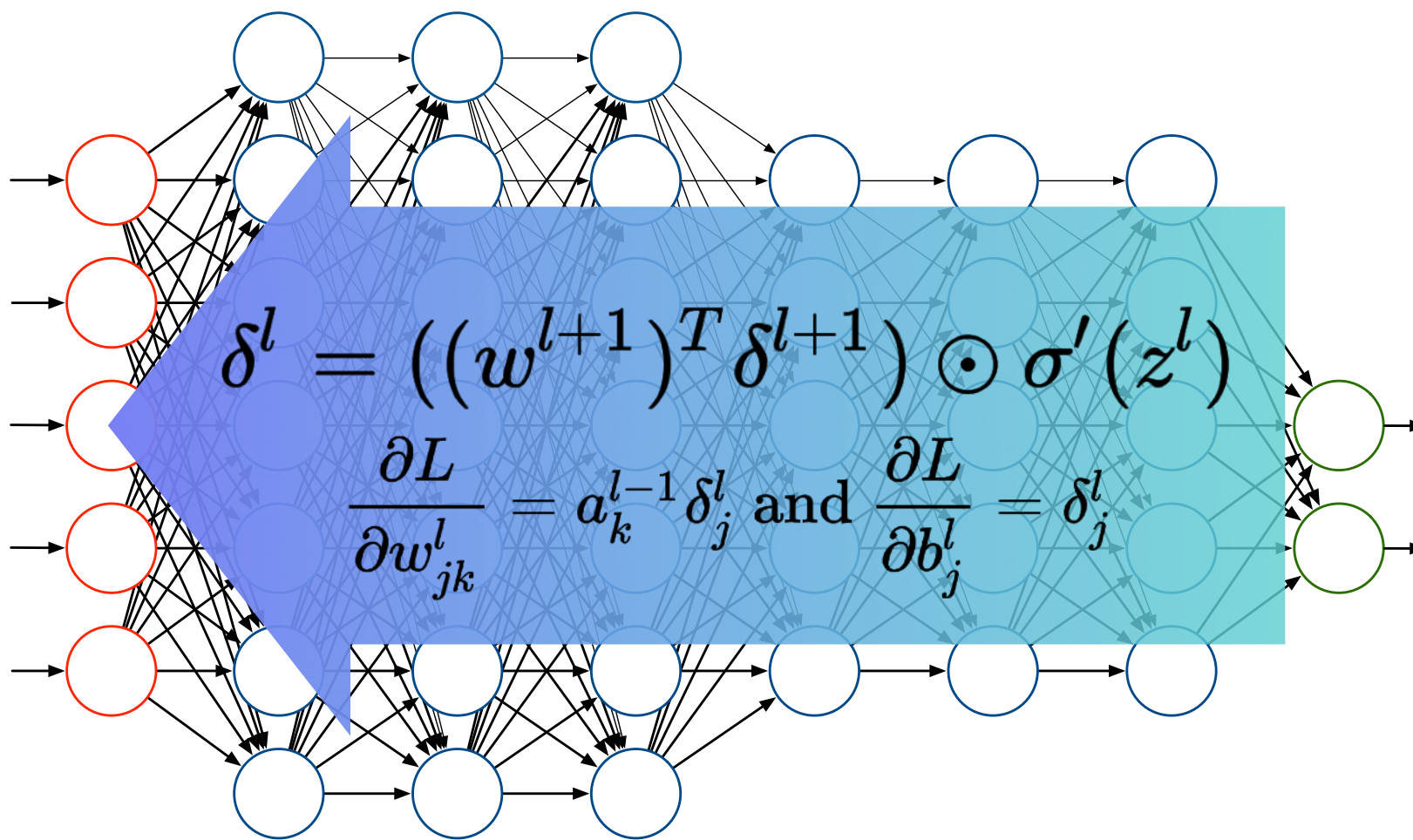


# Deep Learning

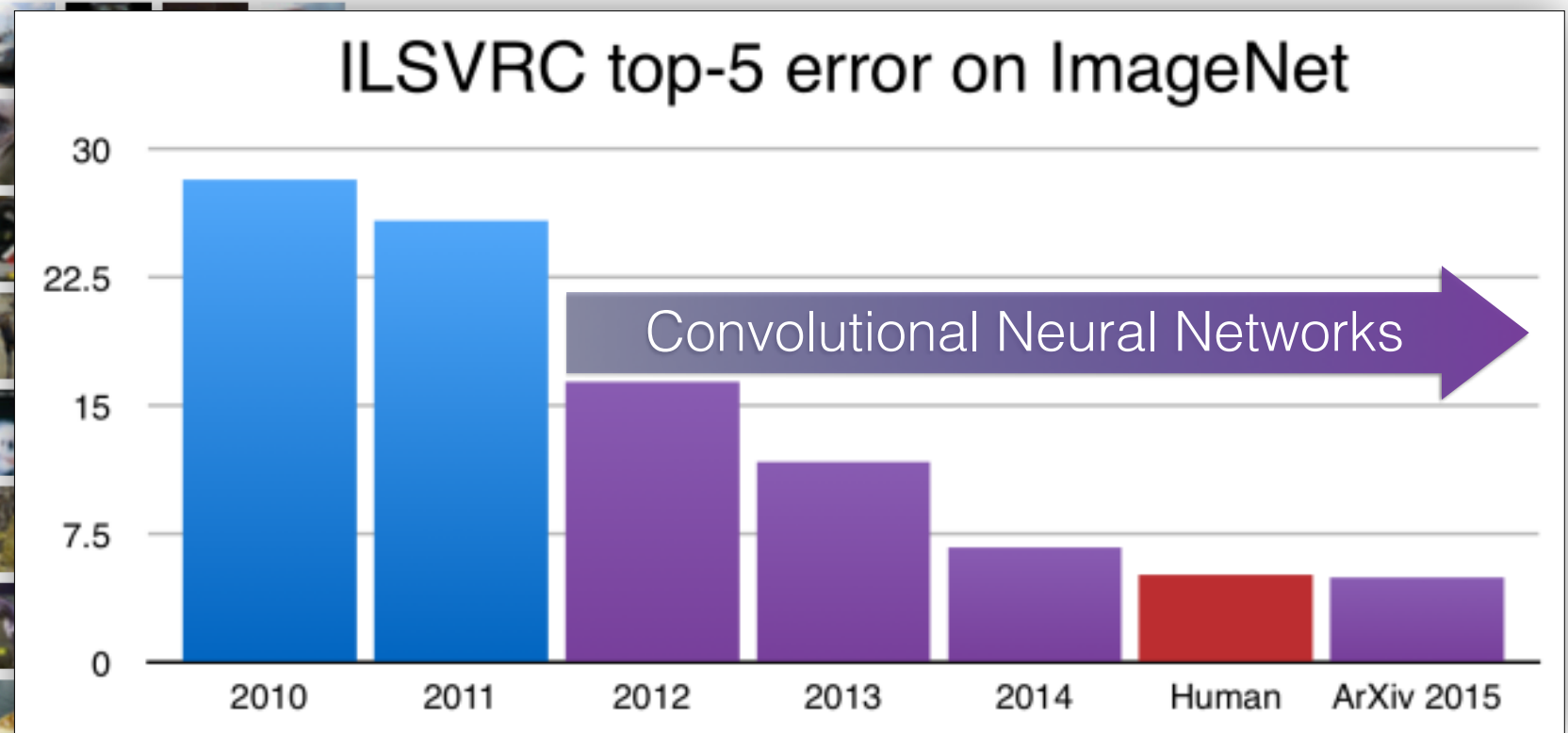
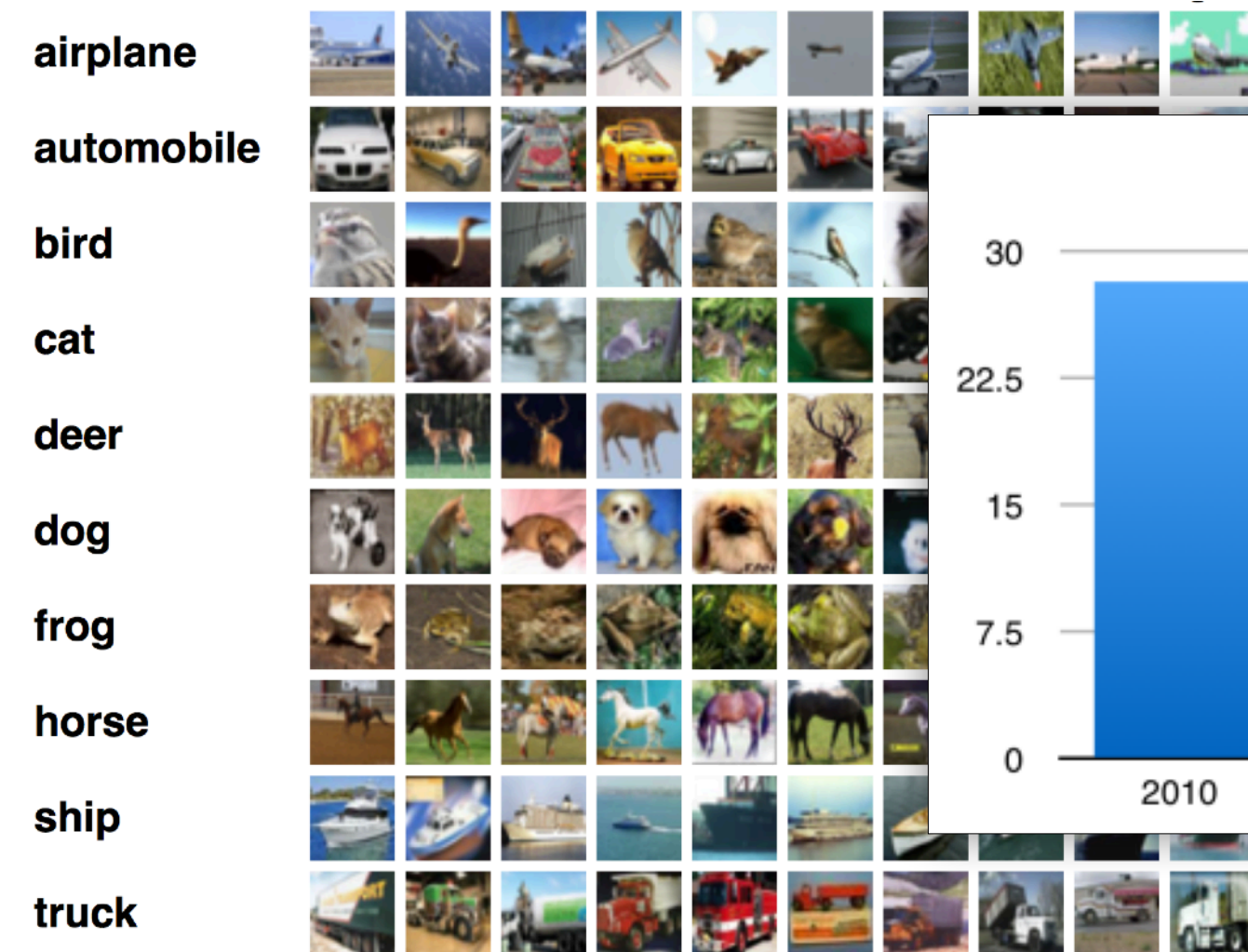




# Deep Learning



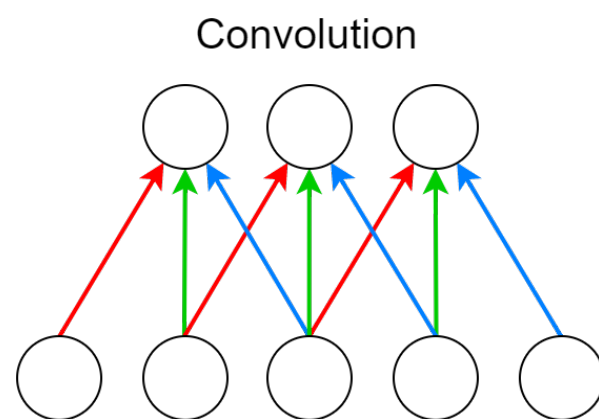
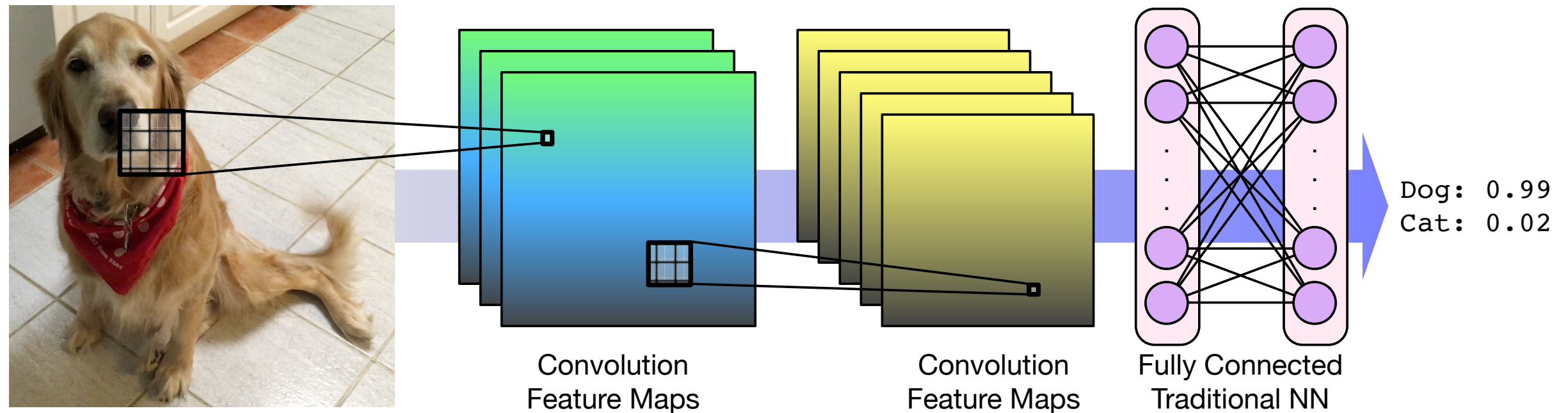
# Image Recognition



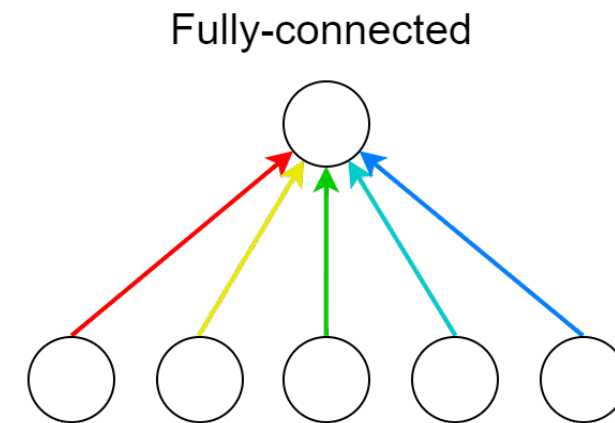
<https://devblogs.nvidia.com>



# Convolutional Neural Networks

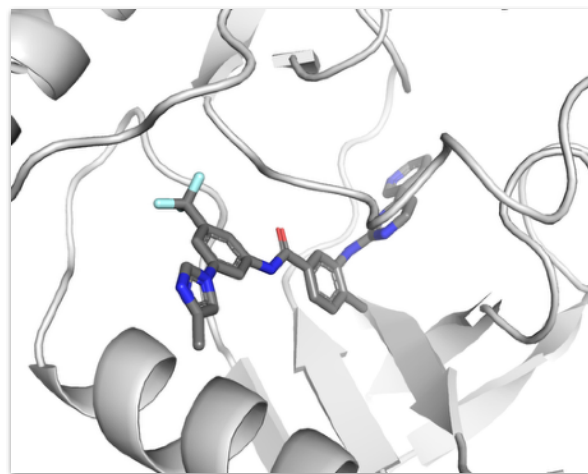


— weight 1  
— weight 2  
— weight 3



— weight 1  
— weight 2  
— weight 3  
— weight 4  
— weight 5

# CNNs for Protein-Ligand Scoring

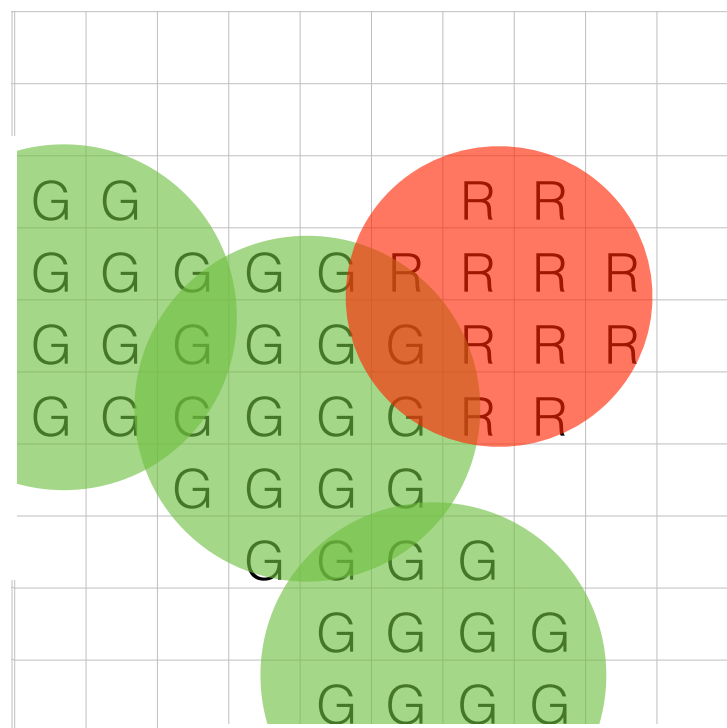


Pose Prediction

Binding  
Discrimination

Affinity Prediction

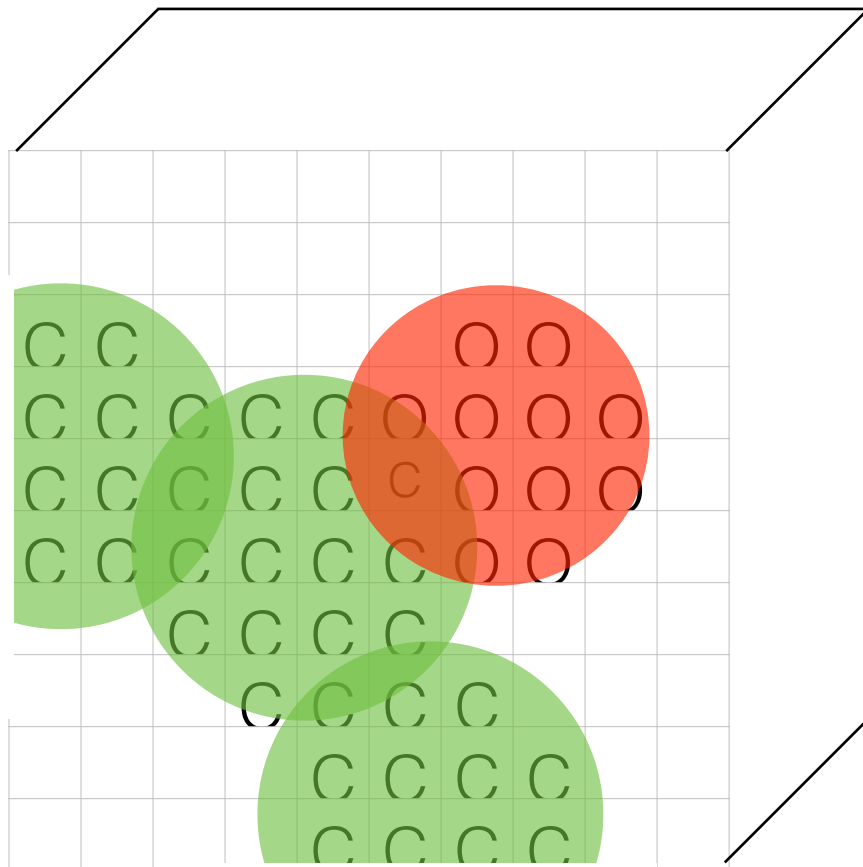
# Protein-Ligand Representation



(R,G,B) pixel



# Protein-Ligand Representation

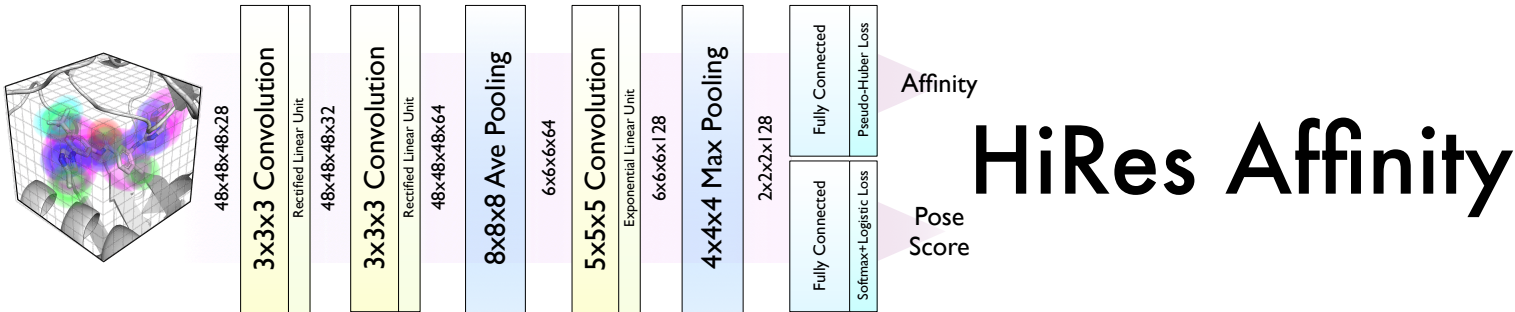
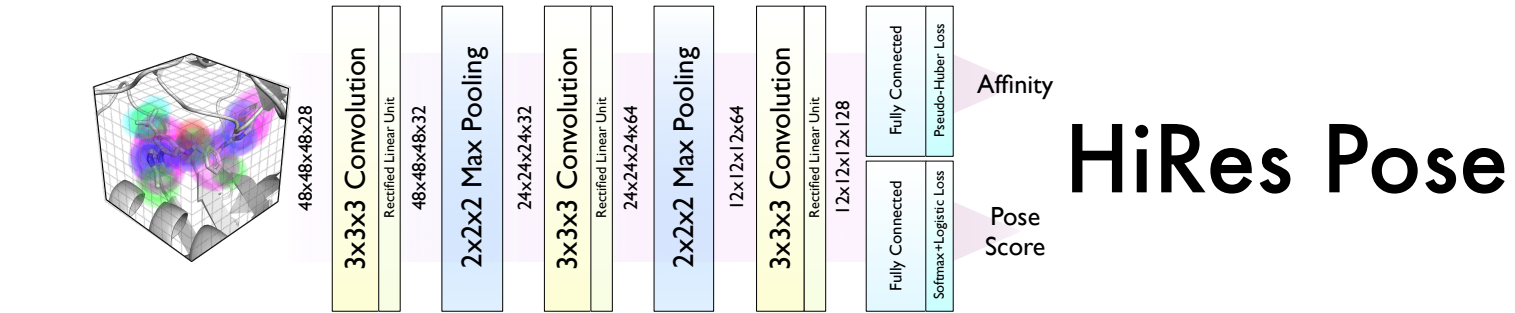
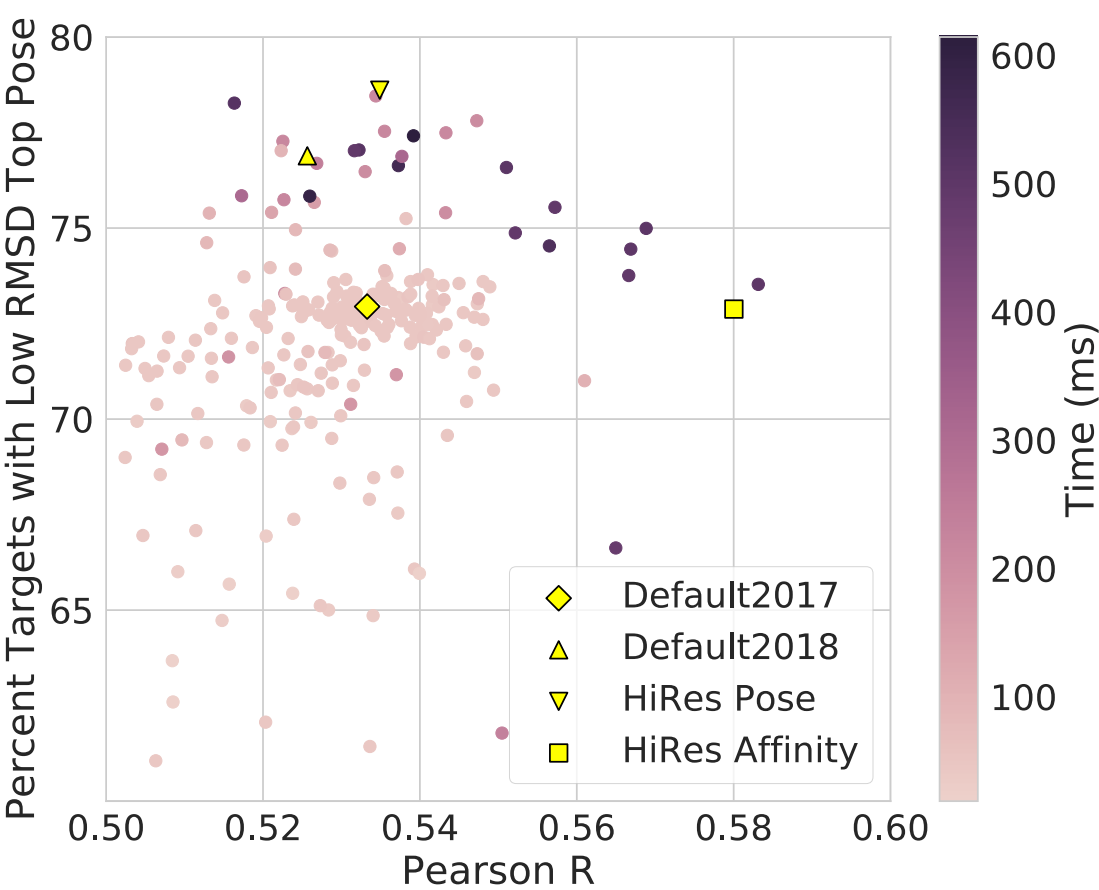


(R,G,B) pixel →

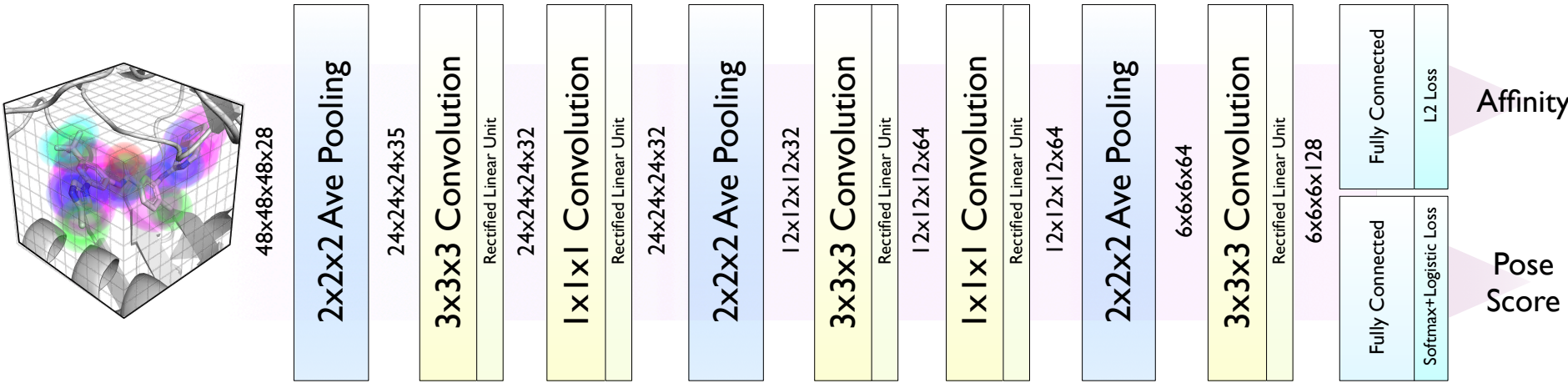
(Carbon, Nitrogen, Oxygen,...) **voxel**

The only parameters for this representation are the choice of **grid resolution**, **atom density**, and **atom types**.

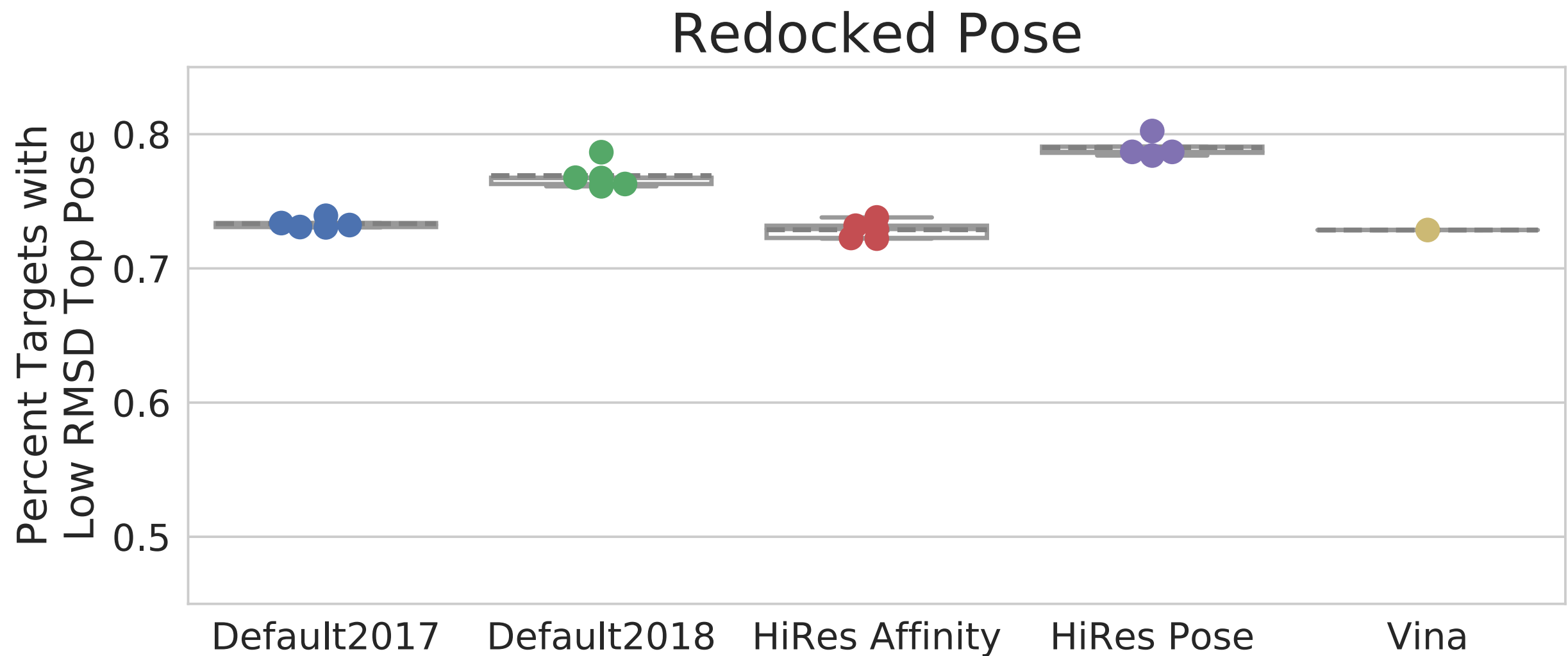
# Optimized Models



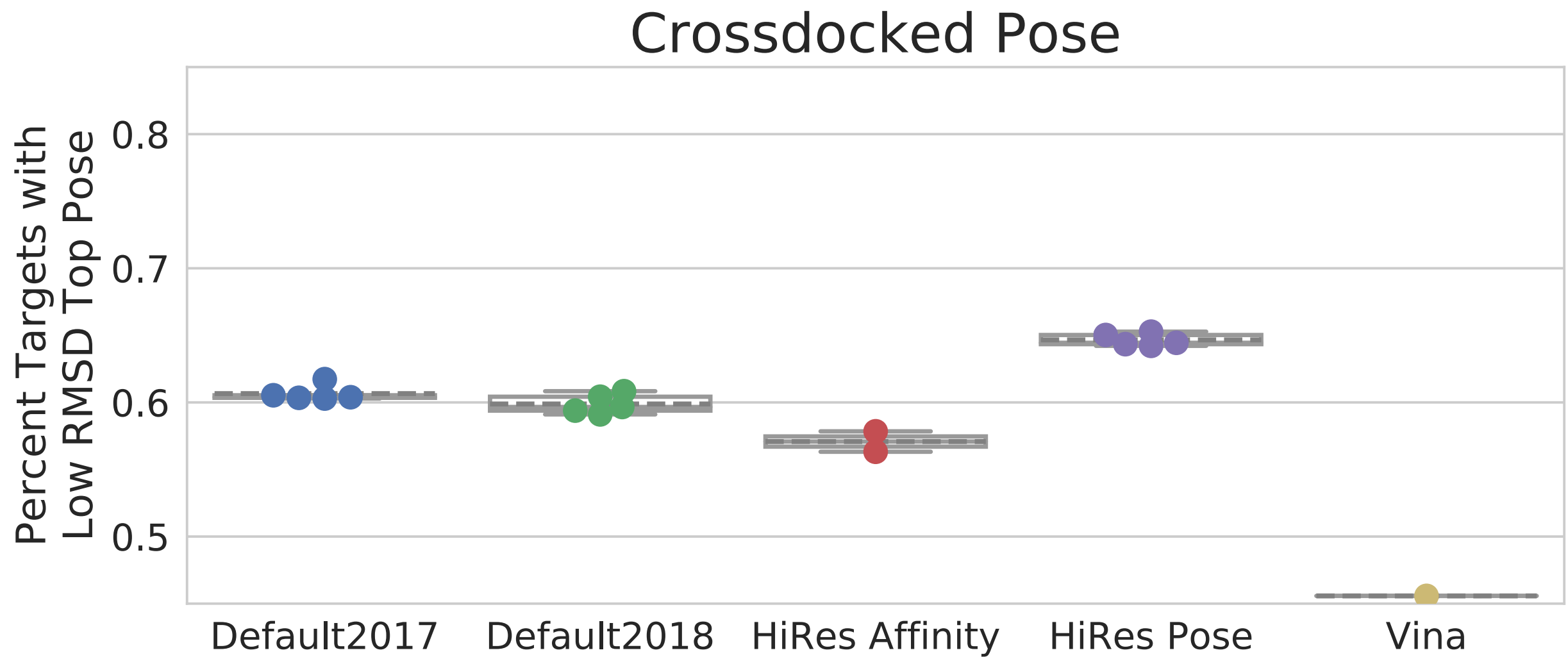
## Default2018



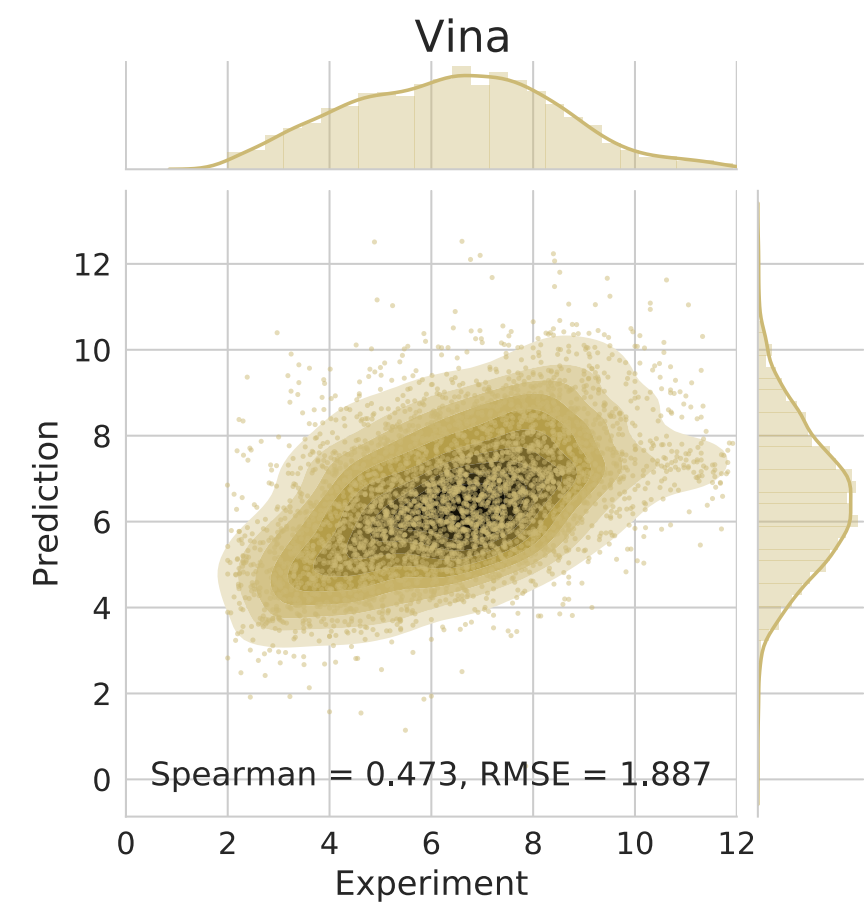
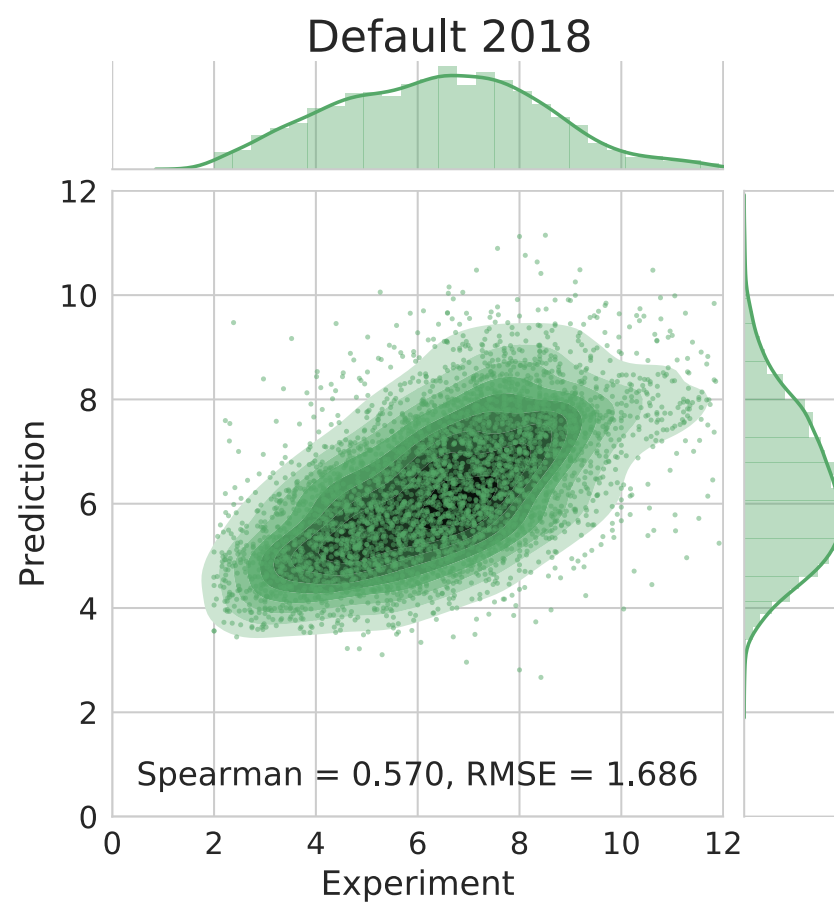
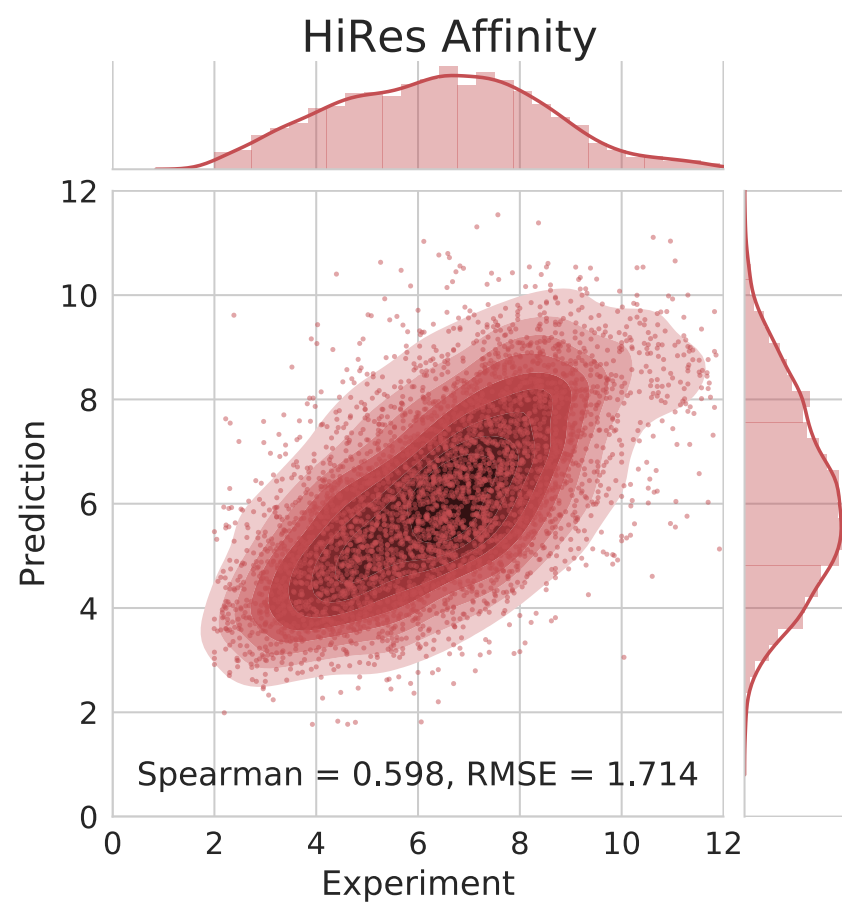
# Pose Results



# Pose Results

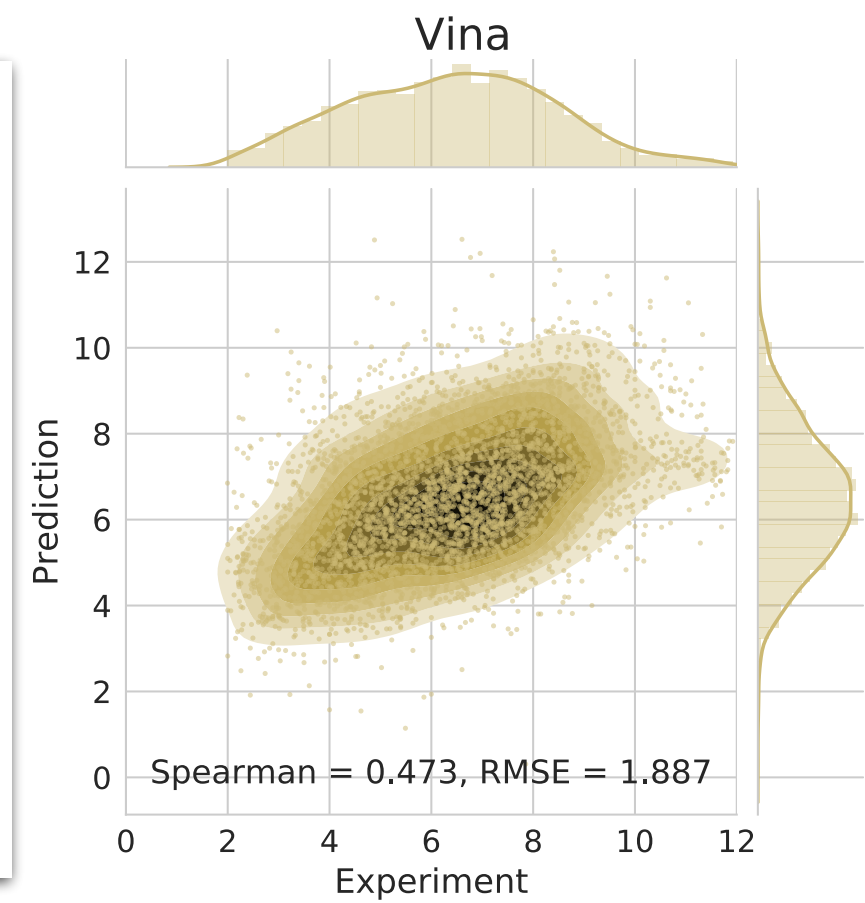
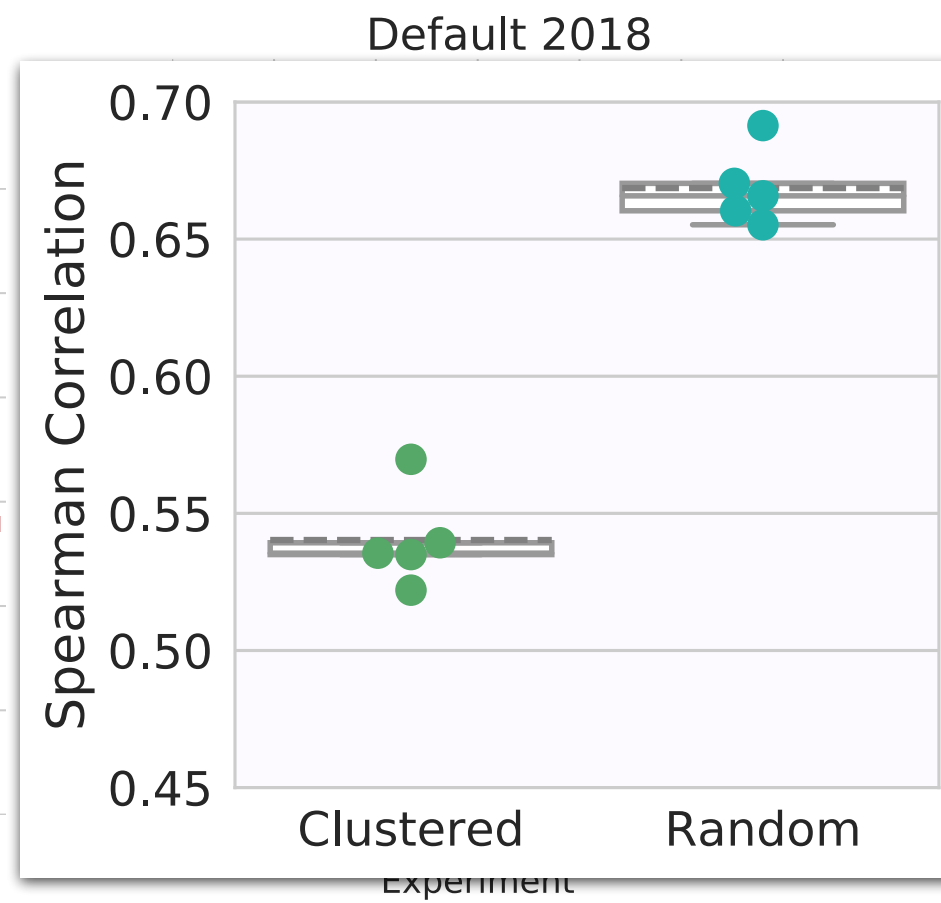
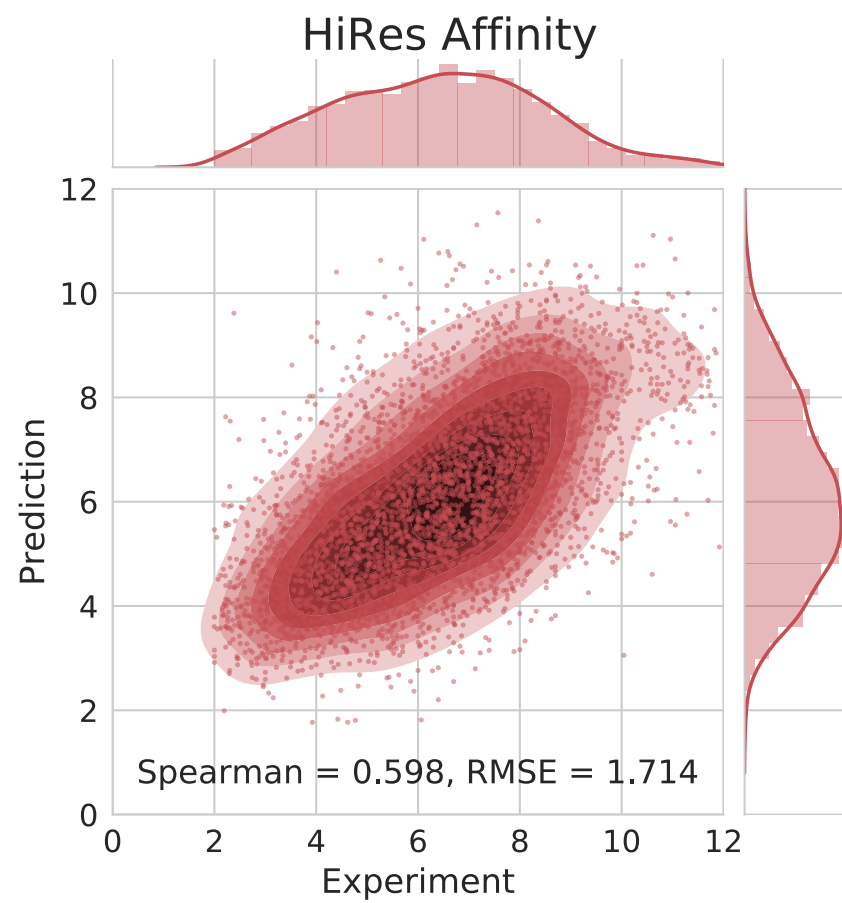


# Affinity Results

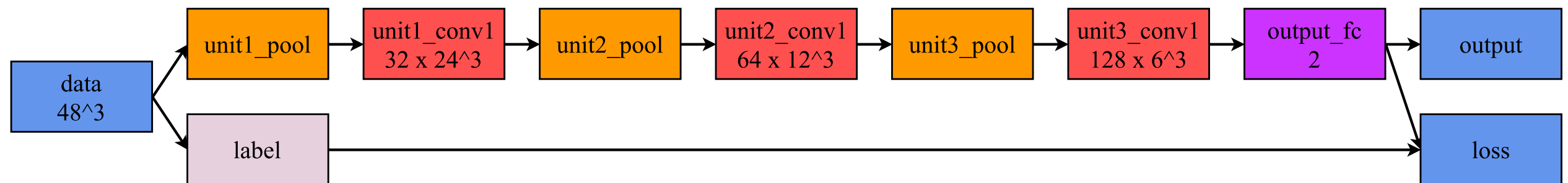




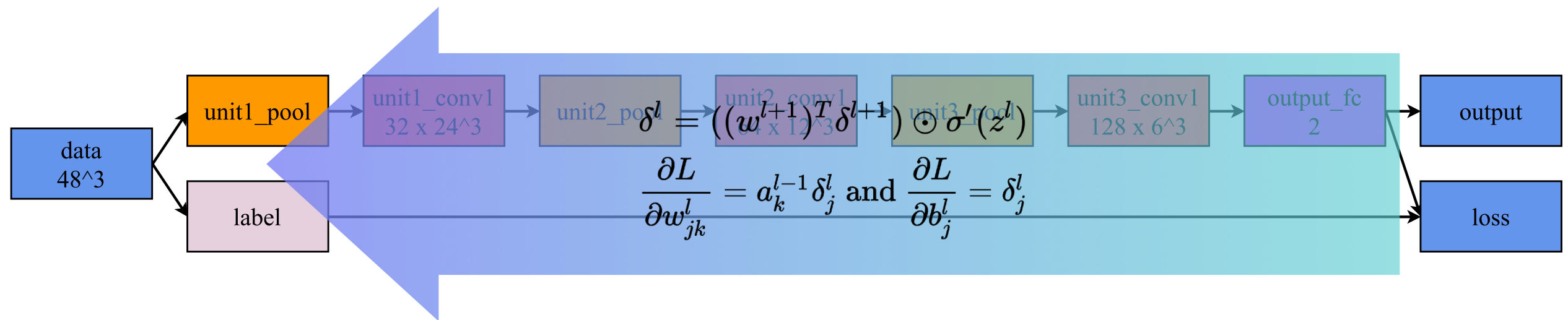
# Affinity Results



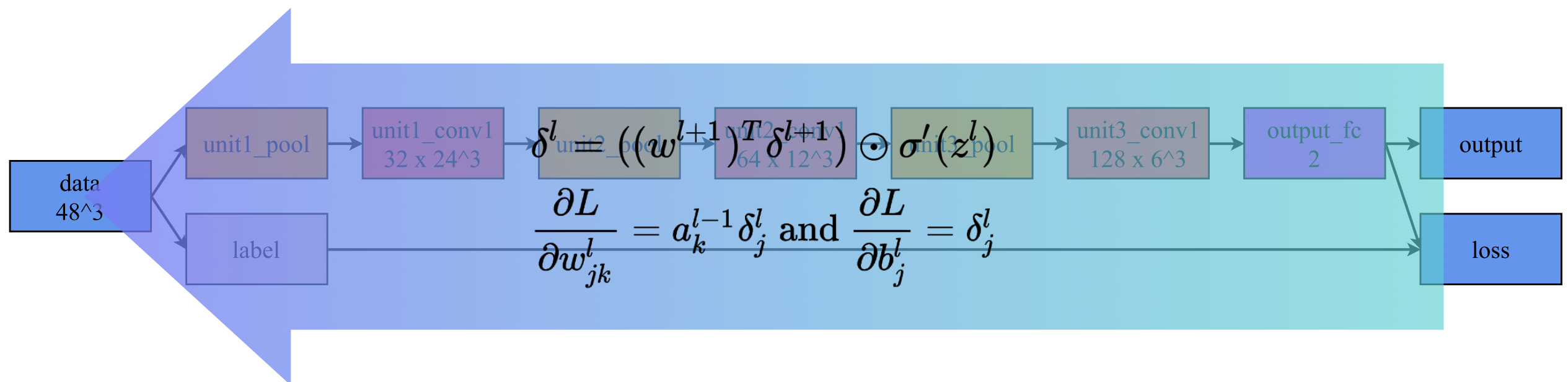
# Beyond Scoring



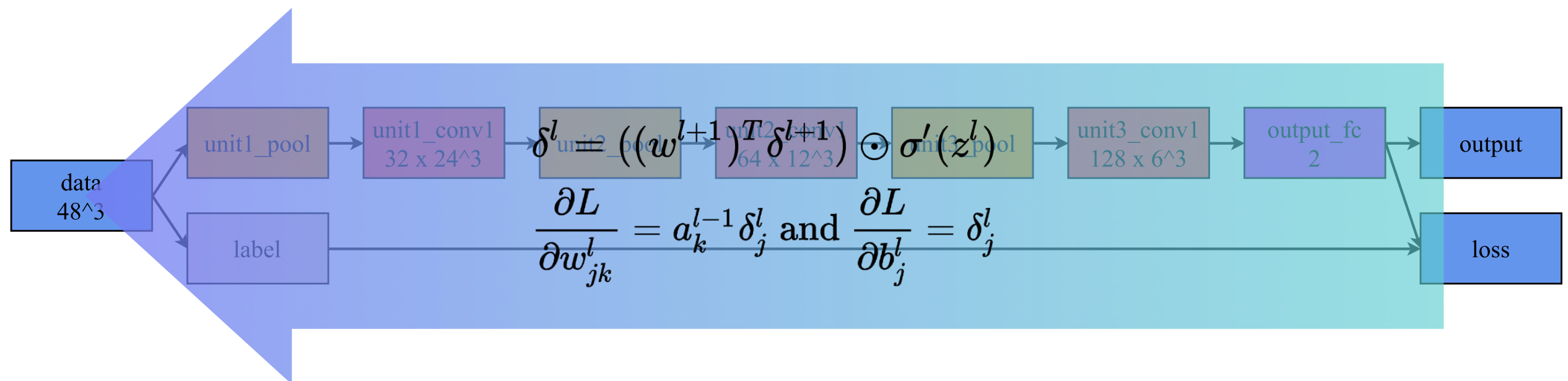
# Beyond Scoring



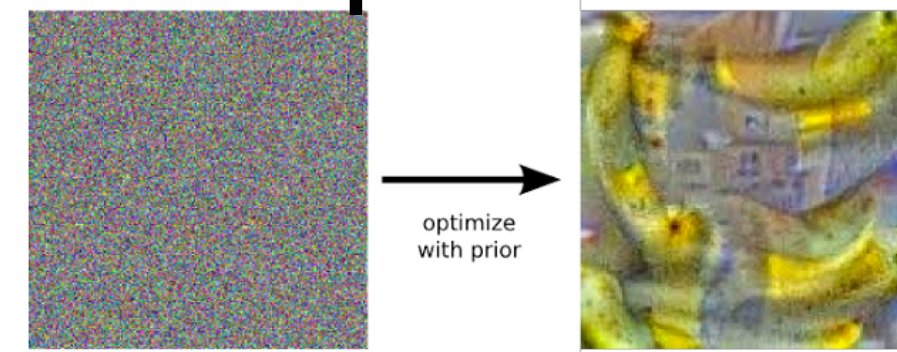
# Beyond Scoring



# Beyond Scoring

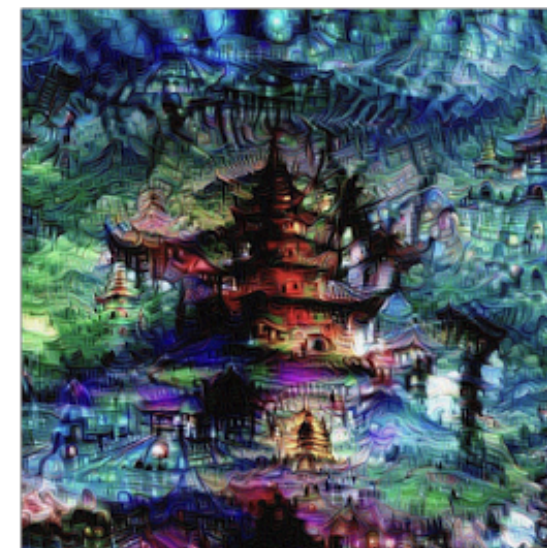
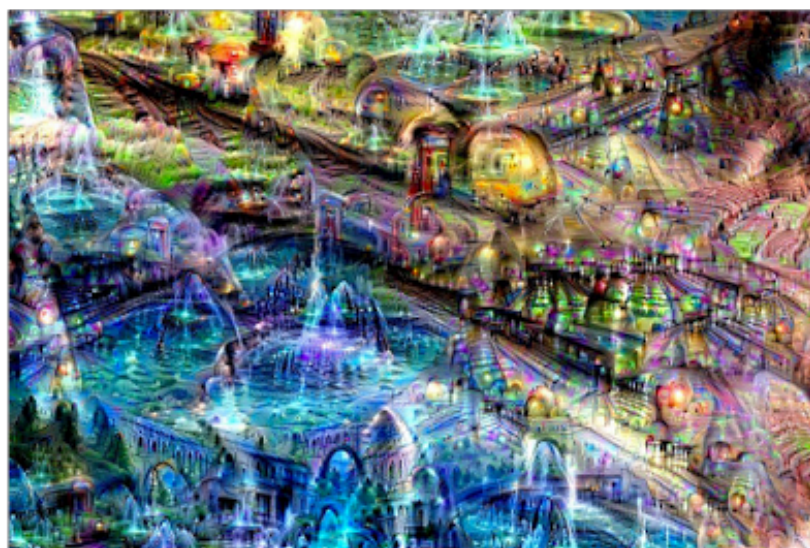
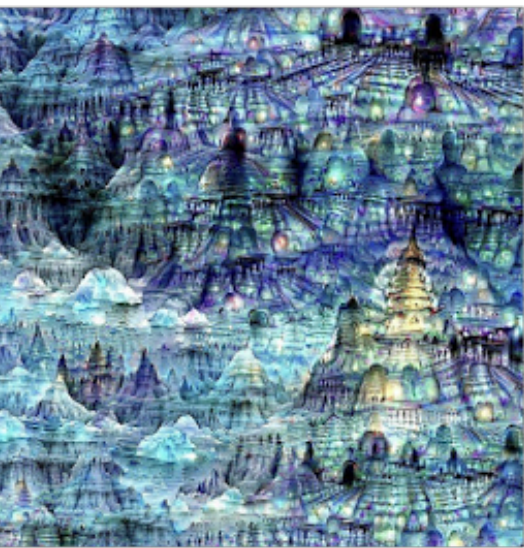
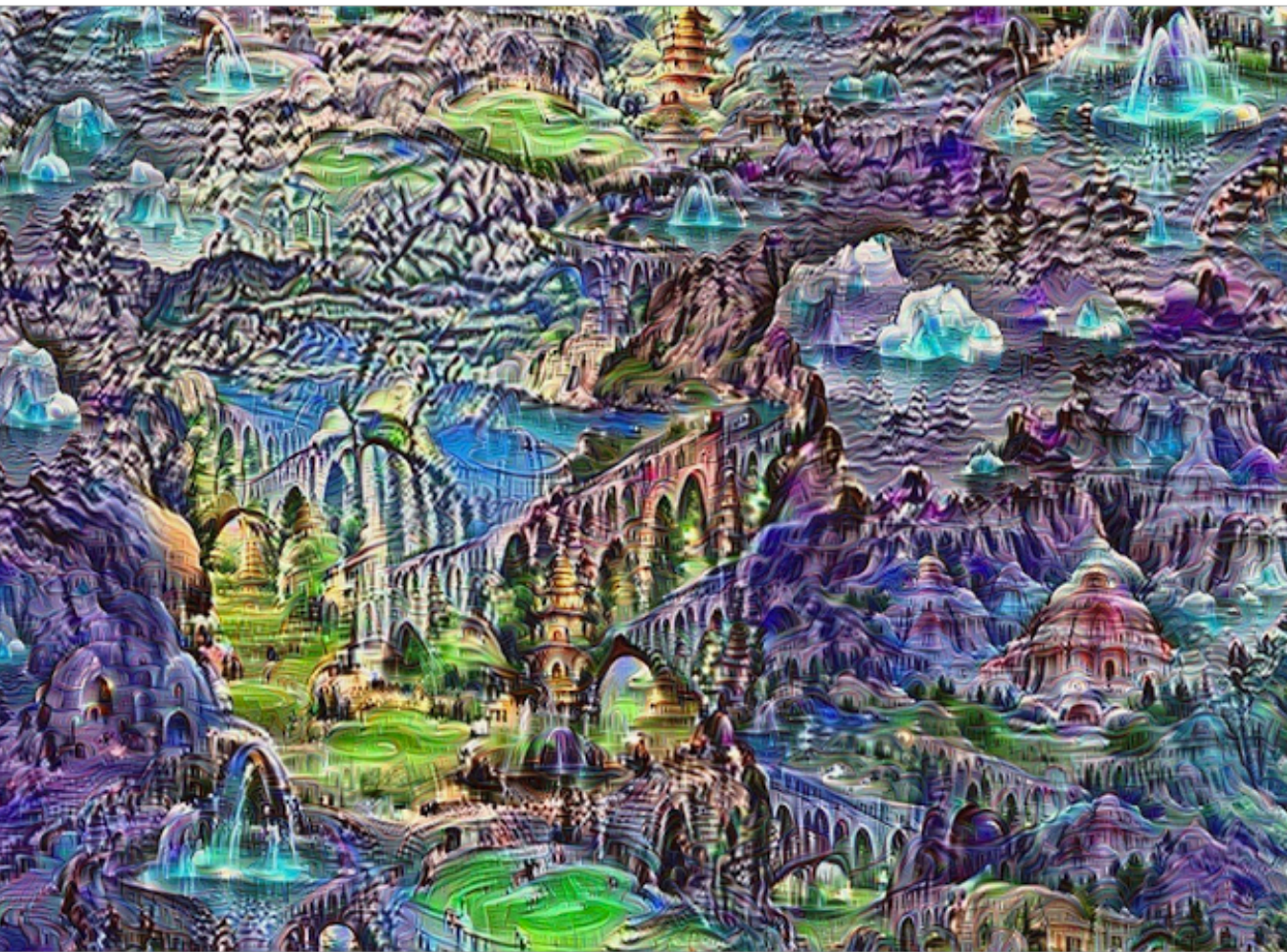


## Deep Dreams



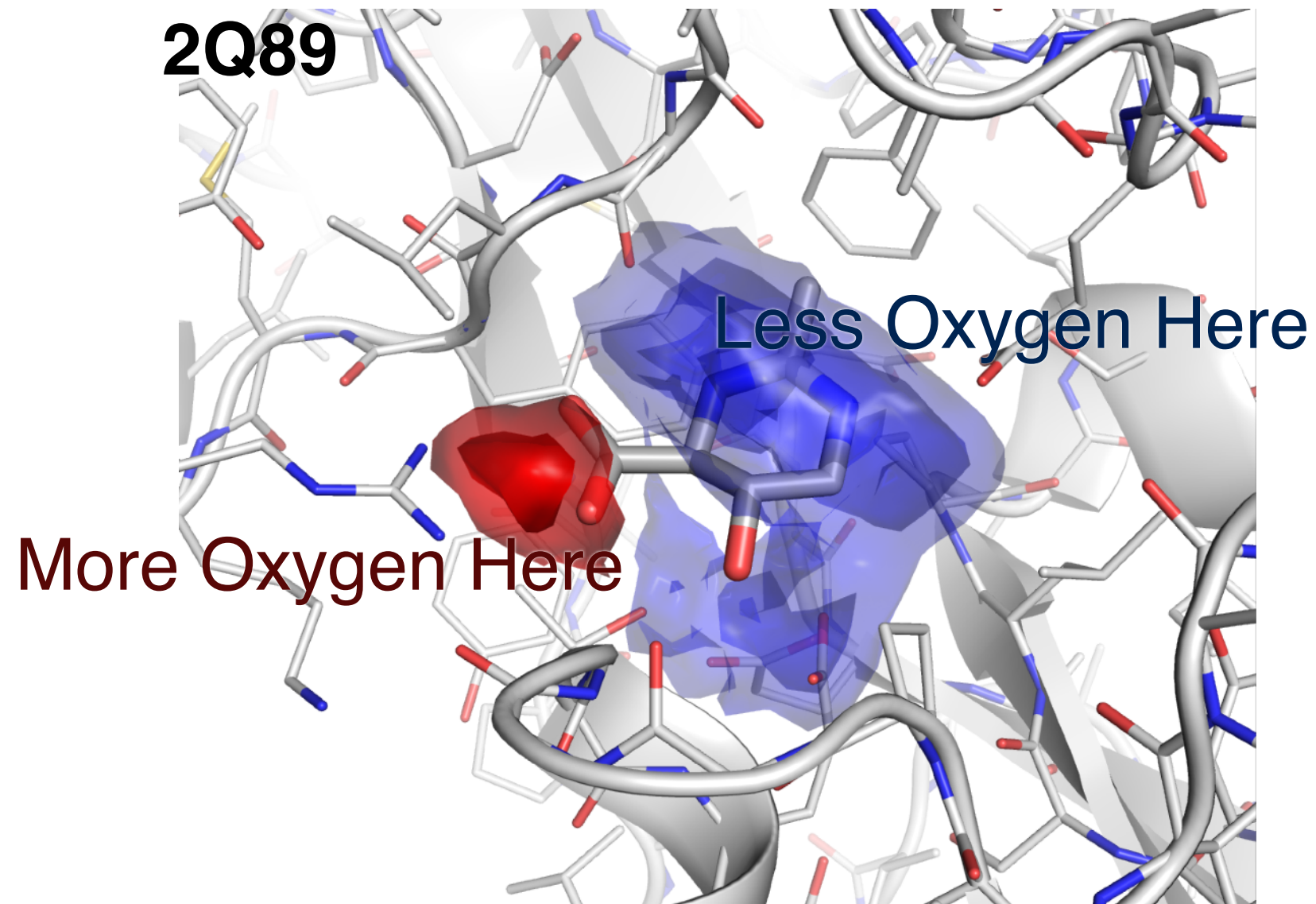
<https://research.googleblog.com/2015/06/inceptionism-going-deeper-into-neural.html>



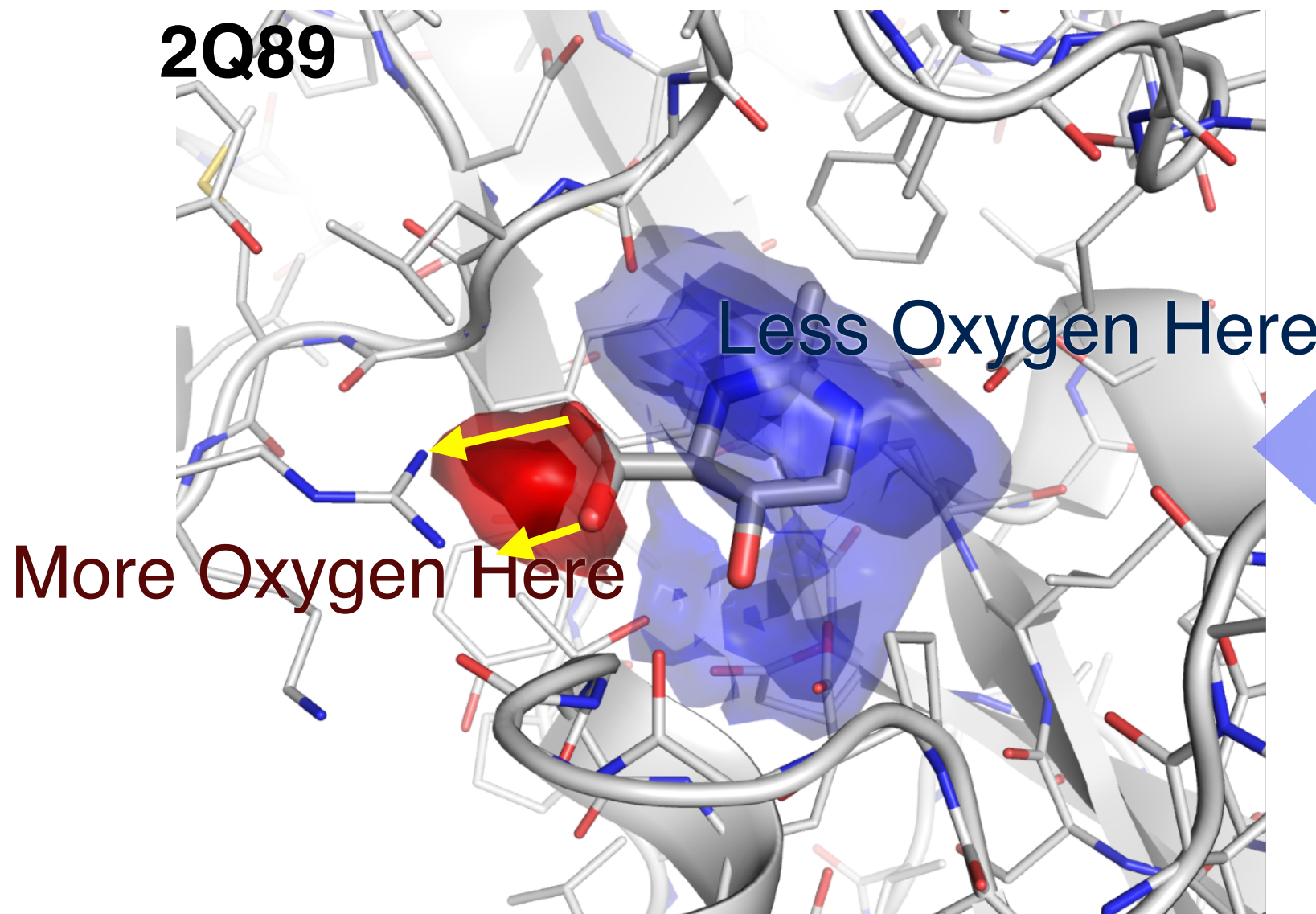




# Beyond Scoring



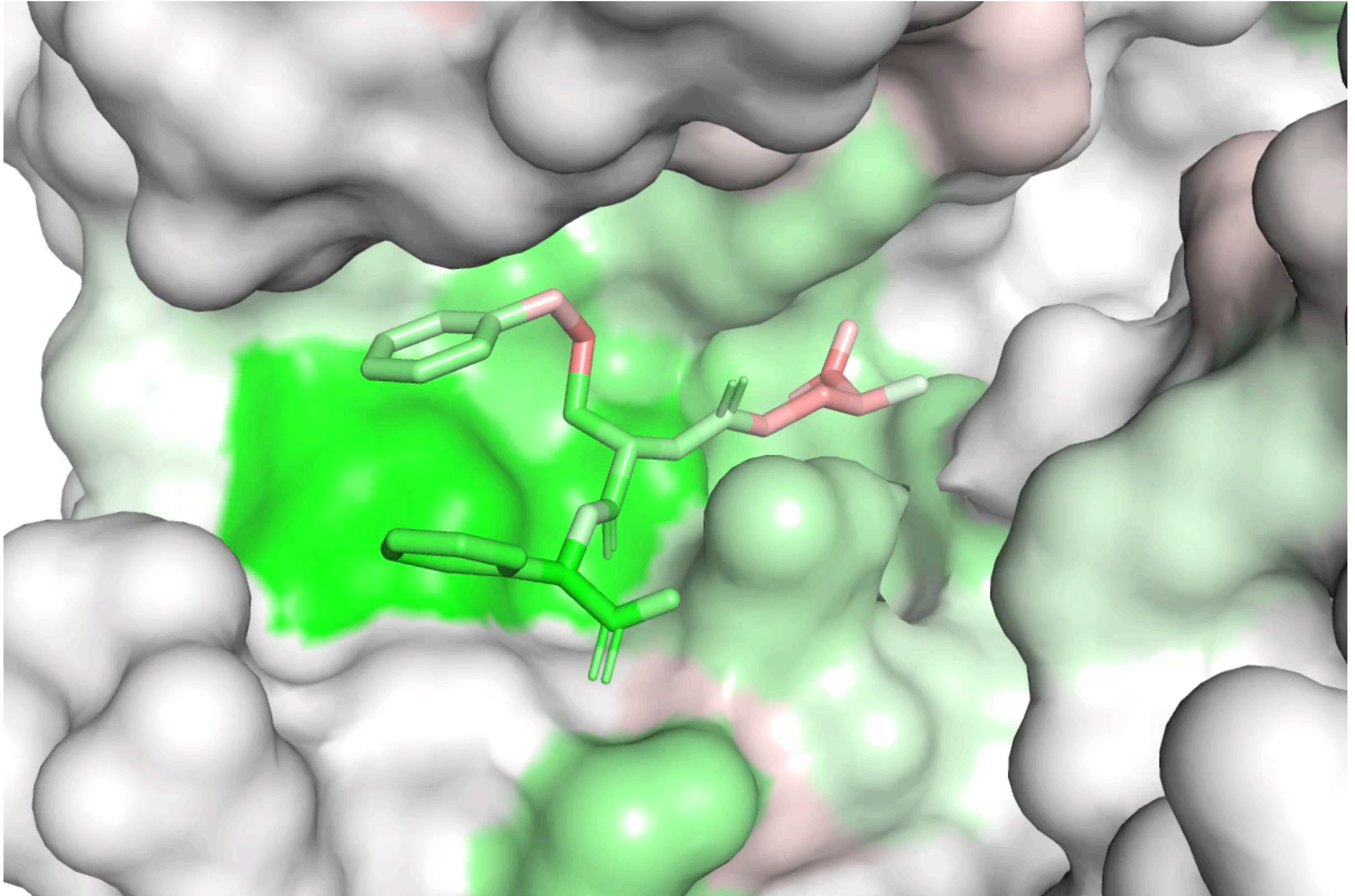
# Beyond Scoring



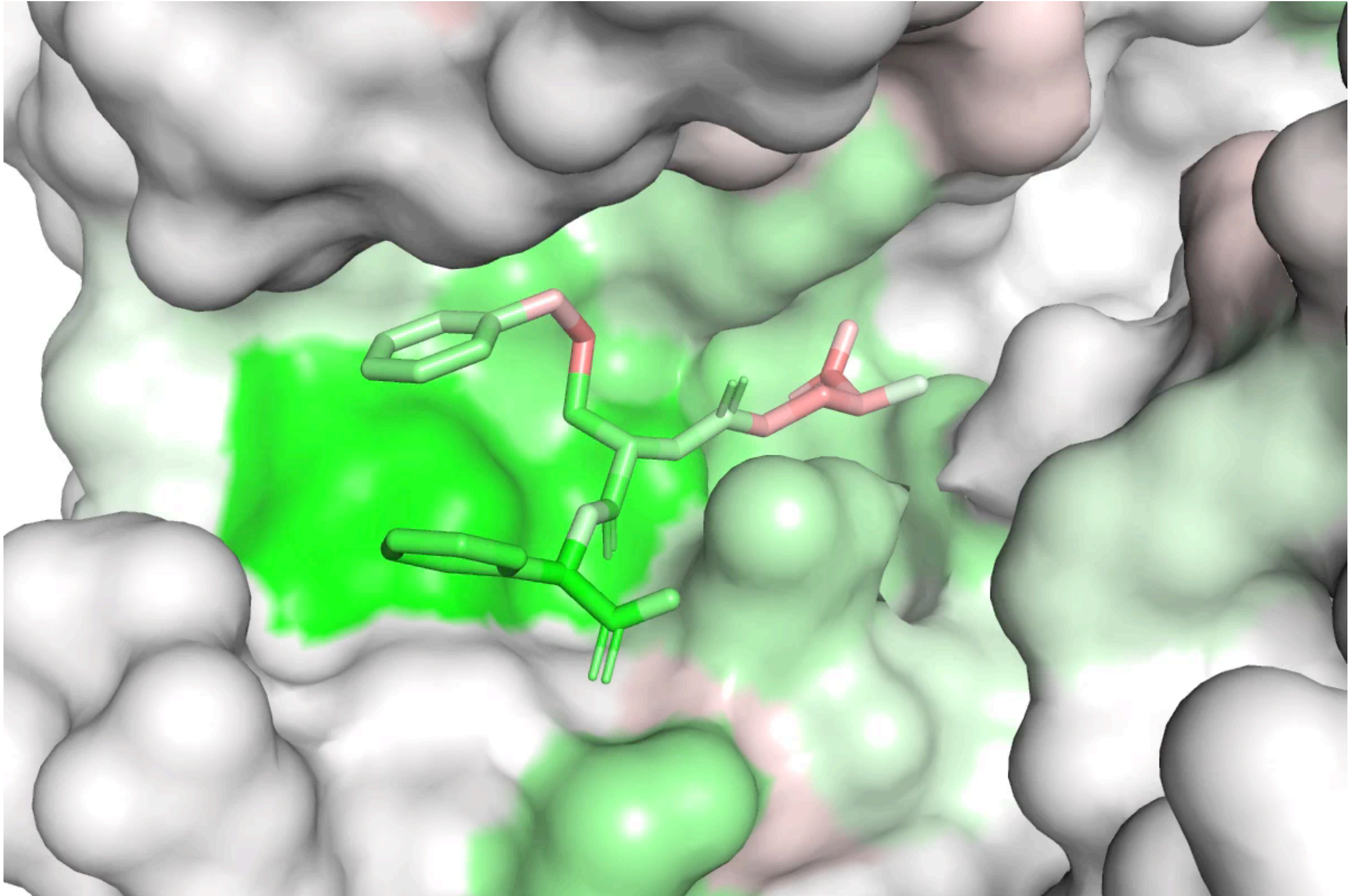
$$\frac{\partial L}{\partial A} = \sum_{i \in G_A} \frac{\text{data}_{i \in G_A} \frac{\partial L}{\partial G_i}}{\frac{\partial G_i}{\partial D} \frac{\partial D}{\partial A}}$$

unit1\_pool

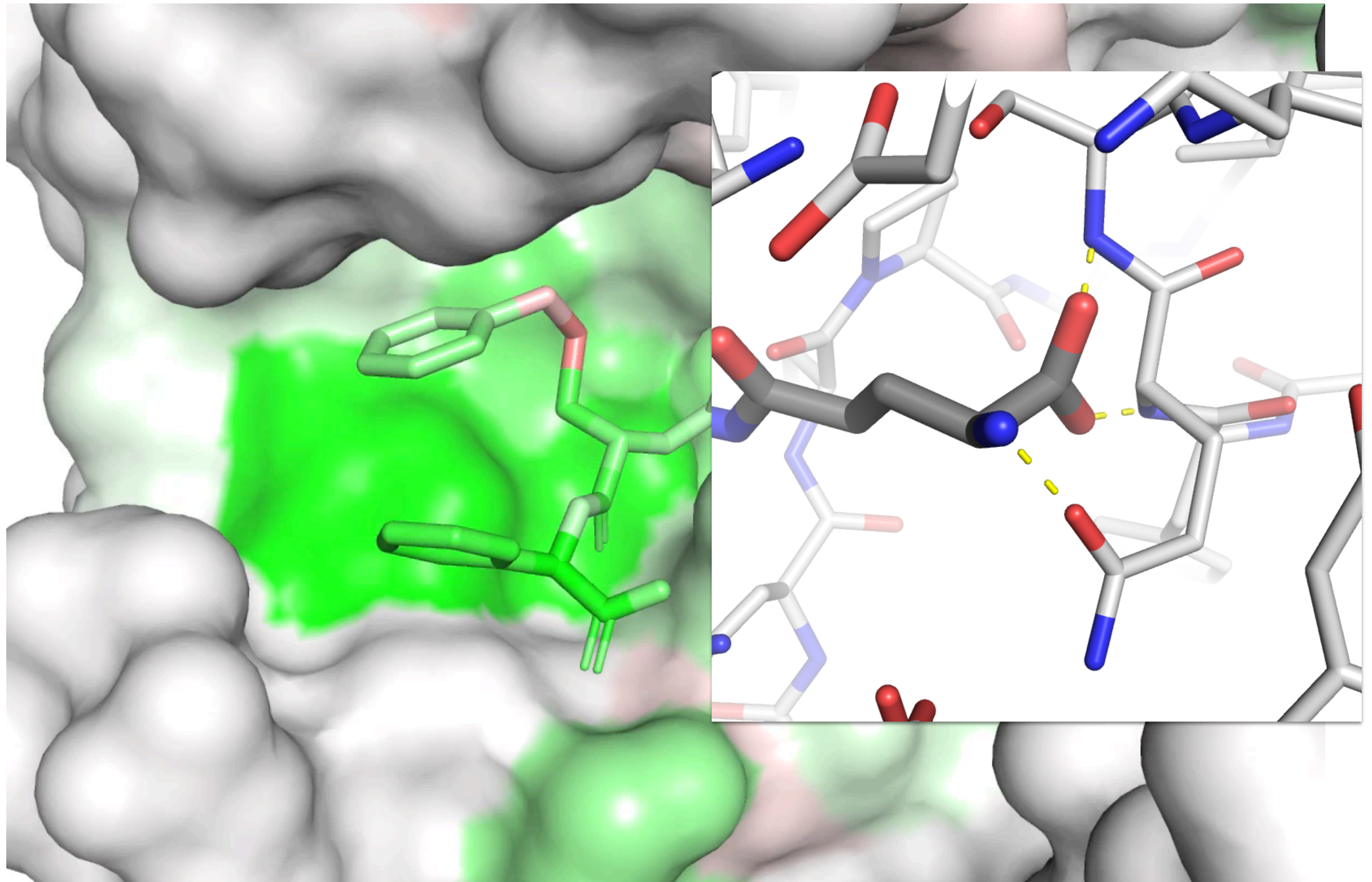
label

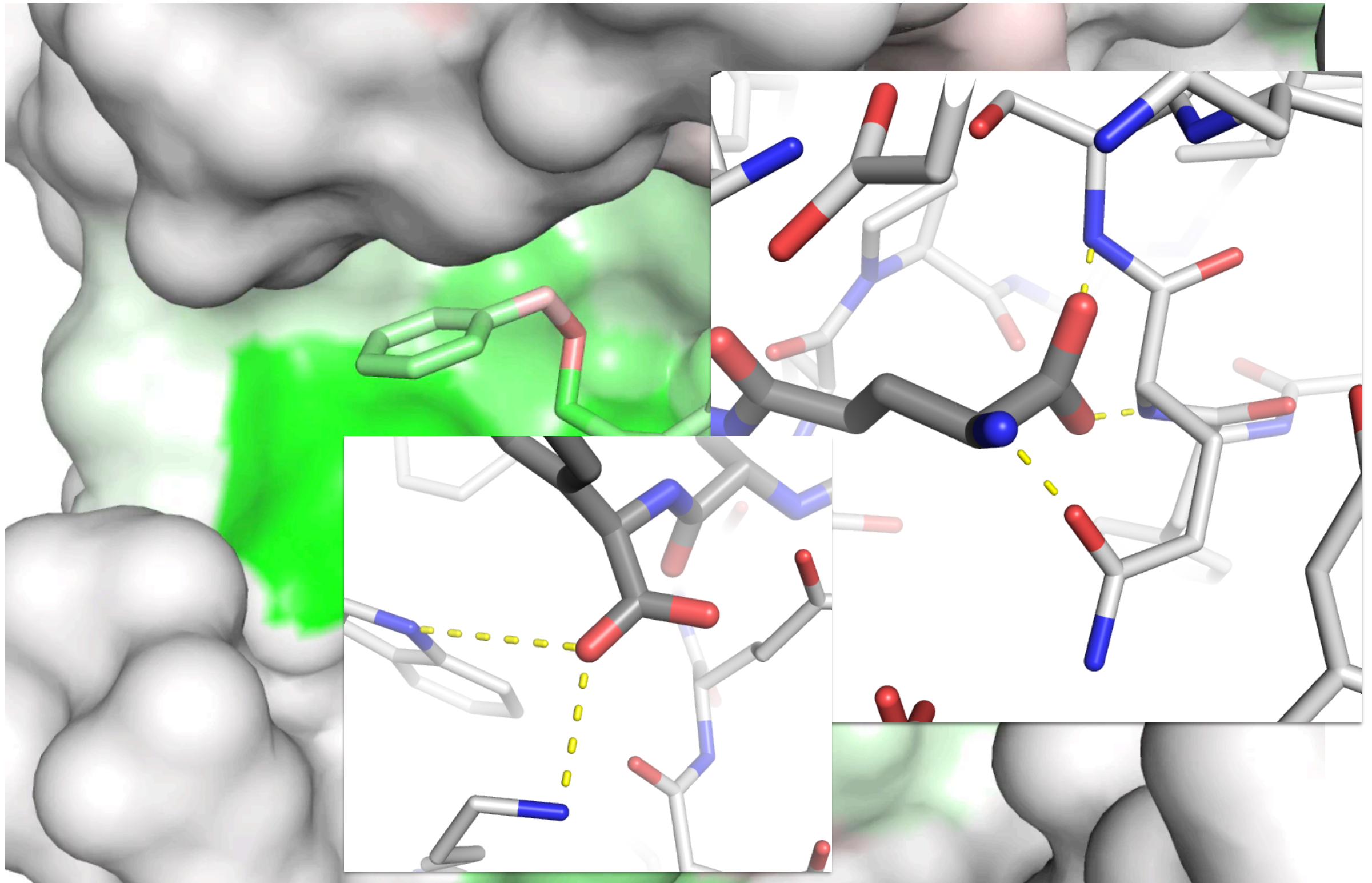




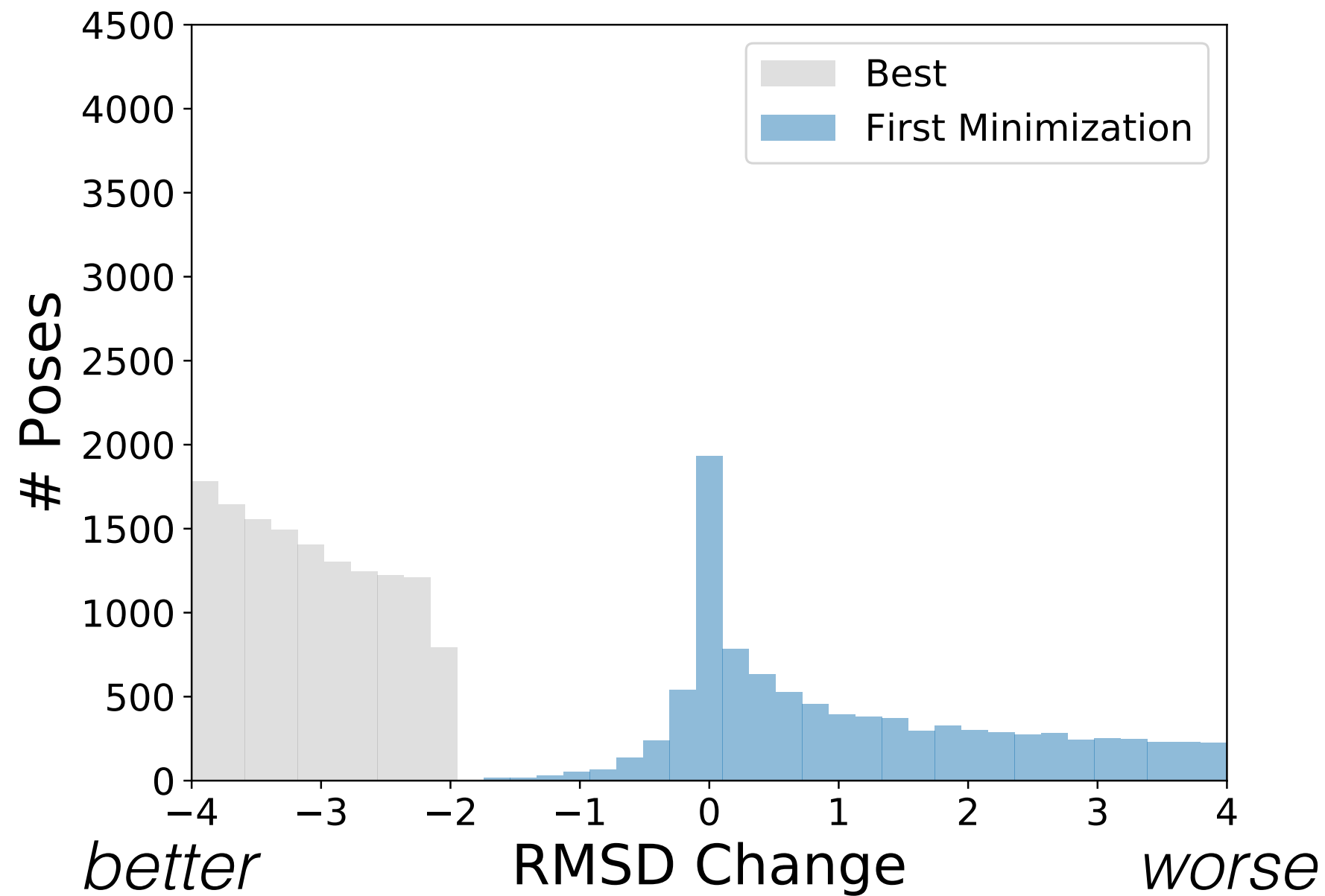






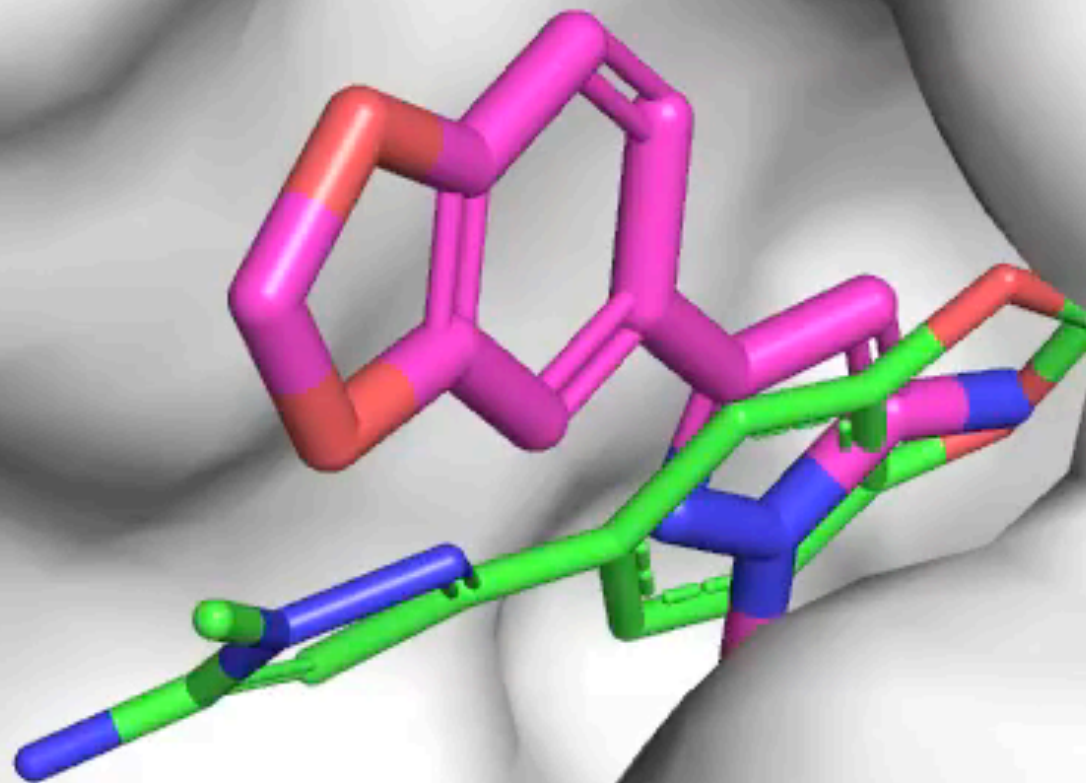


# Minimizing Low RMSD Poses



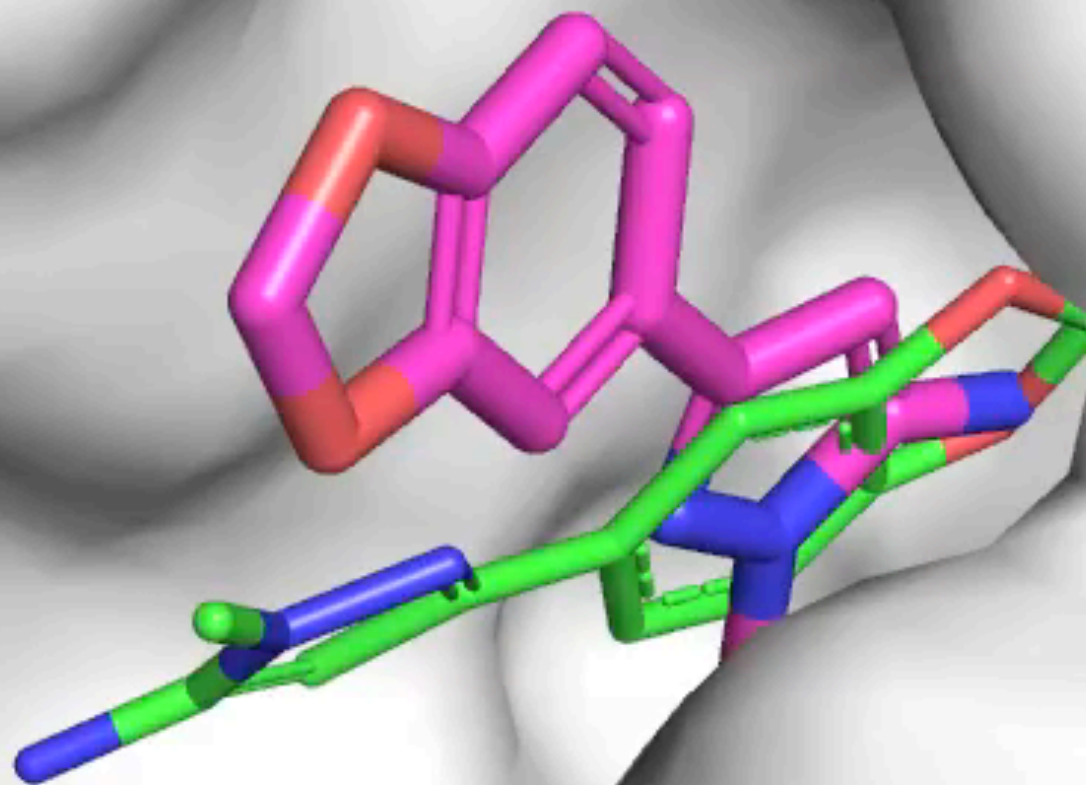


**3AO4**

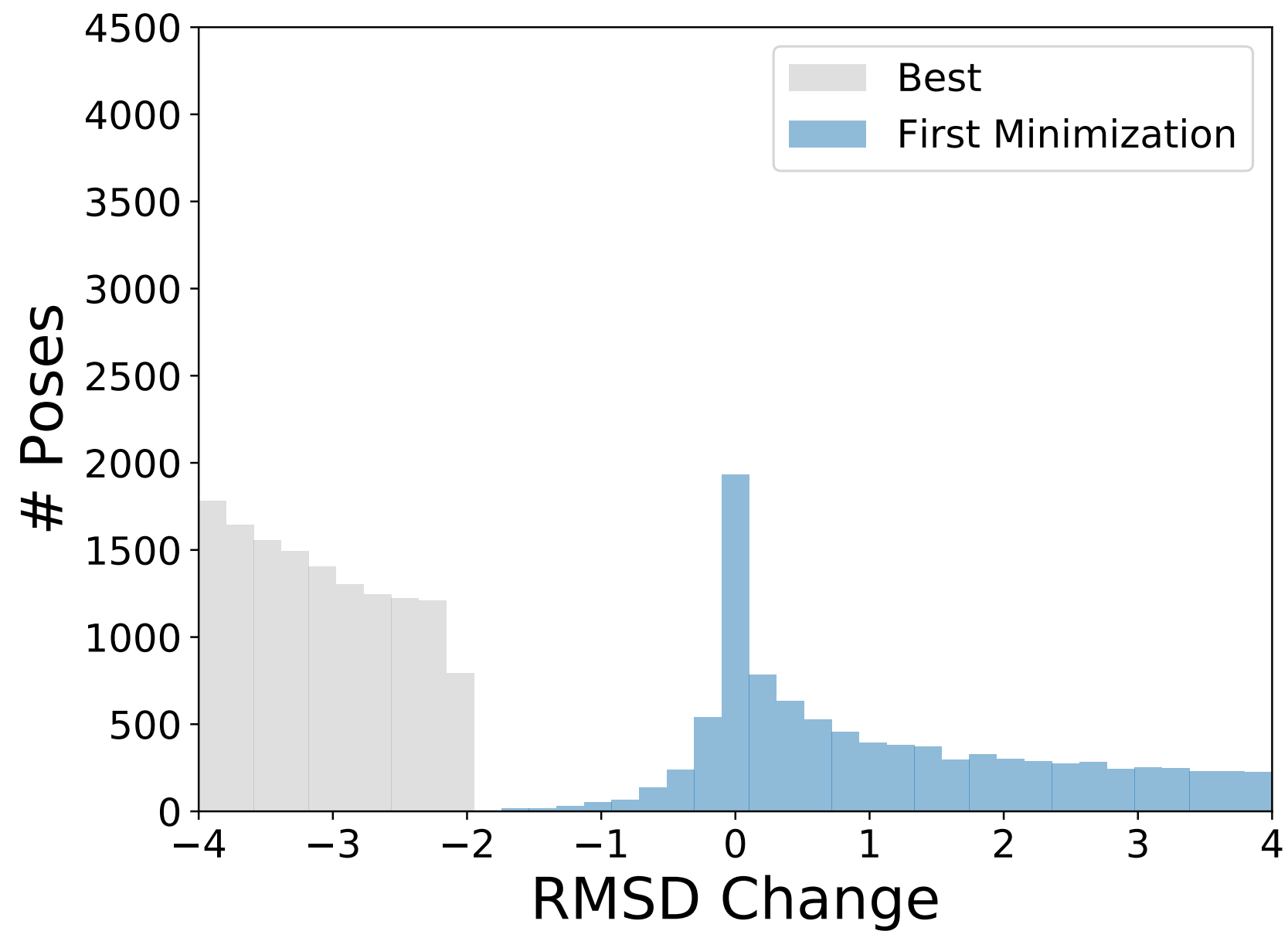




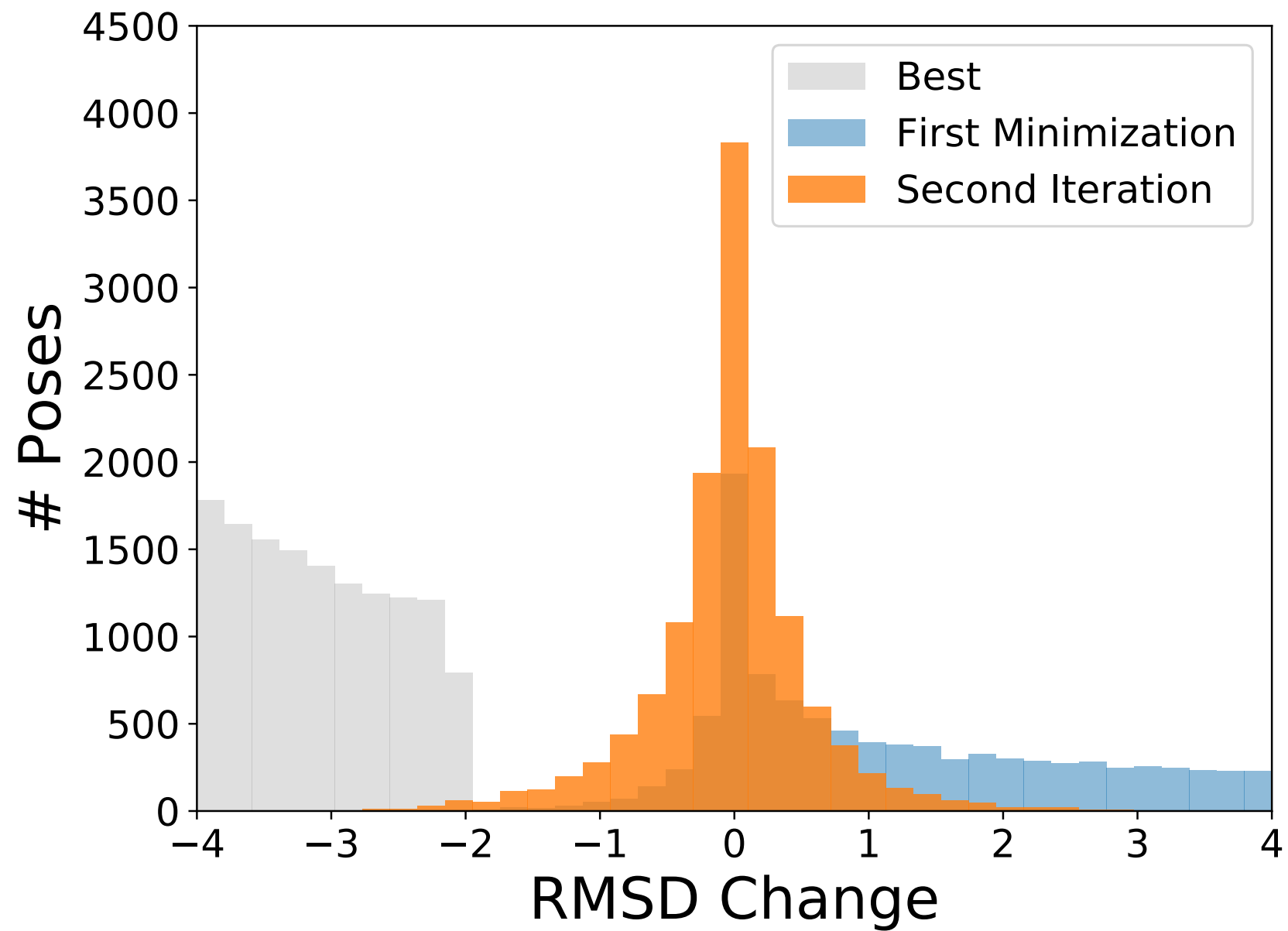
**3AO4**



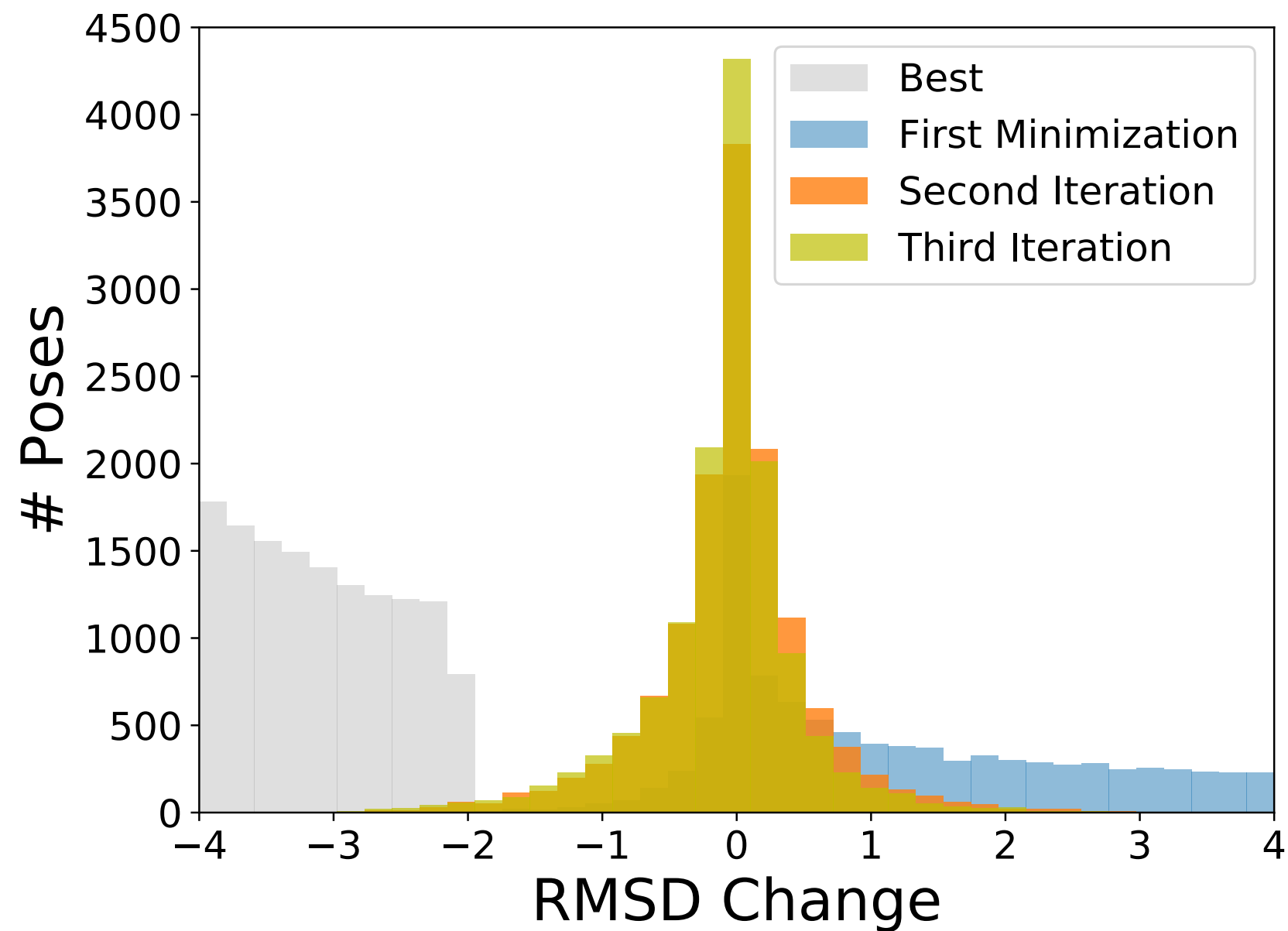
# Iterative Refinement



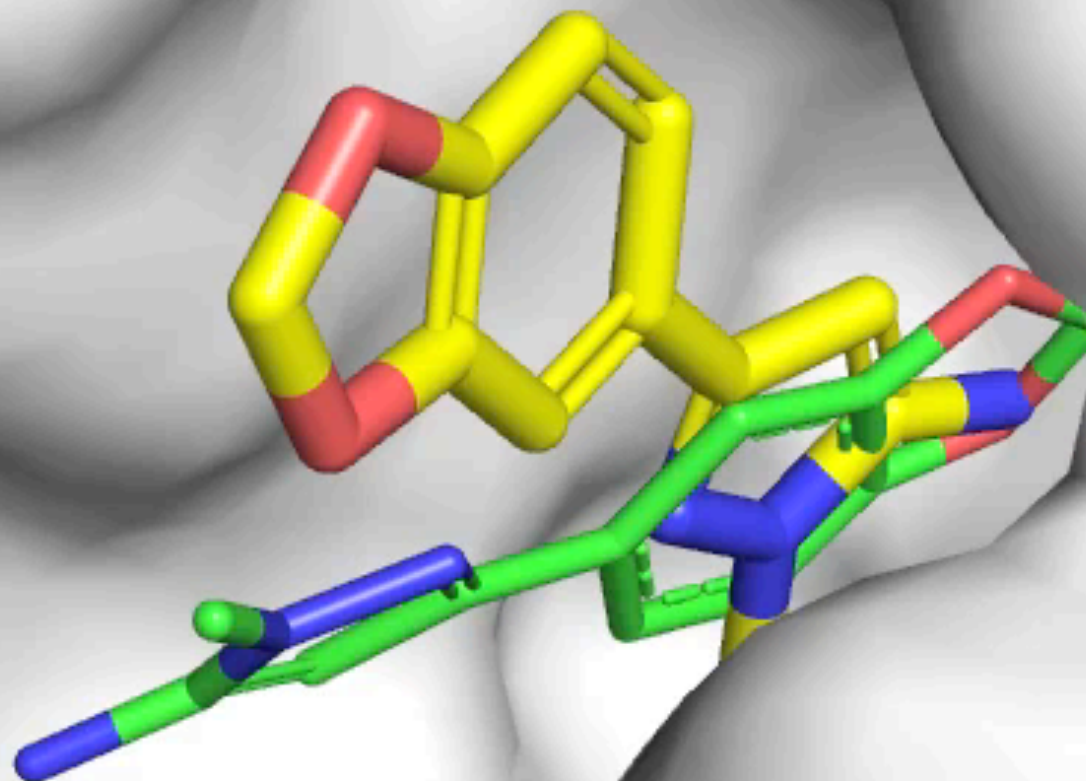
# Iterative Refinement

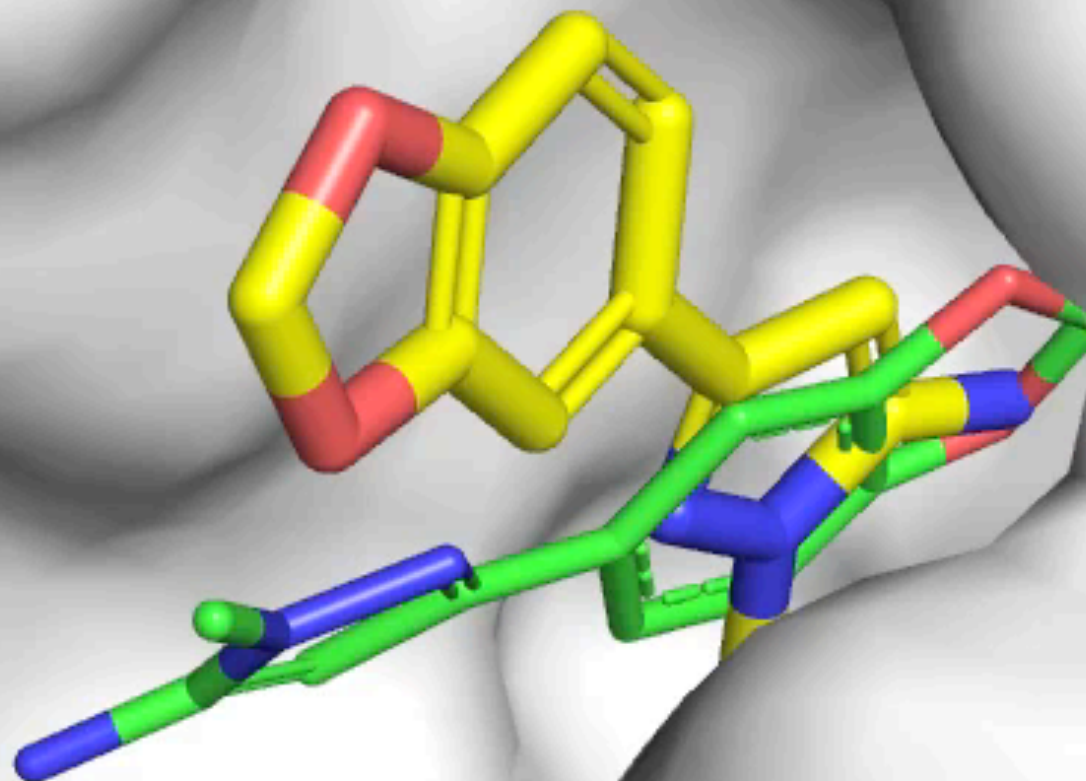


# Iterative Refinement





**3AO4**

**3AO4**

# Related Work

## MolecuLeNet: A continuous-filter convolutional neural network for modeling quantum interactions

[Kristof T. Schütt](#), [Pieter-Jan Kindermans](#), [Huziel E. Sauceda](#), [Stefan Chmiela](#), [Alexandre Tkatchenko](#), [Klaus-Robert Müller](#)

*(Submitted on 26 Jun 2017)*

## Automatic chemical design using a data-driven continuous representation of molecules

[Rafael Gómez-Bombarelli](#), [David Duvenaud](#), [José Miguel Hernández-Lobato](#), [Jorge Aguilera-Iparraguirre](#), [Timothy D. Hirzel](#), [Ryan P. Adams](#), [Alán Aspuru-Guzik](#)

*(Submitted on 7 Oct 2016 (v1), last revised 6 Jan 2017 (this version, v2))*

## AtomNet: A Deep Convolutional Neural Network for Bioactivity Prediction in Structure-based Drug Discovery

[Izhar Wallach](#), [Michael Dzamba](#), [Abraham Heifets](#)

*(Submitted on 10 Oct 2015)*

## ANI-1: An extensible neural network potential with DFT accuracy at force field computational cost

[Justin S. Smith](#), [Olexandr Isayev](#), [Adrian E. Roitberg](#)

*(Submitted on 27 Oct 2016 (v1), last revised 6 Feb 2017 (this version, v4))*

## Convolutional Networks on Graphs for Learning Molecular Fingerprints

[David Duvenaud](#), [Dougal Maclaurin](#), [Jorge Aguilera-Iparraguirre](#), [Rafael Gómez-Bombarelli](#), [Timothy Hirzel](#), [Alán Aspuru-Guzik](#), [Ryan P. Adams](#)

*(Submitted on 30 Sep 2015 (v1), last revised 3 Nov 2015 (this version, v2))*

## Atomic Convolutional Networks for Predicting Protein-Ligand Binding Affinity

[Joseph Gomes](#), [Bharath Ramsundar](#), [Evan N. Feinberg](#), [Vijay S. Pande](#)

*(Submitted on 30 Mar 2017)*

## Deep Architectures and Deep Learning in Chemoinformatics: The Prediction of Aqueous Solubility for Drug-Like Molecules

[Alessandro Lusci](#)<sup>†‡</sup>, [Gianluca Pollastri](#)<sup>†</sup>, and [Pierre Baldi](#)<sup>†‡</sup>

<sup>†</sup> School of Computer Science and Informatics, University College Dublin, Belfield, Dublin 4, Ireland

<sup>‡</sup> Department of Computer Science, University of California, Irvine, Irvine, California 92697, United States

*J. Chem. Inf. Model.*, **2013**, 53 (7), pp 1563–1575

DOI: 10.1021/ci400187y

Publication Date (Web): June 24, 2013

## Low Data Drug Discovery with One-shot Learning

[Han Altae-Tran](#), [Bharath Ramsundar](#), [Aneesh S. Pappu](#), [Vijay Pande](#)


*(Submitted on 10 Nov 2016)*

## Massively Multitask Networks for Drug Discovery

[Bharath Ramsundar](#), [Steven Kearnes](#), [Patrick Riley](#), [Dale Webster](#), [David Konerding](#), [Vijay Pande](#)

*(Submitted on 6 Feb 2015)*

## Protein-Ligand Scoring with Convolutional Neural Networks

[Matthew Ragoza](#)<sup>†‡</sup>, [Joshua Hochuli](#)<sup>‡¶</sup>, [Elisa Idrobo](#)<sup>§</sup>, [Jocelyn Sunseri](#)<sup>¶</sup>, and [David Ryan Koes](#)<sup>†</sup> 

<sup>†</sup>Department of Neuroscience, <sup>‡</sup>Department of Computer Science, <sup>¶</sup>Department of Biological Sciences, and <sup>§</sup>Department of Computational and Systems Biology, University of Pittsburgh, Pittsburgh, Pennsylvania 15260, United States

<sup>§</sup> Department of Computer Science, The College of New Jersey, Ewing, New Jersey 08628, United States

*J. Chem. Inf. Model.*, **2017**, 57 (4), pp 942–957

DOI: 10.1021/acs.jcim.6b00740

Publication Date (Web): April 3, 2017

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 github.com/gnina

 http://bits.csb.pitt.edu

